



## **NCERT SOLUTIONS**

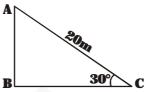
**Some Applications of Trigonometry** 

**<sup>\*</sup>Saral** हैं, तो शब शरल है।



## Ex - 9.1

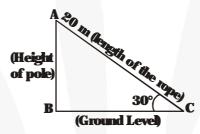
Q1. A circus artist is climbing a 20 m long rope, which is tightly stretched and tied from the top of a vertical pole to the ground. Find the height of the pole if the angle made by the rope with the ground level is 30° (see fig.).



**Sol.** AC = 20 m is the length of the rope.

Let AB = h metres be the height of the pole

$$\angle ACB = 30^{\circ}$$
 (Given)



Now, 
$$\frac{\mathbf{AB}}{\mathbf{AC}} = \sin 30^{\circ} = \frac{1}{2}$$
  $\Rightarrow$   $\frac{\mathbf{h}}{20} = \frac{1}{2}$   $\Rightarrow$   $\mathbf{h} = 10 \text{ m}$ 

- Q2. A tree breaks due to storm and the broken part bends so that the top of the trees touches the ground making an angle of 30° with the ground. The distance between the foot of the tree to the point where the top touches the ground is 8 m. Find the height of the tree.
- **Sol.** Let tree is broken at A and its top is touching the ground at B.

Now, in right 
$$\triangle AOB$$
, we have

$$\frac{\mathbf{AO}}{\mathbf{OB}} = \tan 30^{\circ}$$

$$\Rightarrow \frac{\mathbf{A0}}{\mathbf{8}} = \frac{\mathbf{1}}{\sqrt{\mathbf{3}}}$$

$$\Rightarrow \frac{\mathbf{A0}}{\mathbf{8}} = \frac{\mathbf{1}}{\sqrt{\mathbf{3}}} \Rightarrow AO = \frac{\mathbf{8}}{\sqrt{\mathbf{3}}} m$$

Also, 
$$\frac{\mathbf{AB}}{\mathbf{OB}} = \sec 30^{\circ}$$

$$\Rightarrow \frac{\mathbf{AB}}{\mathbf{8}} = \frac{\mathbf{2}}{\sqrt{\mathbf{3}}} \Rightarrow AB = \frac{\mathbf{2} \times \mathbf{8}}{\sqrt{\mathbf{3}}} = \frac{\mathbf{16}}{\sqrt{\mathbf{3}}} \,\mathrm{m}$$

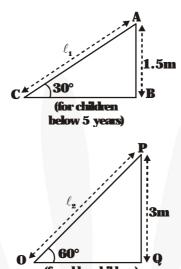
Now, height of the tree OP = OA + AB

$$=\frac{8}{\sqrt{3}}+\frac{16}{\sqrt{3}}=\frac{24}{\sqrt{3}}\times\frac{\sqrt{3}}{\sqrt{3}}m=8\sqrt{3}m$$





- Q3. A contractor plans to install two slides for the children to play in a park. For the children below the age of 5 years, she perfers to have a slide whose top is at a height of 1.5 m and is inclinded at an angle of 30° to the ground, whereas for elder children, she wants to have a steep slide at a height of 3 m, and inclined at an angle of 60° to the ground. What should be the length of the slide in each case?
- **Sol.** In figure,  $\ell_1$  is the length of the slide made for children below the age of 5 years and  $\ell_2$  is the length of the slide made for elder children.



In figure, AB = 1.5 m, AC =  $\ell_1$  m and  $\angle$ ACB = 30°; PQ = 3 m, OP =  $\ell_2$  m and  $\angle$ POQ = 60°

$$\frac{\mathbf{AB}}{\mathbf{AC}} = \sin 30^{\circ} \quad \text{and} \quad \frac{\mathbf{PQ}}{\mathbf{OP}} = \sin 60^{\circ}$$

$$\Rightarrow \frac{\mathbf{1.5}}{\ell_1} = \frac{1}{\mathbf{2}} \quad \text{and} \quad \frac{\mathbf{3}}{\ell_2} = \frac{\sqrt{\mathbf{3}}}{\mathbf{2}}$$

$$\Rightarrow \ell_1 = 2 \times 1.5 \text{ m and } \ell_2 = \frac{\mathbf{3} \times \mathbf{2}}{\sqrt{\mathbf{3}}} \text{ m}$$

$$\Rightarrow \ell_1 = 3 \text{ m} \quad \text{and} \quad \ell_2 = \mathbf{2} \sqrt{\mathbf{3}} \text{ m}$$

- **Q4.** The angle of elevation of the top of a tower from a point on the ground, which is 30 m away from the foot of the tower, is 30°. Find the height of the tower.
- **Sol.** In right ABC, AB = height of the tower and point C is 30m away from the foot of the tower,

$$\therefore AC = 30 \text{ m}$$

$$\text{Now } \frac{\mathbf{AB}}{\mathbf{AC}} = \tan 30^{\circ}$$

$$\Rightarrow \frac{\mathbf{h}}{\mathbf{30}} = \frac{1}{\sqrt{3}}$$

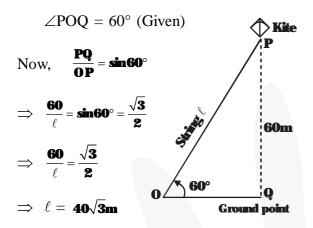
$$[\because \tan 30^{\circ} = \frac{1}{\sqrt{3}}]$$

$$\Rightarrow h = \frac{\mathbf{30}}{\sqrt{3}} = \frac{\mathbf{30}}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = \mathbf{10}\sqrt{3}$$

Thus, the required height of the tower is  $10\sqrt{3}$  m



- **Q5.** A kite is flying at a height of 60 m above the ground. The string attached to the kite is temporarily tied to a point on the ground. The inclination of the string with the ground is 60°. find the length of the string, assuming that there is no slack in the string.
- **Sol.** P is the position of the kite. Its height from the point Q (on the ground) = PQ = 60 m Let  $OP = \ell$  be the length of the string.



- **Q6.** A 1.5 m tall boy is standing at some distance from a 30 m tall building. The angle of elevation from his eyes to the top of the building increases from 30° to 60° as he walks towards the building. Find the distance he walked towards the building.
- **Sol.** PQ = 30 m is the height of the building. OA = 1.5 m is the height of the boy. Its first position is at OA OR is horizontal line through the position of the eye at O.

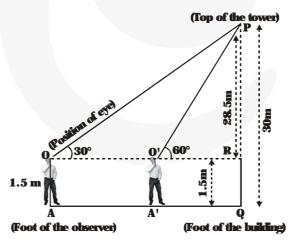
$$\angle POR = 30^{\circ}$$
 (Given)

The second position of the boy is at O'A' and

$$\angle PO'R = 60^{\circ}.$$

Here, 
$$RQ = OA = 1.5 \text{ m}$$

and 
$$PR = 30 \text{ m} - 1.5 \text{ m} = 28.5 \text{ m}$$



From  $\triangle POR$ ,

From 
$$\Delta PO'R$$
,

$$\frac{PR}{OR} = tan 30^{\circ}$$

$$\frac{PR}{\Omega P} = tan60^\circ$$

$$\Rightarrow \frac{28.5}{OR} = \frac{1}{\sqrt{3}}$$

$$\frac{28.5}{0'R} = \sqrt{3}$$



$$\Rightarrow$$
 OR = 28.5 ×  $\sqrt{3}$  m ...(1)  $\Rightarrow$  O'R= $\frac{28.5}{\sqrt{3}}$  m ...(2)

The distance walked by the boy towards the building.

$$= OO' = OR - O'R$$

= 
$$28.5 \times \sqrt{3} \, \mathbf{m} - \frac{28.5}{\sqrt{3}} \, \mathbf{m}$$
 [From (1) and (2)]

$$= 28.5 \times \left\{ \sqrt{3} - \frac{1}{\sqrt{3}} \right\} \mathbf{m}$$

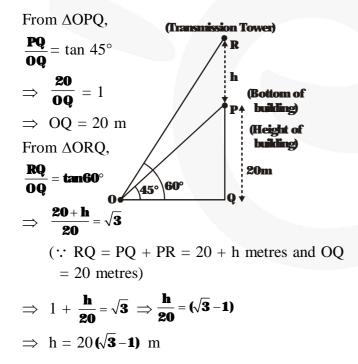
= 
$$28.5 \times \frac{(3-1)}{\sqrt{3}}$$
m =  $28.5 \times \frac{2}{\sqrt{3}}$ m

$$=\frac{57}{\sqrt{3}}$$
 m  $=19\sqrt{3}$  m

- **Q7.** From a point on the ground the angles of elevation of the bottom and top of a transmission tower fixed at the top of a 20 m high building are 45° and 60° respectively. Find the height of the tower.
- **Sol.** PQ = 20 m is the height of the building.

Let PR = h metres be the height of the transmission tower. P is the bottom and R is the top of the transmission tower.

$$\angle POQ = 45^{\circ} \text{ and } \angle ROQ = 60^{\circ}$$





- **Q8.** A statue, 1.6 m tall, stands on the top of pedestal. From a point on the ground, the angle of elevation of the top of the statue is 60° and from the same point the angle of elevation of the top of the pedestal is 45°. Find the height of the pedestal.
- Sol. In the figure, DC represents the statue and BC represents the pedestal.

Now, in right  $\triangle ABC$ , we have  $\frac{\mathbf{AB}}{\mathbf{BC}} = \cot 45^{\circ} = 1$   $\Rightarrow \frac{\mathbf{AB}}{\mathbf{h}} = 1$ 

$$\Rightarrow$$
 AB = h metres.

Now in right  $\triangle ABD$ , we have

$$\frac{\mathbf{BD}}{\mathbf{AB}} = \tan 60^{\circ} = \sqrt{3}$$

$$\Rightarrow BD = \sqrt{3} \times AB = \sqrt{3} \times h$$

$$\Rightarrow h + 1.6 = \sqrt{3} h$$

$$\Rightarrow h(\sqrt{3} - 1) = 1.6$$

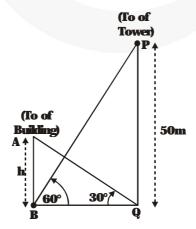
$$\Rightarrow h = \frac{1.6}{\sqrt{3} - 1} = \frac{1.6}{\sqrt{3} - 1} \times \frac{\sqrt{3} + 1}{\sqrt{3} + 1}$$

$$\Rightarrow h = \frac{1.6}{3 - 1} \times (\sqrt{3} + 1) = \frac{1.6}{2} \times (\sqrt{3} + 1)$$

$$= 0.8(\sqrt{3} + 1)m$$

Thus, the height of the pedestal is  $0.8(\sqrt{3} + 1)$ m.

- **Q9.** The angle of elevation of the top of the building from the foot of the tower is 30° and the angle of elevation of the top of the tower from the foot of the building is 60°. If the tower is 50 m high, find the height of the building.
- **Sol.** PQ = 50 metres is the height of the tower. Let AB = h metres be the height of the building. Angle of elevation of the top of the building from the foot of the tower =  $30^{\circ}$ , i.e.,  $\angle AQB = 30^{\circ}$ .





Angle of elevation of the top of the tower from the foot of the building

$$= 60, i.e., \angle PBQ = 60$$

From ∆AQB

$$\frac{h}{BQ}=tan30^\circ=\frac{1}{\sqrt{3}}$$

$$\Rightarrow BQ = h\sqrt{3}$$
 ...(1)

From ΔPBQ

$$\frac{50}{BQ}=tan60^\circ=\sqrt{3}$$

$$\Rightarrow$$
 BQ =  $\frac{50}{\sqrt{3}}$  ...(2)

From (1) and (2), we have  $\mathbf{h}\sqrt{\mathbf{3}} = \frac{\mathbf{50}}{\sqrt{\mathbf{3}}}$ 

$$\Rightarrow h = \frac{50}{3}m$$
, i.e.,  $h = 16\frac{2}{3}m$ 

- **Q10.** Two poles of equal heights are standing opposite to each other on either side of the road which is 80 m wide. From a point between them on the road, the angles of elevation of the top of the poles are 60° and 30°, respectively. Find the height of the poles and the distances of the point from the poles.
- Sol. Let AB and CD be the towels & P is the point between them.

AB = h metres

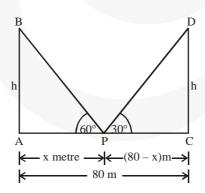
CD = h metres

$$AP = x m$$

$$CP = (80 - x) \text{ m}$$

Now, in right  $\triangle APB$ , We have

$$\frac{\mathbf{AB}}{\mathbf{AP}} = \tan 60^{\circ} \quad \Rightarrow \quad \frac{\mathbf{h}}{\mathbf{x}} = \sqrt{3}$$



$$\Rightarrow$$
 h = x $\sqrt{3}$  .....(1)

Again in right  $\Delta$ CPD, we have

$$\frac{\text{CD}}{\text{CP}} = \tan 30^{\circ}$$

$$\Rightarrow \frac{\mathbf{h}}{(80-\mathbf{x})} = \frac{1}{\sqrt{3}}$$



$$\Rightarrow h = \frac{80 - x}{\sqrt{3}}$$
 ....(2)

From (1) and (2), we get

$$\sqrt{3}x = \frac{80 - x}{\sqrt{3}}$$

$$\Rightarrow \sqrt{3} \times \sqrt{3} \times x = 80 - x \Rightarrow 3x = 80 - x$$

$$\Rightarrow$$
 3x + x = 80  $\Rightarrow$  4x = 80  $\Rightarrow$  x =  $\frac{80}{4}$  = 20

$$\therefore$$
 CP = 80 - x = 80 - 20 = 60 m

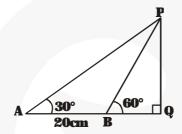
Now, from (1), we have

$$h = \sqrt{3} \times 20 = 1.732 \times 20 = 34.64$$

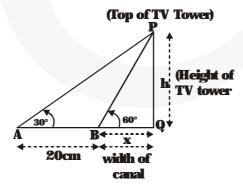
Thus, the required point is 20 m away from the first pole and 60 m away from the second pole.

Height of each pole = 34.64 m.

Q11. A TV tower stands vertically on a bank of a canal. From a point on the other bank directly opposite the tower, the angle of elevation of the top of the tower is 60°. From another point 20 m away this point on the line joining this point to the foot of the tower, the angle of elevation of the top of the tower is 30° (see fig.). Find the height of the tower and the width of the canal.



**Sol.** Let PQ = h metres be the height of the tower and BQ = x metres be the width of the canal  $\angle PBQ = 60^{\circ}$ 



Now, the angle of elevation of the top of the tower from the point  $A=30^\circ$ , i.e.,  $\angle PAQ=30^\circ$  where AB=20 metres.

From  $\triangle PBQ$ ,

$$\frac{\mathbf{h}}{\mathbf{x}} = \mathbf{tan} \mathbf{60}^{\circ}$$



$$\Rightarrow \frac{\mathbf{h}}{\mathbf{x}} = \sqrt{\mathbf{3}} \text{ or } \mathbf{h} = \mathbf{x}\sqrt{\mathbf{3}} \dots(1)$$

From  $\triangle PAQ$ ,

$$\frac{\mathbf{h}}{20+\mathbf{x}} = \tan 30^{\circ} = \frac{1}{\sqrt{3}} \implies \mathbf{h} = \frac{20+\mathbf{x}}{\sqrt{3}} \quad ...(2)$$

From (1) and (2), we have  $x\sqrt{3} = \frac{20 + x}{\sqrt{3}}$ 

$$\Rightarrow$$
 3x = 20 + x or 2x = 20  $\Rightarrow$  x = 10

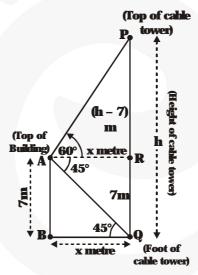
From (1),  $h = 10\sqrt{3} m$ 

- Q12. From the top of a 7 m high building, the angle of elevation of the top of a cable tower is  $60^{\circ}$  and the angle of depression of its foot is  $45^{\circ}$ . Determine the height of the tower.
- **Sol.** Let PQ = h metres be the height of the cable tower.

AB = 7 metres is the height of the bulding

 $\angle PAR = 60^{\circ}$  is the angle of elevation of the top of the cable tower from the top of the building.

 $\angle RAQ = 45^{\circ}$  is the angle of depression of the foot of the cable tower from the top of the building. Then  $\angle AQB = 45^{\circ}$ .



Now, BQ = AR = x metres (say)

From 
$$\triangle AQB$$
,  $\frac{AB}{BQ} = \tan 45^{\circ} \Rightarrow \frac{7}{x} = 1 \Rightarrow x = 7 \text{ m}$ 

Now, from 
$$\triangle PAR$$
,  $\frac{PR}{AR} = \tan 60^{\circ} \Rightarrow \frac{PQ - QR}{x} = \sqrt{3}$ 

$$\Rightarrow \frac{\mathbf{h} - \mathbf{7}}{\mathbf{x}} = \sqrt{\mathbf{3}} \Rightarrow \frac{\mathbf{h} - \mathbf{7}}{\mathbf{7}} = \sqrt{\mathbf{3}} \Rightarrow \mathbf{h} = 7(\sqrt{\mathbf{3}} + \mathbf{1})$$

Hence, the height of the cable tower is  $7(\sqrt{3}+1)$  metre.



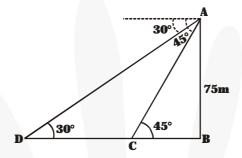
- Q13. As observed from the top of a 75m high lighthouse from the sea-level, the angles of depression of two ships are 30° and 45°. If one ship is exactly behind the other on the same side of the lighthouse, find the distance between the two ships.
- Sol. In the figure, let AB represent the light house.

$$\therefore$$
 AB = 75 m

Let the two ships be C and D such that angle of depression from A are  $45^{\circ}$  and  $30^{\circ}$  respectively.

Now, in right  $\triangle ABC$ , we have

$$\frac{\mathbf{AB}}{\mathbf{BC}} = \tan 45^{\circ}$$



$$\Rightarrow \frac{75}{BC} = 1 \Rightarrow BC = 75$$

Again, in right  $\triangle$ ABD, We have

$$\frac{\mathbf{AB}}{\mathbf{BD}} = \tan 30^{\circ} \implies \frac{\mathbf{75}}{\mathbf{BD}} = \frac{\mathbf{1}}{\sqrt{\mathbf{3}}}$$

$$\Rightarrow$$
 BD= 75  $\sqrt{3}$ 

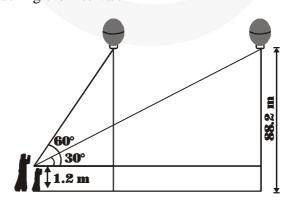
Since the distance between the two ships

$$= CD = BD - BC = 75\sqrt{3} - 75 = 75[\sqrt{3} - 1]$$

$$= 75[1.732 - 1] = 75 \times 0.732 = 54.9$$

Thus, the required distance between the ships is 54.9 m.

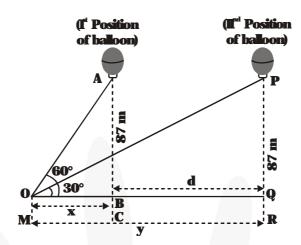
**Q14.** A 1.2 m tall girl spots a balloon moving with the wind in a horizontal line at a height of 88.2 m from the ground. The angle of elevation of the balloon from the eyes of the girl at any instant is 60°. After some time, the angle of elevation reduces to 30°. Find the distance travelled by the balloon during the interval.





**Sol.** From figure, we have  $\angle POQ = 30^{\circ}$  is the angle of elevation for the first position of the balloon. Let

$$OQ = y m$$
.



We are given that

$$AC = 88.2 \text{ m.}, AB = 88.2 - 1.2 = 87 \text{ m}$$

For the second position of the balloon, we have

$$\angle POQ = 30^{\circ}$$
. Let  $OB = x$  m.

We have to find d = BQ = (y - x)

$$\frac{AB}{OB}$$
 = tam60° and  $\frac{PQ}{OQ}$  = tam30°

$$\Rightarrow \frac{87}{x} = \sqrt{3}$$
 and  $\frac{87}{y} = \frac{1}{\sqrt{3}}$ 

$$\Rightarrow$$
 x =  $\frac{87}{\sqrt{3}}$ m and y =  $87\sqrt{3}$  m

Then 
$$d = y - x = \left\{ 87\sqrt{3} - \frac{87}{\sqrt{3}} \right\} m$$

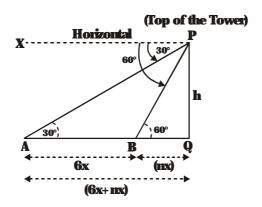
$$=87\times\left\{\sqrt{\mathbf{3}}-\frac{\mathbf{1}}{\sqrt{\mathbf{3}}}\right\}\mathbf{m}$$

$$= 87 \times \frac{2}{\sqrt{3}} \text{ m} = 87 \times \frac{2}{3} \times \sqrt{3} \text{ m}$$

$$=\frac{174}{3}\sqrt{3}$$
m  $= 58\sqrt{3}$  m

- Q15. A straight highway leads to the foot of a tower. A man standing at the top of the tower observes a car at an angle of depression of 30°, which is approaching the foot of the tower with a uniform speed. Six seconds later, the angle of depression of the car is found to be 60°. Find the time taken by the car to reach the foot of the tower.
- **Sol.** Let PQ = h metres be the height of the tower. P is the top of the tower. PX is horizontal line through P. The first and second positions of the car are at A and B respectively.





$$\angle APX = 30^{\circ}$$

(Angle of depression of the car when observed at A) and  $\angle BPX = 60^{\circ}$ 

(Angle of depression of the car when observed at B)

Then 
$$\angle PAQ = 30^{\circ}$$
 and  $\angle PBQ = 60^{\circ}$ 

Let the speed of the car be x m/second

Then distance  $AB = 6 \times metres$ .

Let the time taken from B to Q be n second.

Then distance BQ = nx metres.

In right  $\Delta PAQ$ ,

In right 
$$\triangle PAQ$$

$$\frac{h}{6x + nx} = tan 30^{\circ} = \frac{1}{\sqrt{3}}$$

$$\Rightarrow h = \frac{(n + 6)x}{\sqrt{3}} ...(1)$$
In right  $\triangle PBQ$ 

$$\frac{h}{nx} = tan 60^{\circ} = \sqrt{3}$$

$$\Rightarrow h = nx\sqrt{3} ...(2)$$

From (1) and (2), we have

$$\frac{(n+6)x}{\sqrt{3}} = nx\sqrt{3}$$

$$\Rightarrow$$
 n + 6 =  $\mathbf{n}\sqrt{3} \times \sqrt{3}$ 

$$\Rightarrow$$
 3n = n + 6

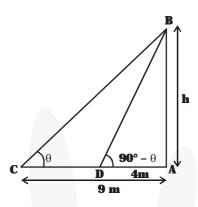
$$\Rightarrow$$
 2n = 6

$$\Rightarrow$$
 n = 3

Hence, the time from B to Q = 3 seconds.



- **Q16.** The angles of a elevation of the top of a tower from two points at a distance of 4 m and 9 m from the base of the tower and in the same straight line with it are complementary. Prove that the height of the tower is 6 m.
- Sol. Let the tower be represented by AB in the figure.



Let AB = h metres.

 $\therefore$  In right  $\triangle$  ABC, we have

$$\frac{\mathbf{AB}}{\mathbf{AC}} = \tan\theta$$

$$\Rightarrow \frac{\mathbf{h}}{\mathbf{9}} = \tan \theta$$
 .....(1)

In right  $\triangle ABD$ , we have

$$\frac{\mathbf{AB}}{\mathbf{AD}} = \tan(90^{\circ} - \theta) = \cot \theta$$

$$\Rightarrow \frac{\mathbf{h}}{\mathbf{4}} = \cot \theta \qquad \dots (2)$$

Multiplying (1) and (2), we get

$$\frac{\mathbf{h}}{\mathbf{9}} \times \frac{\mathbf{h}}{\mathbf{4}} = \tan\theta \times \cot\theta = 1 \quad [\because \tan\theta \times \cot\theta = 1]$$

$$\Rightarrow \frac{\mathbf{h^2}}{\mathbf{36}} = 1 \Rightarrow \mathbf{h^2} = 36$$

$$\Rightarrow$$
 h = ± 6 m  $\therefore$  h = 6 m

[∵ Height is positive only]

Thus, the height of the tower is 6 m.