

Q 1. Identify the terms, their coefficients for each of the following expressions.

(i) $5xyz^2 - 3zy$

(ii) $1 + x + x^2$

(iii) $4x^2y^2 - 4x^2y^2z^2 + z^2$

(iv) $3 - pq + qr - rp$

(v) $\frac{x}{2} + \frac{y}{2} - xy$

(vi) $0.3a - 0.6ab + 0.5b$

Answer :

The terms and the respective coefficients of the given expressions are as follows.

-	Terms	Coefficients
(i)	$5xyz^2$	5
	$- 3zy$	- 3
(ii)	1	1
	x	1
	x^2	1
(iii)	$4x^2y^2$	4
	$- 4x^2y^2z^2$	- 4
	z^2	1
(iv)	3	3

	$-pq$	-1
	qr	1
	$-rp$	-1
(v)	$\frac{x}{2}$	$\frac{1}{2}$
	$\frac{y}{2}$	$\frac{1}{2}$
	$-xy$	-1
(vi)	$0.3a$	0.3
	$-0.6ab$	-0.6
	$0.5b$	0.5

Q2 :

Classify the following polynomials as monomials, binomials, trinomials. Which polynomials do not fit in any of these three categories?

$x + y$, 1000 , $x + x^2 + x^3 + x^4$, $7 + y + 5x$, $2y - 3y^2$, $2y - 3y^2 + 4y^3$, $5x - 4y + 3xy$, $4z - 15z^2$, $ab + bc + cd + da$, pqr , $p^2q + pq^2$, $2p + 2q$

Answer :

The given expressions are classified as

Monomials: 1000 , pqr

Binomials: $x + y$, $2y - 3y^2$, $4z - 15z^2$, $p^2q + pq^2$, $2p + 2q$

Trinomials: $7 + y + 5x$, $2y - 3y^2 + 4y^3$, $5x - 4y + 3xy$

Polynomials that do not fit in any of these categories are

$x + x^2 + x^3 + x^4$, $ab + bc + cd + da$

Questions and Solutions | Exercise 8.1 - NCERT B

$$\begin{array}{r} 2p^2q^2 - 3pq + 4 \\ + \quad -3p^2q^2 + 7pq + 5 \\ \hline - p^2q^2 + 4pq + 9 \end{array}$$

Thus, the sum of the given expressions is $- p^2q^2 + 4pq + 9$.

(iv)

$$\begin{array}{r} l^2 + m^2 \\ + \quad m^2 + n^2 \\ + \quad l^2 \quad + n^2 \\ + \quad 2lm + 2mn + 2nl \\ \hline 2l^2 + 2m^2 + 2n^2 + 2lm + 2mn + 2nl \end{array}$$

Thus, the sum of the given expressions is $2(l^2 + m^2 + n^2 + lm + mn + nl)$.

Q4 :

(a) Subtract $4a - 7ab + 3b + 12$ from $12a - 9ab + 5b - 3$

(b) Subtract $3xy + 5yz - 7zx$ from $5xy - 2yz - 2zx + 10xyz$

(c) Subtract $4p^2q - 3pq + 5pq^2 - 8p + 7q - 10$ from $18 - 3p - 11q + 5pq - 2pq^2 + 5p^2q$

Answer :

The given expressions in separate rows, with like terms one below the other and then the subtraction of these expressions is as follows.

(a)

$$\begin{array}{r} 12a - 9ab + 5b - 3 \\ 4a - 7ab + 3b + 12 \\ (-) \quad (+) \quad (-) \quad (-) \\ \hline 8a - 2ab + 2b - 15 \end{array}$$

(b)

$$\begin{array}{r} 5xy - 2yz - 2zx + 10xyz \\ 3xy + 5yz - 7zx \\ \hline (-) \quad (-) \quad (+) \\ 2xy - 7yz + 5zx + 10xyz \end{array}$$

(c)

$$\begin{array}{r} 18 - 3p - 11q + 5pq - 2pq^2 + 5p^2q \\ -10 - 8p + 7q - 3pq + 5pq^2 + 4p^2q \\ \hline (+) \quad (+) \quad (-) \quad (+) \quad (-) \quad (-) \\ 28 + 5p - 18q + 8pq - 7pq^2 + p^2q \end{array}$$

Questions and Solutions | Exercise 8.2 - NCERT Books

Exercise 9.2 : Solutions of Questions on Page Number : 143

Q1 :

Find the product of the following pairs of monomials.

(i) $4, 7p$ (ii) $-4p, 7p$ (iii) $-4p, 7pq$

(iv) $4p^3, -3p$ (v) $4p, 0$

Answer :

The product will be as follows.

(i) $4 \times 7p = 4 \times 7 \times p = 28p$

(ii) $-4p \times 7p = -4 \times p \times 7 \times p = (-4 \times 7) \times (p \times p) = -28p^2$

(iii) $-4p \times 7pq = -4 \times p \times 7 \times p \times q = (-4 \times 7) \times (p \times p \times q) = -28p^2q$

(iv) $4p^3 \times -3p = 4 \times (-3) \times p \times p \times p \times p = -12p^4$

(v) $4p \times 0 = 4 \times p \times 0 = 0$

Q2 :

Find the areas of rectangles with the following pairs of monomials as their lengths and breadths respectively.

(p, q) ; $(10m, 5n)$; $(20x^2, 5y^2)$; $(4x, 3x^2)$; $(3mn, 4np)$

Answer :

We know that,

Area of rectangle = Length x Breadth

Area of 1st rectangle = $p \times q = pq$

Area of 2nd rectangle = $10m \times 5n = 10 \times 5 \times m \times n = 50 mn$

Area of 3rd rectangle = $20x^2 \times 5y^2 = 20 \times 5 \times x^2 \times y^2 = 100 x^2y^2$

Area of 4th rectangle = $4x \times 3x^2 = 4 \times 3 \times x \times x^2 = 12x^3$

Area of 5th rectangle = $3mn \times 4np = 3 \times 4 \times m \times n \times n \times p = 12mn^2p$

Q3 :

Complete the table of products.

First monomial → Second monomial ↓	$2x$	$-5y$	$3x^2$	$-4xy$	$7x^2y$	$-9x^2y^2$
$2x$	$4x^2$
$-5y$	$-15x^2y$
$3x^2$
-4						

Answer :

The table can be completed as follows.

<u>First monomial</u> → <u>Second monomial</u> ↓	$2x$	$-5y$	$3x^2$	$-4xy$	$7x^2y$	$-9x^2y^2$
$2x$	$4x^2$	$-10xy$	$6x^3$	$-8x^2y$	$14x^3y$	$-18x^3y^2$
$-5y$	$-10xy$	$25y^2$	$-15x^2y$	$20xy^2$	$-35x^2y^2$	$45x^2y^3$
$3x^2$	$6x^3$	$-15x^2y$	$9x^4$	$-12x^3y$	$21x^4y$	$-27x^4y^2$
$-4xy$	$-8x^2y$	$20xy^2$	$-12x^3y$	$16x^2y^2$	$-28x^3y^2$	$36x^3y^3$
$7x^2y$	$14x^3y$	$-35x^2y^2$	$21x^4y$	$-28x^3y^2$	$49x^4y^2$	$-63x^4y^3$
$-9x^2y^2$	$-18x^3y^2$	$45x^2y^3$	$-27x^4y^2$	$36x^3y^3$	$-63x^4y^3$	$81x^4y^4$

Q4 :

Obtain the volume of rectangular boxes with the following length, breadth and height respectively.

(i) $5a, 3a^2, 7a^4$ (ii) $2p, 4q, 8r$ (iii) $xy, 2x^2y, 2xy^2$

(iv) $a, 2b, 3c$

Answer :

We know that,

Volume = Length x Breadth x Height

(i) Volume = $5a \times 3a^2 \times 7a^4 = 5 \times 3 \times 7 \times a \times a^2 \times a^4 = 105 a^7$

(ii) Volume = $2p \times 4q \times 8r = 2 \times 4 \times 8 \times p \times q \times r = 64pqr$

(iii) Volume = $xy \times 2x^2y \times 2xy^2 = 2 \times 2 \times xy \times x^2y \times xy^2 = 4x^4y^4$

(iv) Volume = $a \times 2b \times 3c = 2 \times 3 \times a \times b \times c = 6abc$

Q5 :

Obtain the product of

(i) xy, yz, zx (ii) $a, -a^2, a^3$ (iii) $2, 4y, 8y^2, 16y^3$

(iv) $a, 2b, 3c, 6abc$ (v) $m, -mn, mnp$

Answer :

(i) $xy \times yz \times zx = x^2y^2z^2$

(ii) $a \times (-a^2) \times a^3 = -a^6$

(iii) $2 \times 4y \times 8y^2 \times 16y^3 = 2 \times 4 \times 8 \times 16 \times y \times y^2 \times y^3 = 1024 y^6$

(iv) $a \times 2b \times 3c \times 6abc = 2 \times 3 \times 6 \times a \times b \times c \times abc = 36a^2b^2c^2$

(v) $m \times (-mn) \times mnp = -m^3n^2p$

Questions and Solutions | Exercise 8.3 - NCERT Books

Exercise 9.3 : Solutions of Questions on Page Number : 146

Q1 :

Carry out the multiplication of the expressions in each of the following pairs.

(i) $4p, q + r$ (ii) $ab, a - b$ (iii) $a + b, 7a^2b^2$

(iv) $a^2 - 9, 4a$ (v) $pq + qr + rp, 0$

Answer :

(i) $(4p) \times (q + r) = (4p \times q) + (4p \times r) = 4pq + 4pr$

(ii) $(ab) \times (a - b) = (ab \times a) + [ab \times (-b)] = a^2b - ab^2$

(iii) $(a + b) \times (7a^2b^2) = (a \times 7a^2b^2) + (b \times 7a^2b^2) = 7a^3b^2 + 7a^2b^3$

(iv) $(a^2 - 9) \times (4a) = (a^2 \times 4a) + (-9) \times (4a) = 4a^3 - 36a$

(v) $(pq + qr + rp) \times 0 = (pq \times 0) + (qr \times 0) + (rp \times 0) = 0$

Q2 :

Complete the table

---	First expression	Second Expression	Product
(i)	a	$b + c + d$	-
(ii)	$x + y - 5$	$5xy$	-
(iii)	p	$6p^2 - 7p + 5$	-
(iv)	$4p^2q^2$	$p^2 - q^2$	-
(v)	$a + b + c$	abc	-

Answer :

The table can be completed as follows.

-	First expression	Second Expression	Product
(i)	a	$b + c + d$	$ab + ac + ad$
(ii)	$x + y - 5$	$5xy$	$5x^2y + 5xy^2 - 25xy$
(iii)	p	$6p^2 - 7p + 5$	$6p^3 - 7p^2 + 5p$
(iv)	$4p^2q^2$	$p^2 - q^2$	$4p^4q^2 - 4p^2q^4$
(v)	$a + b + c$	abc	$a^2bc + ab^2c + abc^2$

Q3 :

Find the product.

(i) $(a^2) \times (2a^{22}) \times (4a^{26})$

(ii) $\left(\frac{2}{3}xy\right) \times \left(\frac{-9}{10}x^2y^2\right)$

$$(iii) \left(-\frac{10}{3} pq^3\right) \times \left(\frac{6}{5} p^3 q\right)$$

$$(iv) x \times x^2 \times x^3 \times x^4$$

Answer :

$$(i) (a^2) \times (2a^{22}) \times (4a^{26}) = 2 \times 4 \times a^2 \times a^{22} \times a^{26} = 8a^{50}$$

$$(ii) \left(\frac{2}{3} xy\right) \times \left(\frac{-9}{10} x^2 y^2\right) = \left(\frac{2}{3}\right) \times \left(\frac{-9}{10}\right) \times x \times y \times x^2 \times y^2 = \frac{-3}{5} x^3 y^3$$

$$(iii) \left(-\frac{10}{3} pq^3\right) \times \left(\frac{6}{5} p^3 q\right) = \left(-\frac{10}{3}\right) \times \left(\frac{6}{5}\right) \times pq^3 \times p^3 q = -4p^4 q^4$$

$$(iv) x \times x^2 \times x^3 \times x^4 = x^{10}$$

Q4 :

$$(a) \text{ Simplify } 3x(4x - 5) + 3 \text{ and find its values for (i) } x = 3, \text{ (ii) } x = \frac{1}{2}.$$

$$(b) a(a^2 + a + 1) + 5 \text{ and find its values for (i) } a = 0, \text{ (ii) } a = 1, \text{ (iii) } a = -1.$$

Answer :

$$(a) 3x(4x - 5) + 3 = 12x^2 - 15x + 3$$

$$(i) \text{ For } x = 3, 12x^2 - 15x + 3 = 12(3)^2 - 15(3) + 3$$

$$= 108 - 45 + 3$$

$$= 66$$

$$(ii) \text{ For } x = \frac{1}{2}, 12x^2 - 15x + 3 = 12\left(\frac{1}{2}\right)^2 - 15\left(\frac{1}{2}\right) + 3$$

$$\begin{aligned} &= 12 \times \frac{1}{4} - \frac{15}{2} + 3 \\ &= 3 - \frac{15}{2} + 3 = 6 - \frac{15}{2} \\ &= \frac{12 - 15}{2} = \frac{-3}{2} \end{aligned}$$

(b) $a(a^2 + a + 1) + 5 = a^3 + a^2 + a + 5$

(i) For $a = 0$, $a^3 + a^2 + a + 5 = 0 + 0 + 0 + 5 = 5$

(ii) For $a = 1$, $a^3 + a^2 + a + 5 = (1)^3 + (1)^2 + 1 + 5$

$$= 1 + 1 + 1 + 5 = 8$$

(iii) For $a = -1$, $a^3 + a^2 + a + 5 = (-1)^3 + (-1)^2 + (-1) + 5$

$$= -1 + 1 - 1 + 5 = 4$$

Q5 :

(a) Add: $p(p - q)$, $q(q - r)$ and $r(r - p)$

(b) Add: $2x(z - x - y)$ and $2y(z - y - x)$

(c) Subtract: $3l(l - 4m + 5n)$ from $4l(10n - 3m + 2l)$

(d) Subtract: $3a(a + b + c) - 2b(a - b + c)$ from $4c(-a + b + c)$

Answer :

(a) First expression = $p(p - q) = p^2 - pq$

Second expression = $q(q - r) = q^2 - qr$

Third expression = $r(r - p) = r^2 - pr$

Adding the three expressions, we obtain

$$\begin{array}{r} p^2 - pq \\ + \quad \quad \quad q^2 - qr \\ + \quad \quad \quad \quad \quad r^2 - pq \\ \hline p^2 - pq + q^2 - qr + r^2 - pq \end{array}$$

Therefore, the sum of the given expressions is $p^2 + q^2 + r^2 - pq - qr - rp$.

(b) First expression = $2x(z - x - y) = 2xz - 2x^2 - 2xy$

Second expression = $2y(z - y - x) = 2yz - 2y^2 - 2yx$

Adding the two expressions, we obtain

$$\begin{array}{r} 2xz - 2x^2 - 2xy \\ + \quad \quad \quad -2yx + 2yz - 2y^2 \\ \hline 2xz - 2x^2 - 4xy + 2yz - 2y^2 \end{array}$$

Therefore, the sum of the given expressions is $-2x^2 - 2y^2 - 4xy + 2yz + 2zx$.

(c) $3l(l - 4m + 5n) = 3l^2 - 12lm + 15ln$

$4l(10n - 3m + 2l) = 40ln - 12lm + 8l^2$

Subtracting these expressions, we obtain

$$\begin{array}{r} 40ln - 12lm + 8l^2 \\ 15ln - 12lm + 3l^2 \\ (-) \quad (+) \quad (-) \\ \hline +25ln \quad \quad +5l^2 \end{array}$$

Therefore, the result is $5l^2 + 25ln$.

(d) $3a(a + b + c) - 2b(a - b + c) = 3a^2 + 3ab + 3ac - 2ba + 2b^2 - 2bc$

$= 3a^2 + 2b^2 + ab + 3ac - 2bc$

$4c(-a + b + c) = -4ac + 4bc + 4c^2$

Subtracting these expressions, we obtain

$$\begin{array}{r} -4ac + 4bc + 4c^2 \\ 3ac - 2bc \quad + 3a^2 + 2b^2 + ab \\ \hline (-) \quad (+) \quad (-) \quad (-) \quad (-) \\ -7ac + 6bc + 4c^2 - 3a^2 - 2b^2 - ab \end{array}$$

Therefore, the result is $-3a^2 - 2b^2 + 4c^2 - ab + 6bc - 7ac$.

Questions and Solutions | Exercise 8.4 - NCERT Books

Exercise 9.4 : Solutions of Questions on Page Number : 148

Q1 :

Multiply the binomials.

(i) $(2x + 5)$ and $(4x - 3)$ (ii) $(y - 8)$ and $(3y - 4)$

(iii) $(2.5l - 0.5m)$ and $(2.5l + 0.5m)$ (iv) $(a + 3b)$ and $(x + 5)$

(v) $(2pq + 3q^2)$ and $(3pq - 2q^2)$

(vi) $\left(\frac{3}{4}a^2 + 3b^2\right)$ and $4\left(a^2 - \frac{2}{3}b^2\right)$

Answer :

$$(i) (2x + 5) \times (4x - 3) = 2x \times (4x - 3) + 5 \times (4x - 3)$$

$$= 8x^2 - 6x + 20x - 15$$

$$= 8x^2 + 14x - 15 \text{ (By adding like terms)}$$

$$(ii) (y - 8) \times (3y - 4) = y \times (3y - 4) - 8 \times (3y - 4)$$

$$= 3y^2 - 4y - 24y + 32$$

$$= 3y^2 - 28y + 32 \text{ (By adding like terms)}$$

$$(iii) (2.5l - 0.5m) \times (2.5l + 0.5m) = 2.5l \times (2.5l + 0.5m) - 0.5m (2.5l + 0.5m)$$

$$= 6.25l^2 + 1.25lm - 1.25lm - 0.25m^2$$

$$= 6.25l^2 - 0.25m^2$$

$$(iv) (a + 3b) \times (x + 5) = a \times (x + 5) + 3b \times (x + 5)$$

$$= ax + 5a + 3bx + 15b$$

$$(v) (2pq + 3q^2) \times (3pq - 2q^2) = 2pq \times (3pq - 2q^2) + 3q^2 \times (3pq - 2q^2)$$

$$= 6p^2q^2 - 4pq^3 + 9pq^3 - 6q^4$$

$$= 6p^2q^2 + 5pq^3 - 6q^4$$

$$(vi) \left(\frac{3}{4}a^2 + 3b^2 \right) \times \left[4 \left(a^2 - \frac{2}{3}b^2 \right) \right] = \left(\frac{3}{4}a^2 + 3b^2 \right) \times \left(4a^2 - \frac{8}{3}b^2 \right)$$

$$= \frac{3}{4}a^2 \times \left(4a^2 - \frac{8}{3}b^2 \right) + 3b^2 \times \left(4a^2 - \frac{8}{3}b^2 \right)$$

$$= 3a^4 - 2a^2b^2 + 12b^2a^2 - 8b^4$$

$$= 3a^4 + 10a^2b^2 - 8b^4$$

Q2 :

Find the product.

$$(i) (5 - 2x)(3 + x) \quad (ii) (x + 7y)(7x - y)$$

$$(iii) (a^2 + b)(a + b^2) \quad (iv) (p^2 - q^2)(2p + q)$$

Answer :

$$(i) (5 - 2x)(3 + x) = 5(3 + x) - 2x(3 + x)$$

$$= 15 + 5x - 6x - 2x^2$$

$$= 15 - x - 2x^2$$

$$(ii) (x + 7y)(7x - y) = x(7x - y) + 7y(7x - y)$$

$$= 7x^2 - xy + 49xy - 7y^2$$

$$= 7x^2 + 48xy - 7y^2$$

$$(iii) (a^2 + b) (a + b^2) = a^2 (a + b^2) + b (a + b^2)$$

$$= a^3 + a^2b^2 + ab + b^3$$

$$(iv) (p^2 - q^2) (2p + q) = p^2 (2p + q) - q^2 (2p + q)$$

$$= 2p^3 + p^2q - 2pq^2 - q^3$$

Q3 :

Simplify.

$$(i) (x^2 - 5) (x + 5) + 25$$

$$(ii) (a^2 + 5) (b^3 + 3) + 5$$

$$(iii) (t + s^2) (t^2 - s)$$

$$(iv) (a + b) (c - d) + (a - b) (c + d) + 2 (ac + bd)$$

$$(v) (x + y) (2x + y) + (x + 2y) (x - y)$$

$$(vi) (x + y) (x^2 - xy + y^2)$$

$$(vii) (1.5x - 4y) (1.5x + 4y + 3) - 4.5x + 12y$$

$$(viii) (a + b + c) (a + b - c)$$

Answer :

$$(i) (x^2 - 5) (x + 5) + 25$$

$$= x^2 (x + 5) - 5 (x + 5) + 25$$

$$= x^3 + 5x^2 - 5x - 25 + 25$$

$$= x^3 + 5x^2 - 5x$$

$$(ii) (a^2 + 5) (b^3 + 3) + 5$$

$$= a^2 (b^3 + 3) + 5 (b^3 + 3) + 5$$

$$= a^2b^3 + 3a^2 + 5b^3 + 15 + 5$$

$$= a^2b^3 + 3a^2 + 5b^3 + 20$$

$$(iii) (t + s^2) (t^2 - s)$$

$$= t (t^2 - s) + s^2 (t^2 - s)$$

$$= t^3 - st + s^2t^2 - s^3$$

$$(iv) (a + b) (c - d) + (a - b) (c + d) + 2 (ac + bd)$$

$$= a (c - d) + b (c - d) + a (c + d) - b (c + d) + 2 (ac + bd)$$

$$= ac - ad + bc - bd + ac + ad - bc - bd + 2ac + 2bd$$

$$= (ac + ac + 2ac) + (ad - ad) + (bc - bc) + (2bd - bd - bd)$$

$$= 4ac$$

$$(v) (x + y) (2x + y) + (x + 2y) (x - y)$$

$$= x (2x + y) + y (2x + y) + x (x - y) + 2y (x - y)$$

$$= 2x^2 + xy + 2xy + y^2 + x^2 - xy + 2xy - 2y^2$$

$$= (2x^2 + x^2) + (y^2 - 2y^2) + (xy + 2xy - xy + 2xy)$$

$$= 3x^2 - y^2 + 4xy$$

$$(vi) (x + y) (x^2 - xy + y^2)$$

$$= x (x^2 - xy + y^2) + y (x^2 - xy + y^2)$$

$$= x^3 - x^2y + xy^2 + x^2y - xy^2 + y^3$$

$$= x^3 + y^3 + (xy^2 - xy^2) + (x^2y - x^2y)$$

$$= x^3 + y^3$$

$$(vii) (1.5x - 4y) (1.5x + 4y + 3) - 4.5x + 12y$$

$$= 1.5x (1.5x + 4y + 3) - 4y (1.5x + 4y + 3) - 4.5x + 12y$$

$$= 2.25x^2 + 6xy + 4.5x - 6xy - 16y^2 - 12y - 4.5x + 12y$$

$$= 2.25x^2 + (6xy - 6xy) + (4.5x - 4.5x) - 16y^2 + (12y - 12y)$$

$$= 2.25x^2 - 16y^2$$

$$(viii) (a + b + c)(a + b - c)$$

$$= a(a + b - c) + b(a + b - c) + c(a + b - c)$$

$$= a^2 + ab - ac + ab + b^2 - bc + ca + bc - c^2$$

$$= a^2 + b^2 - c^2 + (ab + ab) + (bc - bc) + (ca - ca)$$

$$= a^2 + b^2 - c^2 + 2ab$$