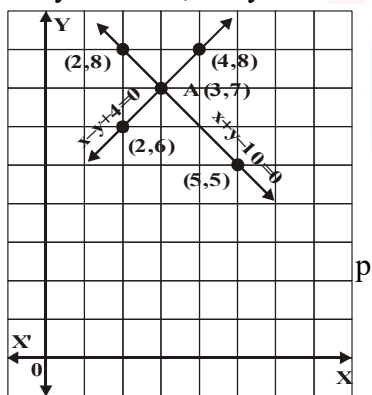


**Class X : MATH**

**Chapter - 8 : Pair of Linear Equations in Two Variable  
Questions & Solutions - Exercise - 3.1 - NCERT Book**

- Q1.** Form the pair of linear equations in the following problems, and find their solutions graphically.
- (i) 10 students of class X took part in a Mathematics quiz. If the number of girls is 4 more than the number of boys, find the number of boys and girls who took part in the quiz.
  - (ii) 5 pencils and 7 pens together cost ` 50, whereas 7 pencils and 5 pens together cost 46.
- Find the cost of one pencil and that of one pen.

**Sol.** (i) Let the number of boys be  $x$  and the number of girls be  $y$ .  
According to the given conditions  
 $x + y = 10$  and  $y = x + 4$   
We get the required pair of linear equations as  
 $x + y - 10 = 0$ ,  $x - y + 4 = 0$



Graphical Solution

$x + y - 10 = 0$  ... (i)

$x$	2	5
$y = 10 - x$	8	5

$x - y + 4 = 0$  ... (ii)

$x$	2	4
$y = x + 4$	6	8

From the graph, we have :  $x = 3, y = 7$  common solution of the two linear equations.  
Hence, the number of boys = 3 and the number of girls = 7.

(ii) Let the cost of 1 pencil be Rs  $x$  and cost of 1 pen be Rs.  $y$ .

$$5x + 7y = 50$$

$$7x + 5y = 46$$

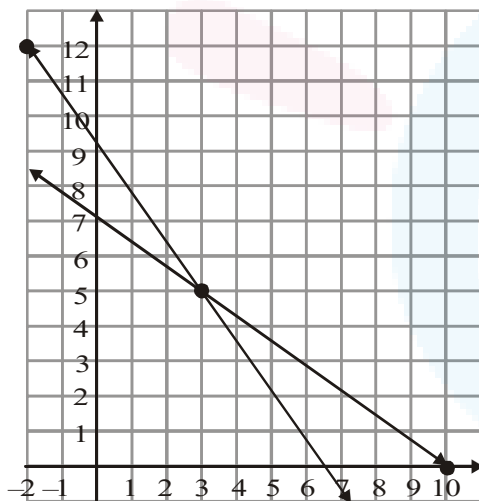
Graphical solution

$$5x + 7y = 50 \quad 7x + 5y = 46$$

$$y = \frac{50 - 5x}{7} \quad y = \frac{46 - 7x}{5}$$

x	3	10
y	5	0

x	3	-2
y	5	12



From the graph we have  $x = 3, y = 5$ .

Hence, cost of one pencil = Rs.3 and cost of one pen = Rs.5

**Q2.** On comparing the ratios  $\frac{a_1}{a_2}, \frac{b_1}{b_2}$  and  $\frac{c_1}{c_2}$ , find out whether the lines representing the

following pairs of linear equations intersect at a point, are parallel or coincident.

(i)  $5x - 4y + 8 = 0$ ;  $7x + 6y - 9 = 0$

(ii)  $9x + 3y + 12 = 0$ ;  $18x + 6y + 24 = 0$

(iii)  $6x - 3y + 10 = 0$ ;  $2x - y + 9 = 0$

**Sol.** (i)  $5x - 4y + 8 = 0$       ... (i)

$7x + 6y - 9 = 0$       ... (ii)

$$\frac{a_1}{a_2} = \frac{5}{7}, \frac{b_1}{b_2} = \frac{-4}{6} = -\frac{2}{3} \Rightarrow \frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

$\Rightarrow$  Lines represented by (i) and (ii) intersect at a point

(ii)  $9x + 3y + 12 = 0$       .... (i)

$18x + 6y + 24 = 0$       .... (ii)

$$\frac{a_1}{a_2} = \frac{9}{18}, \frac{b_1}{b_2} = \frac{3}{6}, \frac{c_1}{c_2} = \frac{12}{24}$$

$$\Rightarrow \frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$

$\therefore$  Lines represented by (i) and (ii) are coincident.

(iii)  $6x - 3y + 10 = 0$       .... (i)

$2x - y + 9 = 0$       .... (ii)

$$\frac{a_1}{a_2} = \frac{6}{2} = \frac{3}{1}, \frac{b_1}{b_2} = \frac{-3}{-1} = \frac{3}{1}, \frac{c_1}{c_2} = \frac{10}{9}$$

$$\Rightarrow \frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$

$\therefore$  Lines represented by (i) and (ii) are parallel

**Q3.** On comparing the ratios  $\frac{a_1}{a_2}$ ,  $\frac{b_1}{b_2}$  and  $\frac{c_1}{c_2}$ , find out whether the following pairs of linear equations are consistent, or inconsistent.

- (i)  $3x + 2y = 5; 2x - 3y = 7$   
 (ii)  $2x - 3y = 8; 4x - 6y = 9$   
 (iii)  $\frac{3}{2}x + \frac{5}{3}y = 7; 9x - 10y = 14$   
 (iv)  $5x - 3y = 11; -10x + 6y = -22$   
 (v)  $\frac{4}{3}x + 2y = 8; 2x + 3y = 12$

**Sol.** (i)  $3x + 2y - 5 = 0$  .....(i)  
 $2x - 3y - 7 = 0$  .....(ii)

$$\frac{a_1}{a_2} = \frac{3}{2}, \frac{b_1}{b_2} = \frac{2}{-3} = -\frac{2}{3}$$

$$\Rightarrow \frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

$\Rightarrow$  The equations have a unique solution.

Hence, consistent.

(ii)  $2x - 3y = 8$  .....(i)  
 $4x - 6y = 9$  .....(ii)

$$\frac{a_1}{a_2} = \frac{2}{4}, \frac{b_1}{b_2} = \frac{-3}{-6}, \frac{c_1}{c_2} = \frac{8}{9}$$

$$\Rightarrow \frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$

$\therefore$  The equations have no solution. Hence inconsistent.

(iii)  $\frac{3}{2}x + \frac{5}{3}y = 7$  .....(i)

$9x - 10y = 14$  .....(ii)

$$\frac{a_1}{a_2} = \frac{3/2}{9} = \frac{1}{6}, \frac{b_1}{b_2} = \frac{5/3}{-10} = -\frac{1}{6}$$

$$\Rightarrow \frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

$\Rightarrow$  The equations have a unique solutions

Hence, consistent.

(iv)  $5x - 3y = 11$  .....(i)

$-10x + 6y = -22$  .....(ii)

$$\frac{a_1}{a_2} = \frac{5}{-10} = \frac{-1}{2}, \frac{b_1}{b_2} = \frac{-3}{6} = \frac{-1}{2},$$

$$\frac{c_1}{c_2} = \frac{11}{-22} = \frac{-1}{2}$$

$$\Rightarrow \frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$

The equations have infinite solutions.

Hence, consistent.

(v)  $\frac{4}{3}x + 2y = 8$  .....(i)

$2x + 3y = 12$  .....(ii)

$$\frac{a_1}{a_2} = \frac{\frac{4}{3}}{2} = \frac{2}{3}, \frac{b_1}{b_2} = \frac{2}{3} = \frac{c_1}{c_2} = \frac{8}{12} = \frac{2}{3}$$

$$\Rightarrow \frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$

The equations have infinite solutions.

Hence, consistent.

**Q4.** Which of the following pairs of linear equations are consistent/inconsistent? If consistent, obtain the solution graphically :

(i)  $x + y = 5, 2x + 2y = 10$

(ii)  $x - y = 8, 3x - 3y = 16$

(iii)  $2x + y - 6 = 0, 4x - 2y - 4 = 0$

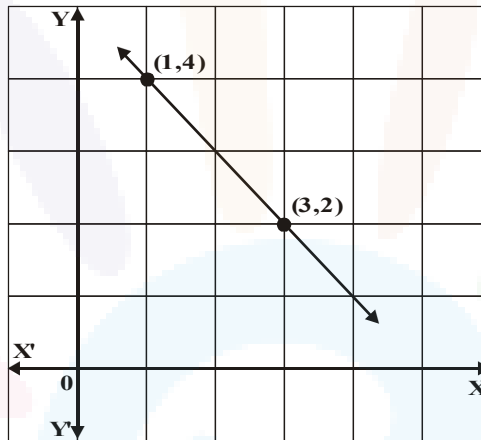
(iv)  $2x - 2y - 2 = 0, 4x - 4y - 5 = 0$

**Sol.** (i)  $x + y = 5$  ... (i)

$2x + 2y = 10$  ... (ii)

$$\frac{a_1}{a_2} = \frac{1}{2}, \frac{b_1}{b_2} = \frac{1}{2}, \frac{c_1}{c_2} = \frac{-5}{-10} = \frac{1}{2}$$

i.e.,  $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$



Hence, the pair of linear equations is consistent.

(i) and (ii) are same equations and hence the graph is coincident straight line.

x	1	3
$y = 5 - x$	4	2

(ii)  $x - y = 8$  ..... (i)

$3x - 3y = 16$  ..... (ii)

$$\frac{a_1}{a_2} = \frac{1}{3}, \frac{b_1}{b_2} = \frac{-1}{-3} = \frac{1}{3}, \frac{c_1}{c_2} = \frac{8}{16} = \frac{1}{2}$$

$$\Rightarrow \frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$

Therefore, lines have no solution

Hence, inconsistent.

(iii)  $2x + y = 6$  .....(i)  
 $4x - 2y = 4$  .....(ii)

$$\frac{a_1}{a_2} = \frac{2}{4} = \frac{1}{2}, \frac{b_1}{b_2} = \frac{1}{-2} = \frac{-1}{2}, \frac{c_1}{c_2} = \frac{6}{4} = \frac{3}{2}$$

$$\Rightarrow \frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

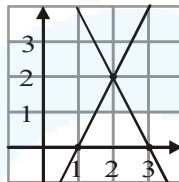
Therefore, lines have unique solution.

Hence, consistent

from (i)      from (ii)

x	2	3
y	2	0

x	2	1
y	2	0



from graph  $x = 2, y = 2$

(iv)  $2x - 2y = 2$  .....(i)  
 $4x - 4y = 5$  .....(ii)

$$\frac{a_1}{a_2} = \frac{2}{4} = \frac{1}{2}, \frac{b_1}{b_2} = \frac{-2}{-4} = \frac{1}{2}, \frac{c_1}{c_2} = \frac{2}{5}$$

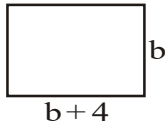
$$\Rightarrow \frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$

Therefore, lines have no solution.

Hence, Inconsistent.

**Q5.** Half the perimeter of a rectangular garden, whose length is 4 m more than its width, is 36 m. Find the dimensions of the garden

Sol.

Length,  $\ell = b + 4$  and Breadth =  $b$ Perimeter of rectangle =  $2(\ell + b)$ 

$$\frac{1}{2}[2(\ell + b)] = 36$$

$$(\ell + b) = 36 \quad \dots\dots(i)$$

As,  $\ell = b + 4$ , so putting the value of  $\ell$  in equation (i), we get

$$\Rightarrow b + 4 + b = 36$$

$$2b + 4 = 36$$

$$2b = 32$$

$$b = 16\text{m}, \ell = b + 4 = 16 + 4 = 20\text{m}$$

Thus, length of garden = 20m and breadth of garden = 16 m

**Q6.** Given the linear equation  $2x + 3y - 8 = 0$ , write another linear equation in two variables such that the geometrical representation of the pair so formed is :

- (i) Intersecting lines
- (ii) Parallel lines
- (iii) Coincident lines

**Sol.** (i)  $2x + 3y - 8 = 0$  (Given equation)

$$3x + 2y + 4 = 0 \quad \text{(New equation)}$$

Here,  $\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$

Hence, the graph of the two equations will be two intersecting lines.

(ii)  $2x + 3y - 8 = 0$  (given equation)

$$4x + 6y - 10 = 0 \quad \text{(New equation)}$$



Here,  $\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$

Hence, the graph of the two equations will be two parallel lines.

(iii)  $2x + 3y - 8 = 0$  (given equation)  
 $4x + 6y - 16 = 0$  (New equation)

Here,  $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$

Hence, the graph of the two equations will be two coincident lines.

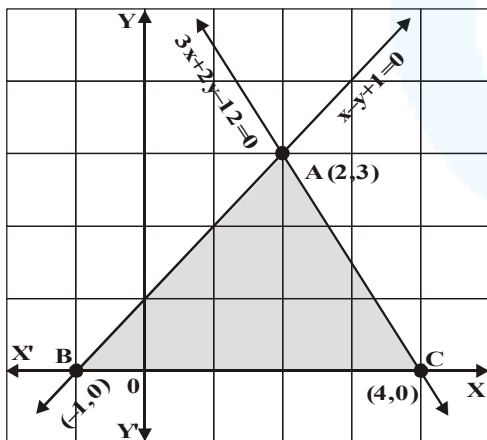
**Q7.** Draw the graphs of the equations  $x - y + 1 = 0$  and  $3x + 2y - 12 = 0$ . Determine the coordinates of the vertices of the triangle formed by these lines and the x-axis, and shade the triangular region.

**Sol.**  $x - y + 1 = 0$  ... (i)

x	-1	2
$y = x + 1$	0	3

$3x + 2y - 12 = 0$  ... (ii)

x	2	4
$y = \frac{12 - 3x}{2}$	3	0



The vertices of the triangle are  
 A (2, 3), B (-1, 0) and C (4, 0)