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Class X : MATH Chapter 7 : Coordinate geometry Questions & Answers - Exercise : 7.1 - NCERT Book

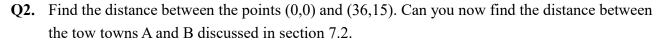
Find the distance between the following pairs of points : **Q1**. (a) (2,3), (4, 1) (b) (-5, 7), (-1,3)(c) (a, b), (-a, -b)**Sol.**(a) The given points are : A (2, 3), B (4, 1). Required distance = AB = BA = $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ AB = $\sqrt{(4-2)^2 + (1-3)^2} = \sqrt{(2)^2 + (-2)^2}$ $=\sqrt{4+4} = \sqrt{8} = 2\sqrt{2}$ units (b) Here $x_1 = -5$, $y_1 = 7$ and $x_2 = -1$, $y_2 = 3$... The required distance $=\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ $=\sqrt{[-1-(-5)]^2+(3-7)^2}$ $=\sqrt{(-1+5)^2+(-4)^2}$ $=\sqrt{16+16}=\sqrt{32}=\sqrt{2\times 16}$ $= 4\sqrt{2}$ units (c) Here $x_1 = a$, $y_1 = b$ and $x_2 = -a$, $y_2 = -b$... The required distance $= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ $=\sqrt{(-a-a)^2+(-b-b)^2}$ $=\sqrt{(-2a)^2 + (-2b)^2} = \sqrt{4a^2 + 4b^2}$ $=\sqrt{4(a^2 + b^2)} = 2\sqrt{(a^2 + b^2)}$ units

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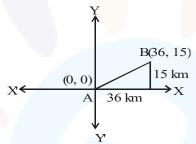
Sol. Part-I

Let the points be A(0, 0) and B(36, 15)

$$\therefore AB = \sqrt{(36 - 0)^2 + (15 - 0)^2}$$
$$= \sqrt{(36)^2 + (15)^2} = \sqrt{1296 + 225}$$
$$= \sqrt{1521} = \sqrt{39^2} = 39$$

Part-II

We have A(0, 0) and B(36, 15) as the positions of two towns



Here
$$x_1 = 0$$
, $x_2 = 36$ and $y_1 = 0$, $y_2 = 15$

:.
$$AB = \sqrt{(36-0)^2 + (15-0)^2} = 39 \text{ km}$$

Q3. Determine if the points (1,5), (2,3) and (-2, -11) are collinear.

Sol. The given points are :

A(1, 5), B(2, 3) and C(-2, -11).

Let us calculate the distance : AB, BC and CA by using distance formula.

AB =
$$\sqrt{(2-1)^2 + (3-5)^2} = \sqrt{(1)^2 + (-2)^2}$$

= $\sqrt{1+4} = \sqrt{5}$ units
BC = $\sqrt{(-2-2)^2 + (-11-3)^2} = \sqrt{(-4)^2 + (-14)^2}$
= $\sqrt{16+196} = \sqrt{212} = 2\sqrt{53}$ units

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CA =
$$\sqrt{(-2-1)^2 + (-11-5)^2}$$

= $\sqrt{(-3)^2 + (-16)^2} = \sqrt{9+256} = \sqrt{265}$
= $\sqrt{5} \times \sqrt{53}$ units

From the above we see that : $AB + BC \neq CA$

Hence the above stated points A(1, 5), B(2, 3) and C(-2, -11) are not collinear.

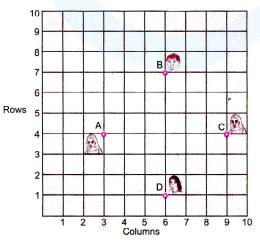
Q4. Check whether (5, -2), (6, 4) and (7, -2) are the vertices of an isosceles triangle.

Sol. Let the points be A(5, -2), B(6, 4) and C(7, -2).

$$AB = \sqrt{(6-5)^2 + [4-(-2)]^2}$$
$$= \sqrt{(1)^2 + (6)^2} = \sqrt{1+36} = \sqrt{37}$$
$$BC = \sqrt{(7-6)^2 + (-2-4)^2}$$
$$= \sqrt{(1)^2 + (-6)^2} = \sqrt{1+36} = \sqrt{37}$$
$$AC = \sqrt{(7-5)^2 + (-2-(-2))^2}$$
$$= \sqrt{(+2)^2 + (0)^2} = \sqrt{4+0} = 2$$

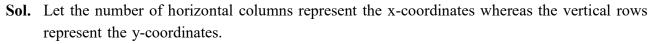
We have $AB = BC \neq AC$.

- $\therefore \Delta ABC$ is an isosceles triangle.
- Q5. In a classroom, 4 friends are seated at the points A, B, C and D as shown in fig. Champa and Chameli walk into the class and after observing for a few minutes Champa asks Chameli, "Don't you think ABCD is a rectangle?" Chameli disagrees. Using distance formula, find which of them is correct.



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are equal



: The points are : A(3, 4), B(6, 7), C(9, 4) and D(6, 1)

$$\therefore AB = \sqrt{(6-3)^2 + (7-4)^2}$$

$$= \sqrt{(3)^2 + (3)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}$$

$$BC = \sqrt{(9-6)^2 + (4-7)^2}$$

$$= \sqrt{3^2 + (-3)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}$$

$$CD = \sqrt{(6-9)^2 + (1-4)^2}$$

$$= \sqrt{(-3)^2 + (-3)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}$$

$$AD = \sqrt{(6-3)^2 + (1-4)^2}$$

$$= \sqrt{(3)^2 + (-3)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}$$
Since, AB = BC = CD = AD i.e., All the four sides
Also AC = $\sqrt{(9-3)^2 + (4-4)^2}$

$$= \sqrt{(+6)^2 + (0)^2} = 6$$
 and
BD = $\sqrt{(6-6)^2 + (1-7)^2} = \sqrt{(0)^2 + (-6)^2} = 6$
i.e., BD = AC

- \Rightarrow Both the diagonals are also equal.
- \therefore ABCD is a square.

Thus, Chameli is correct as ABCD is not a rectangle.

Q6. Name the quadrilateral formed, if any, by the following points, and give reasons for your answer.
(i) (-1, -2), (1, 0), (-1, 2), (-3, 0)
(ii) (-3, 5), (3, 1), (0, 3), (-1, -4)
(iii) (4, 5), (7, 6), (4, 3), (1, 2)

Sol. (i) A(-1, -2), B(1, 0), C(-1, 2), D(-3, 0) Determine distances : AB, BC, CD, DA, AC and BD.

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$$AB = \sqrt{(1 + 1)^{2} + (0 + 2)^{2}} = \sqrt{4 + 4} = \sqrt{8} = 2\sqrt{2}$$

$$BC = \sqrt{(-1 - 1)^{2} + (2 - 0)^{2}} = \sqrt{4 + 4} = \sqrt{8} = 2\sqrt{2}$$

$$CD = \sqrt{(-3 + 1)^{2} + (0 - 2)^{2}} = \sqrt{4 + 4} = \sqrt{8} = 2\sqrt{2}$$

$$DA = \sqrt{(-1 + 3)^{2} + (-2 - 0)^{2}} = \sqrt{4 + 4} = \sqrt{8} = 2\sqrt{2}$$

$$AB = BC = CD = DA$$
The sides of the quadrilateral are equal(1)
$$AC = \sqrt{(-1 + 1)^{2} + (2 + 2)^{2}} = \sqrt{0 + 16} = 4$$

$$BD = \sqrt{(-3 - 1)^{2} + (0 - 0)^{2}} = \sqrt{16 + 0} = 4$$

$$Diagonal AC = Diagonal BD......(2)$$
From (1) and (2) we conclude that ABCD is a square.
(ii) Let the points be A(-3, 5), B(3, 1), C(0, 3) and D(-1, -4).

$$\therefore AB = \sqrt{[3 - (-3)]^{2} + (1 - 5)^{2}} = \sqrt{6^{2} + (-4)^{2}} = \sqrt{36 + 16} = \sqrt{52} = 2\sqrt{13}$$

$$BC = \sqrt{(0 - 3)^{2} + (3 - 1)^{2}} = \sqrt{9 + 4} = \sqrt{13}$$

$$CD = \sqrt{(-1 - 0)^{2} + (-4 - 3)^{2}} = \sqrt{(-1)^{2} + (-7)^{2}} = \sqrt{1 + 49} = \sqrt{50}$$

$$DA = \sqrt{[-3 - (-1)]^{2} + [5 - (-4)]^{2}} = \sqrt{(-2)^{2} + (9)^{2}} = \sqrt{4 + 81} = \sqrt{85}$$

$$AC = \sqrt{[0 - (-3)]^{2} + (3 - 5)^{2}} = \sqrt{(3)^{2} + (-2)^{2}} = \sqrt{9 + 4} = \sqrt{13}$$

$$BD = \sqrt{(-1 - 3)^{2} + (-4 - 1)^{2}} = \sqrt{(-4)^{2} + (-5)^{2}} = \sqrt{9 + 4} = \sqrt{13}$$

$$BD = \sqrt{(-1 - 3)^{2} + (-4 - 1)^{2}} = \sqrt{(-4)^{2} + (-2)^{2}} = \sqrt{9 + 4} = \sqrt{13}$$

$$BD = \sqrt{(-1 - 3)^{2} + (-4 - 1)^{2}} = \sqrt{(-4)^{2} + (-2)^{2}} = \sqrt{9 + 4} = \sqrt{13}$$

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We see that $\sqrt{13} + \sqrt{13} = 2\sqrt{13}$ i.e., AC + BC = AB \Rightarrow A, B and C are collinear. Thus, ABCD is not a quadrilateral.

(iii) Let the points be A(4, 5), B(7, 6), C(4, 3) and D(1, 2).

$$\therefore AB = \sqrt{(7-4)^2 + (6-5)^2} = \sqrt{3^2 + 1^2} = \sqrt{10}$$

BC = $\sqrt{(4-7)^2 + (3-6)^2}$
= $\sqrt{(-3)^2 + (-3)^2} = \sqrt{18}$
CD = $\sqrt{(1-4)^2 + (2-3)^2}$
= $\sqrt{(-3)^2 + (-1)^2} = \sqrt{10}$
DA = $\sqrt{(1-4)^2 + (2-5)^2} = \sqrt{9+9} = \sqrt{18}$
AC = $\sqrt{(4-4)^2 + (3-5)^2} = \sqrt{0 + (-2)^2} = 2$
BD = $\sqrt{(1-7)^2 + (2-6)^2} = \sqrt{36 + 16} = \sqrt{52}$
Since, AB = CD, BC = DA [opposite sides of the quadrilateral are equal]
And AC \neq BD \Rightarrow Diagonals are unequal.
 \therefore ABCD is a parallelogram.

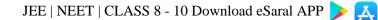
Q7. Find the point on the x-axis which is equidistant from (2, -5) and (-2, 9).

Sol. We know that any point on x-axis has its ordinate = 0Let the required point be P(x, 0).Let the given points be A(2, -5) and B(-2, 9)

$$\therefore AP = \sqrt{(x-2)^2 + 5^2} = \sqrt{x^2 - 4x + 4 + 25}$$
$$= \sqrt{x^2 - 4x + 29}$$
$$BP = \sqrt{[x - (-2)]^2 + (-9)^2} = \sqrt{(x+2)^2 + (-9)^2}$$
$$= \sqrt{x^2 + 4x + 4 + 81} = \sqrt{x^2 + 4x + 85}$$
Since, A and B are equidistant from P,

 \therefore AP = BP

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$$\Rightarrow \sqrt{x^2 - 4x + 29} = \sqrt{x^2 + 4x + 85}$$
$$\Rightarrow x^2 - 4x + 29 = x^2 + 4x + 85$$

$$\Rightarrow$$
 x²-4x-x²-4x = 85-29

$$\Rightarrow -8x = 56 \Rightarrow x = \frac{56}{9} = -7$$

 \therefore The required point is (-7, 0)

Q8. Find the values of y for which the distance between the points P(2, -3) and Q(10, y) is 10 units. **Sol.** Distance between P(2, -3) and Q(10, y) = 10 units

$$\Rightarrow \sqrt{(10-2)^2 + (y+3)^2} = 10$$

$$\Rightarrow 64 + (y+3)^2 = 100$$

$$\Rightarrow (y+3)^2 = 36$$

$$\Rightarrow y^2 + 6y + 9 = 36$$

$$y^2 + 6y - 27 = 0$$

$$\Rightarrow y^2 + 9y - 3y - 27 = 0$$

$$\Rightarrow y(y+9) - 3 (y+9) = 0$$

$$\Rightarrow (y+9) (y-3) = 0$$

$$\Rightarrow y + 9 = 0 \text{ or } y - 3 = 0$$

$$\Rightarrow y = -9 \text{ or } 3$$

Hence, there can be two values of y which are -9 and 3.

Q9. If Q (0,1) is equidistant from P(5, -3) and R(x, 6), find the values of x. Also find the distances QR and PR.

Sol. Here,
$$QP = \sqrt{(5-0)^2 + [(-3)-1]^2} = \sqrt{5^2 + (-4)^2}$$

 $= \sqrt{25+16} = \sqrt{41}$
 $QR = \sqrt{(x-0)^2 + (6-1)^2} = \sqrt{x^2 + 5^2} = \sqrt{x^2 + 25}$
 $\therefore QP = QR$
 $\therefore \sqrt{41} = \sqrt{x^2 + 25}$
Squaring both sides, we have $x^2 + 25 = 41$

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 \Rightarrow x² + 25 - 41 = 0 \Rightarrow x²-16=0 \Rightarrow x=± $\sqrt{16}$ =±4 Thus, the point R is (4, 6) or (-4, 6)Now, $QR = \sqrt{\left[(\pm 4) - (0)\right]^2 + (6 - 1)^2} = \sqrt{16 + 25} = \sqrt{41}$ and PR = $\sqrt{(\pm 4 - 5)^2 + (6 + 3)^2}$ \Rightarrow PR = $\sqrt{(-4-5)^2 + (6+3)^2}$ or $\sqrt{(4-5)^2 + (6+3)^2}$ \Rightarrow PR = $\sqrt{(-9)^2 + 9^2}$ or $\sqrt{1 + 81}$ \Rightarrow PR = $\sqrt{2 \times 9^2}$ or $\sqrt{82}$ \Rightarrow PR = $9\sqrt{2}$ or $\sqrt{82}$

Q10. Find a relation between x and y such that the point (x,y) is equidistant from the point (3, 6) and (-3, 4).

Sol. A(3,6) and B(-3, 4) are the given points. Point P (x, y) is equidistant from the points A and B.

$$\Rightarrow PA = PB$$

$$\Rightarrow \sqrt{(x-3)^{2} + (y-6)^{2}} = \sqrt{(x+3)^{2} + (y-4)^{2}}$$

$$\Rightarrow (x-3)^{2} + (y-6)^{2} = (x+3)^{2} + (y-4)^{2}$$

$$\Rightarrow (x^{2} - 6x + 9) + (y^{2} - 12y + 36)$$

$$= (x^{2} + 6x + 9) + (y^{2} - 8y + 16)$$

$$\Rightarrow - 6x - 12y + 45 = 6x - 8y + 25$$

$$\Rightarrow 12x + 4y - 20 = 0 \Rightarrow 3x + y - 5 = 0$$

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