

**Class X : MATH****Chapter 7 : Coordinate geometry****Questions & Answers - Exercise : 7.2 - NCERT Book**

**Q1.** Find the co-ordinates of the point which divides the line joining of  $(-1, 7)$  and  $(4, -3)$  in the ratio  $2 : 3$ .

**Sol.** Let the required point be  $P(x, y)$ .

Here the end points are  $(-1, 7)$  and  $(4, -3)$

$$\therefore \text{Ratio} = 2 : 3 = m_1 : m_2$$

$$\therefore x = \frac{m_1 x_2 + m_2 x_1}{m_1 + m_2} = \frac{(2 \times 4) + 3(-1)}{2 + 3}$$

$$= \frac{8 - 3}{5} = \frac{5}{5} = 1$$

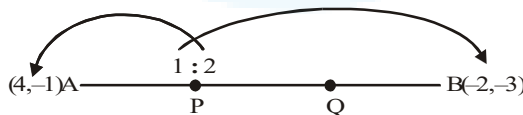
$$\text{And } y = \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2}$$

$$= \frac{2 \times (-3) + 3 \times 7}{2 + 3} = \frac{-6 + 21}{5} = \frac{15}{5} = 3$$

Thus, the required point is  $(1, 3)$ .

**Q2.** Find the coordinates of the points of trisection of the line segment joining  $(4, -1)$  and  $(-2, -3)$ .

**Sol.**



Points P and Q trisect the line segment joining the points  $A(4, -1)$  and  $B(-2, -3)$ ,  
i.e.,  $AP = PQ = QB$ .

Here, P divides AB in the ratio 1 : 2 and Q divides AB in the ratio 2 : 1.

$$\text{x-coordinate of P} = \frac{1 \times (-2) + 2 \times (4)}{1 + 2} = \frac{6}{3} = 2 ;$$

$$\text{y-coordinate of P} = \frac{1 \times (-3) + 2 \times (-1)}{1 + 2} = \frac{-5}{3}$$

Thus, the coordinates of P are  $\left(2, \frac{-5}{3}\right)$ .

$$\text{Now, x coordinate of Q} = \frac{2 \times (-2) + 1 \times (4)}{2 + 1} = 0 ;$$

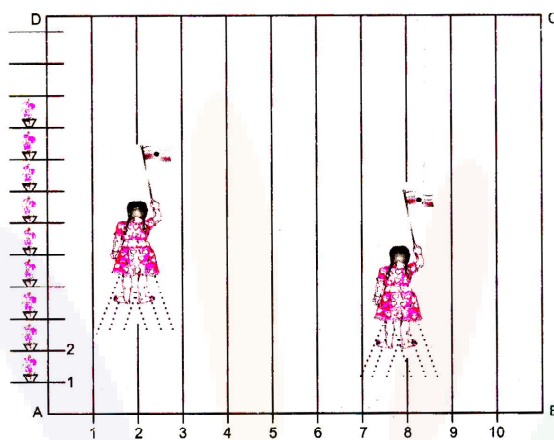
$$\text{y-coordinate of Q} = \frac{2 \times (-3) + 1 \times (-1)}{2 + 1} = -\frac{7}{3}$$

Thus, the coordinates of Q are  $\left(0, -\frac{7}{3}\right)$ .

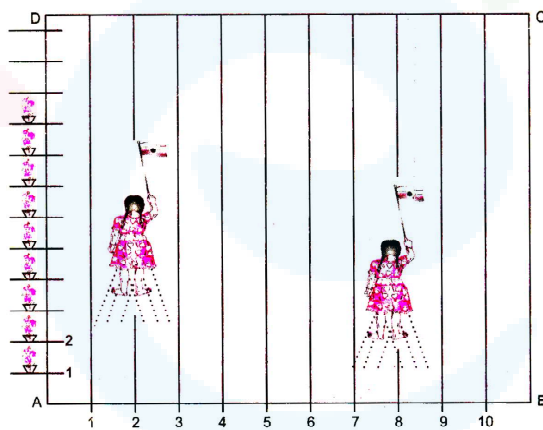
Hence, the points of trisection are  $P\left(2, \frac{-5}{3}\right)$  and  $Q\left(0, -\frac{7}{3}\right)$ .

- Q3.** To conduct Sports Day activities, in your rectangular shaped school ground ABCD, lines have been drawn with chalk powder at a distance of 1 m each. 100 flower pots have been placed at a distance of 1 m from each other along AD, as shown in fig. Niharika runs  $\frac{1}{4}$ th the distance AD on the 2nd line and posts a green flag. Preet runs  $\frac{1}{5}$ th the distance AD on the eighth line and posts a red flag. What is the distance between both the flags? If Rashmi has to post a blue flag exactly halfway between the line segment joining the two flags, where should she post her

flag?



**Sol.** Let us consider 'A' as origin, then



AB is the x-axis.

AD is the y-axis.

Now, the position of green flag-post is

$$\left(2, \frac{100}{4}\right) \text{ or } (2, 25)$$

And, the position of red flag-post is

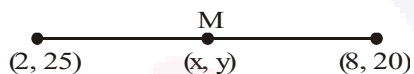
$$\left(8, \frac{100}{5}\right) \text{ or } (8, 20)$$

$\Rightarrow$  Distance between both the flags

$$= \sqrt{(8-2)^2 + (20-25)^2}$$

$$= \sqrt{6^2 + (-5)^2} = \sqrt{36+25} = \sqrt{61}$$

Let the mid-point of the line segment joining the two flags be  $M(x, y)$ .



$$\therefore x = \frac{2+8}{2} \text{ and } y = \frac{25+20}{2}$$

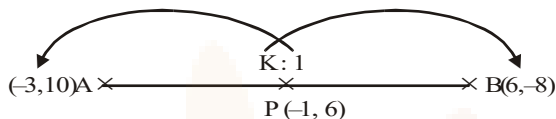
$$\text{or } x = 5 \text{ and } y = 22.5$$

Thus, the blue flag is on the 5th line at a distance 22.5 m above AB.

**Q4.** Find the ratio in which the line segment joining the points  $(-3, 10)$  and  $(6, -8)$  is divided by  $(-1,$

6).

**Sol.** Let the required ratio be  $K : 1$



Comparing x-coordinate

$$\frac{k \times (6) + 1 \times (-3)}{k+1} = -1$$

$$\Rightarrow 6k - 3 = -k - 1$$

$$\Rightarrow 7k = 2$$

$$\Rightarrow k = \frac{2}{7}$$

Comparing y-coordinate

$$\frac{k \times (-8) + 1 \times (10)}{k+1} = 6$$

$$\Rightarrow -8k + 10 = 6k + 6$$

$$\Rightarrow -8K - 6K = 6 - 10$$

$$\Rightarrow -14K = -4$$

$$\Rightarrow k = \frac{2}{7}$$

**Q5.** Find the ratio in which the line segment joining

A(1, -5) and B(-4, 5) is divided by the x-axis. Also find the coordinates of the point of division.

**Sol.** The given points are : A(1, -5) and B(-4, 5). Let the required ratio =  $k : 1$  and the required point be P(x, y)

**Part-I :** To find the ratio

Since, the point P lies on x-axis,

$\therefore$  Its y-coordinate is 0.

$$x = \frac{m_1 x_2 + m_2 x_1}{m_1 + m_2} \text{ and } 0 = \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2}$$

$$\Rightarrow x = \frac{-4k + 1}{k + 1} \text{ and } 0 = \frac{5k - 5}{k + 1}$$

$$\Rightarrow x(k + 1) = -4k + 1$$

$$\text{and } 5k - 5 = 0 \Rightarrow k = 1$$

$$\Rightarrow x(k + 1) = -4k + 1$$

$$\Rightarrow x(1 + 1) = -4 + 1 \quad [ \because k = 1 ]$$

$$\Rightarrow 2x = -3$$

$$\Rightarrow x = -\frac{3}{2}$$

$\therefore$  The required ratio  $k : 1 = 1 : 1$

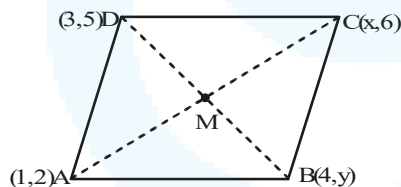
$$\text{Coordinates of P are } (x, 0) = \left( -\frac{3}{2}, 0 \right)$$

**Q6.** If  $(1, 2)$ ,  $(4, y)$ ,  $(x, 6)$  and  $(3, 5)$  are the vertices of a parallelogram taken in order, find  $x$  and  $y$ .

**Sol.** Mid-point of the diagonal AC has x-coordinate

$$= \frac{x+1}{2} \text{ and y-coordinate} = \frac{6+2}{2} = 4$$

i.e.,  $\left( \frac{x+1}{2}, 4 \right)$  is the mid-point of AC.



Similarly, mid-point of the diagonal BD is

$$\left( \frac{4+3}{2}, \frac{y+5}{2} \right), \text{ i.e., } \left( \frac{7}{2}, \frac{y+5}{2} \right)$$

We know that the two diagonals AC and BD bisect each other at M. Therefore,

$$\left(\frac{x+1}{2}, 4\right) \text{ and } \left(\frac{7}{2}, \frac{y+5}{2}\right). \text{ Coincide}$$

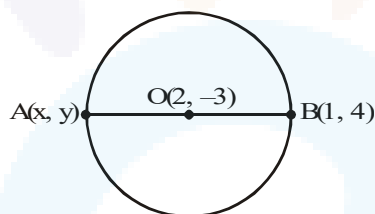
$$\Rightarrow \frac{x+1}{2} = \frac{7}{2} \text{ and } \frac{y+5}{2} = 4$$

$$\Rightarrow x = 6 \text{ and } y = 3$$

**Q7.** Find the coordinates of a point A, where AB is the diameter of a circle whose centre is (2, -3) and B is (1, 4).

**Sol.** Here, centre of the circle is O(2, -3)

Let the end points of the diameter be A(x, y) and B(1, 4)



The centre of a circle bisects the diameter.

$$\therefore 2 = \frac{x+1}{2} \Rightarrow x + 1 = 4 \text{ or } x = 3$$

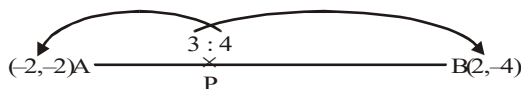
$$\text{And } -3 = \frac{y+4}{2} \Rightarrow y + 4 = -6 \text{ or } y = -10$$

Here, the coordinates of A are (3, -10)

**Q8.** If A and B are (-2, -2) and (2, -4), respectively, find the coordinates of P such that  $AP = \frac{3}{7}$

AB and P lies on the line segment AB.

**Sol.**



$$AP = \frac{3}{7} AB,$$

$$BP = AB - AP = AB - \frac{3}{7} AB = \frac{4}{7} AB$$

$$\frac{AP}{BP} = \frac{\frac{3}{7} AB}{\frac{4}{7} AB} = \frac{3}{4}$$

Thus, P divides AB in the ratio 3 : 4.

$$\text{x-coordinate of P} = \frac{3 \times (2) + 4 \times (-2)}{3 + 4} = -\frac{2}{7}$$

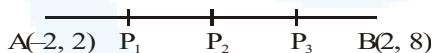
$$\text{y-coordinate of P} = \frac{3 \times (-4) + 4 \times (-2)}{3 + 4} = -\frac{20}{7}$$

Hence, the coordinates of P are  $\left(-\frac{2}{7}, -\frac{20}{7}\right)$ .

**Q9.** Find the coordinates of the points which divide the line segment joining A (-2, 2) and B (2, 8) into four equal parts.

**Sol.** Here, the given points are A(-2, 2) and B(2, 8)

Let  $P_1$ ,  $P_2$  and  $P_3$  divide AB in four equal parts.



$$\therefore AP_1 = P_1P_2 = P_2P_3 = P_3B$$

Obviously,  $P_2$  is the mid-point of AB

$\therefore$  Coordinates of  $P_2$  are

$$\left(\frac{-2+2}{2}, \frac{2+8}{2}\right) \text{ or } (0, 5)$$

Again,  $P_1$  is the mid-point of  $AP_2$ .

$\therefore$  Coordinates of  $P_1$  are



$$\left(\frac{-2+0}{2}, \frac{2+5}{2}\right) \text{ or } \left(-1, \frac{7}{2}\right)$$

Also  $P_3$  is the mid-point of  $P_2B$ .

$\therefore$  Coordinates of  $P_3$  are

$$\left(\frac{0+2}{2}, \frac{5+8}{2}\right) \text{ or } \left(1, \frac{13}{2}\right)$$

Thus, the coordinates of  $P_1$ ,  $P_2$  and  $P_3$  are  $\left(-1, \frac{7}{2}\right)$ ,  $(0, 5)$  and  $\left(1, \frac{13}{2}\right)$  respectively.

**Q10.** Find the area of a rhombus if its vertices are  $(3, 0)$ ,  $(4, 5)$ ,  $(-1, 4)$  and  $(-2, -1)$  taken in order.

**Sol.** Diagonals AC and BD bisect each other at right angle to each other at O.

$$AC = \sqrt{(-1-3)^2 + (4-0)^2}$$

$$= \sqrt{16+16} = \sqrt{32} = 4\sqrt{2}$$

$$BD = \sqrt{(4+2)^2 + (5+1)^2} = \sqrt{36+36} = 6\sqrt{2}$$

$$\text{Then } OA = \frac{1}{2} AC = \frac{1}{2} \times 4\sqrt{2} = 2\sqrt{2}$$

$$OB = \frac{1}{2} BD = \frac{1}{2} \times 6\sqrt{2} = 3\sqrt{2}$$

$$\text{Area of } \triangle AOB = \frac{1}{2} (OA) \times (OB) = \frac{1}{2} \times 2\sqrt{2} \times 3\sqrt{2} = 6 \text{ sq. units}$$

Hence, the area of the rhombus ABCD

$$= 4 \times \text{area of } \triangle AOB = 4 \times 6 = 24 \text{ sq. units.}$$