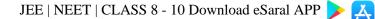
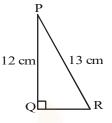


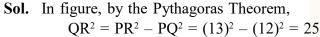
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Q2. In fig, find tan $P - \cot R$.

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$$\Rightarrow$$
 QR = $\sqrt{25}$ = 5 cm

In $\triangle PQR$ right angled at Q, QR = 5 cm is side opposite to the angle P and PQ = 12 cm is side adjacent to the angle P.

Therefore, $\tan P = \frac{QR}{PQ} = \frac{5}{12}$.

Now, QR = 5 cm is side adjacent to the angle R and PQ = 12 cm is side opposite to the angle R.

Therefore, $\cot R = \frac{QR}{PQ} = \frac{5}{12}$

Hence, $\tan P - \cot R = \frac{5}{12} - \frac{5}{12} = 0$

Q3. If $\sin A = \frac{3}{4}$, calculate $\cos A$ and $\tan A$.

Sol. In figure,

$$\sin A = \frac{3}{4}$$
$$\Rightarrow \frac{BC}{AC} = \frac{3}{4}$$
$$\Rightarrow BC = 3k$$
and AC = 4k
where k is the set of the

where k is the constant of proportionality.

By Pythagoras Theorem,

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$$AB^{2} = AC^{2} - BC^{2} = (4k)^{2} - (3k)^{2} = 7k^{2}$$

$$\Rightarrow AB = \sqrt{7} k$$
So, $\cos A = \frac{AB}{AC} = \frac{\sqrt{7}k}{4k} = \frac{\sqrt{7}}{4}$
and $\tan A = \frac{BC}{AB} = \frac{3k}{\sqrt{7k}} = \frac{3}{\sqrt{7}}$
Q4. Given 15 cot A = 8, find sin A and sec A.
Sol. $\cot A = \frac{8}{15}$

$$\Rightarrow \frac{AB}{BC} = \frac{8}{15}$$

$$\Rightarrow AB = 8k$$
and BC = 15 k
Now, AC = $\sqrt{(8k)^{2} + (15k)^{2}} = 17 k$
sin A = $\frac{BC}{AC} = \frac{15k}{17k} = \frac{15}{17}$, sec A = $\frac{AC}{AB} = \frac{17k}{8k} = \frac{17}{8}$
Q5. Given sec $\theta = \frac{13}{12}$, calculate all other trigonometric ratios.

Sol. sec $\theta = \frac{13}{12}$

 $\Rightarrow \frac{AC}{BC} = \frac{13}{12}$

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By Pythagoras Theorem, $AC^2 = AB^2 + BC^2$ $(13k)^2 = AB^2 + (12k)^2$ $AB^2 = 169k^2 - 144 k^2$ $AB = \sqrt{25 k^2} = 5 k$ $\sin \theta = \frac{AB}{AC} = \frac{5k}{13k} = \frac{5}{13}$ $\cos \theta = \frac{BC}{AC} = \frac{12k}{13k} = \frac{12}{13}$ $\tan \theta = \frac{AB}{BC} = \frac{5k}{12k} = \frac{5}{12}$ $\cot \theta = \frac{BC}{AB} = \frac{12k}{5k} = \frac{12}{5}$ $\operatorname{cosec} \theta = \frac{AC}{AB} = \frac{13k}{5k} = \frac{13}{5}$

Q6. If $\angle A$ and $\angle B$ are acute angles such that $\cos A = \cos B$, then show that $\angle A = \angle B$.

13

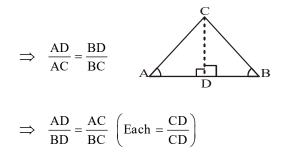
12

B

Sol. In figure $\angle A$ and $\angle B$ are acute angles of $\triangle ABC$.



We are given that $\cos A = \cos B$



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 $\Rightarrow \Delta ADC \sim \Delta BDC$ (SSS similarity criterion) $\Rightarrow \angle A = \angle B$

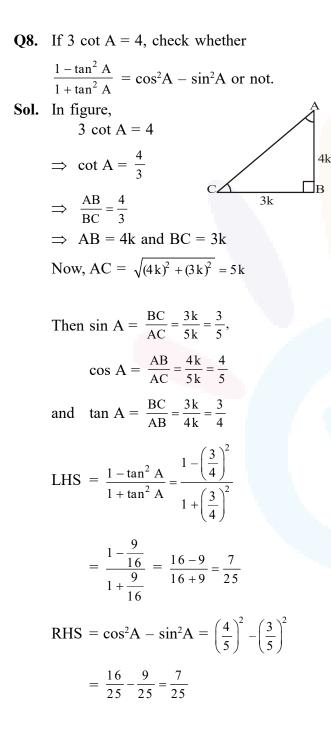
(: all the corresponding angles of two similar triangles are equal)

Q7. If $\cot \theta = \frac{7}{8}$, evaluate : (i) $\frac{(1+\sin\theta)(1-\sin\theta)}{(1+\cos\theta)(1-\cos\theta)}$ (ii) $\cot^2\theta$ Sol. In figure, $\cot \theta = \frac{7}{8}$ 8k $\Rightarrow \frac{AB}{BC} = \frac{7}{8}$ AΔθ \Box_{B} AB = 7 k \Rightarrow and BC = 8 kNow, $AC^2 = AB^2 + BC^2 = (7k)^2 + (8k)^2$ $= 113 k^2$ $AC = \sqrt{113} k$ \Rightarrow Then sin $\theta = \frac{BC}{AC} = \frac{8k}{\sqrt{113}k} = \frac{8}{\sqrt{113}}$ and $\cos \theta = \frac{AB}{AC} = \frac{7k}{\sqrt{113}k} = \frac{7}{\sqrt{113}}$. (i) $\frac{(1+\sin\theta)(1-\sin\theta)}{(1+\cos\theta)(1-\cos\theta)} = \frac{\left(1+\frac{8}{\sqrt{113}}\right)\left(1-\frac{8}{\sqrt{113}}\right)}{\left(1+\frac{7}{\sqrt{113}}\right)\left(1-\frac{7}{\sqrt{113}}\right)}$ $\frac{(\sqrt{113}+8)(\sqrt{113}-8)}{(\sqrt{113}+7)(\sqrt{113}-7)} = \frac{(\sqrt{113})^2 - (8)^2}{(\sqrt{113})^2 - (7)^2}$ $\{:: (a + b) (a - b) = a^2 - b^2\}$ $=\frac{113-64}{113-49}=\frac{49}{64}$ (ii) $\cot\theta = \frac{7}{8} \implies \cot^2 \theta = \left(\frac{7}{8}\right)^2 = \frac{49}{64}$

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Therefore, LHS = RHS,

i.e.,
$$\frac{1 - \tan^2 A}{1 + \tan^2 A} = \cos^2 A - \sin^2 A$$
$$\left(\because \text{ Each side} = \frac{7}{25}\right)$$

Q9. In triangle ABC right angled at B, if $\tan A = \frac{1}{\sqrt{3}}$, find the value of :

- (i) $\sin A \cos C + \cos A \sin C$
- (ii) $\cos A \cos C \sin A \sin C$.

Sol. $\tan A = \frac{1}{\sqrt{3}}$ $\frac{BC}{BA} = \frac{1}{\sqrt{3}}$ BC = k and BA = $\sqrt{3}k^{B}$ $AC^2 = BC^2 + BA^2$ $= k^{2} + (\sqrt{3}k)^{2} = k^{2} + 3k^{2} = 4k^{2}$ $AC = \sqrt{4k^2} = 2k$

(i) $\sin A.\cos C + \cos A \sin C$

$$= \frac{1}{2} \times \frac{1}{2} + \frac{\sqrt{3}}{2} \times \frac{\sqrt{3}}{2} = \frac{1}{4} + \frac{3}{4} = 1$$

(ii) cos A . cos C - sin A . sin C

$$= \frac{\sqrt{3}}{2} \times \frac{1}{2} - \frac{1}{2} \times \frac{\sqrt{3}}{2} = \frac{\sqrt{3}}{4} - \frac{\sqrt{3}}{4} = 0$$

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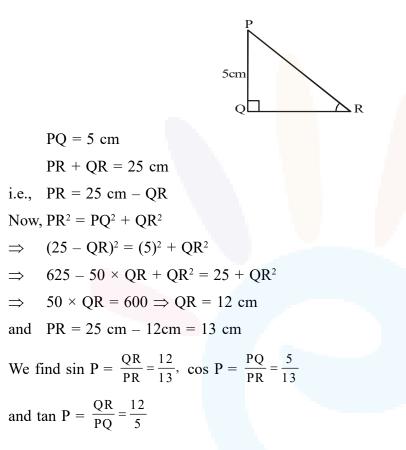
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7

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Q10. In $\triangle PQR$, right angled at Q, PR + QR = 25 cm and PQ = 5 cm. Determine the values of sin P, cos P and tan P.

Sol. In figure,



Q11. State whether the following are true or false. Justify your answer.

- (i) The value of tan A is always less than 1.
- (ii) sec A = $\frac{12}{5}$ for some value of angle A.
- (iii) cos A is the abbreviation used for the cosecant of angle A.
- (iv) cot A is the product of cot and A.
- (v) $\sin \theta = \frac{4}{3}$ for some angle θ .

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Sol. (i) False.

We know that $60^\circ = \sqrt{3} > 1$.

(ii) True.

We know that value of sec A is always ≥ 1 .

(iii) False.

Because cos A is abbreviation used for cosine A.

- (iv) False, because cot A is not the product of cot and A.
- (v) False, because value of sin cannot be more than 1.