



1

Class XI : Maths Chapter 2 : Related And Functions

Questions and Solutions | Exercise 2.1 - NCERT Books

Question 1:

If
$$\left(\frac{x}{3}+1, y-\frac{2}{3}\right)=\left(\frac{5}{3}, \frac{1}{3}\right)$$
, find the values of x and y.

Answer

It is given that
$$\left(\frac{x}{3}+1, y-\frac{2}{3}\right)=\left(\frac{5}{3}, \frac{1}{3}\right)$$
.

Since the ordered pairs are equal, the corresponding elements will also be equal.

Therefore,
$$\frac{x}{3} + 1 = \frac{5}{3}$$
 and $\frac{x}{3} + 1 = \frac{5}{3}$ and $\frac{x}{3} + 1 = \frac{5}{3}$ $\Rightarrow \frac{x}{3} = \frac{5}{3} - 1$ $y - \frac{2}{3} = \frac{1}{3}$ $\Rightarrow \frac{x}{3} = \frac{2}{3}$ $\Rightarrow y = \frac{1}{3} + \frac{2}{3}$ $\Rightarrow x = 2$ $\Rightarrow y = 1$ $\therefore x = 2$ and $y = 1$

Question 2:

If the set A has 3 elements and the set $B = \{3, 4, 5\}$, then find the number of elements in $(A \times B)$?

Answer

It is given that set A has 3 elements and the elements of set B are 3, 4, and 5.

 \Rightarrow Number of elements in set B = 3

Number of elements in $(A \times B)$

= (Number of elements in A) × (Number of elements in B)

 $= 3 \times 3 = 9$

Thus, the number of elements in $(A \times B)$ is 9.

Question 3:

If $G = \{7, 8\}$ and $H = \{5, 4, 2\}$, find $G \times H$ and $H \times G$.

Answer

 $G = \{7, 8\}$ and $H = \{5, 4, 2\}$

We know that the Cartesian product $P \times Q$ of two non-empty sets P and Q is defined as $P \times Q = \{(p, q): p \in P, q \in Q\}$

$$::G \times H = \{(7,5), (7,4), (7,2), (8,5), (8,4), (8,2)\}$$

 $H \times G = \{(5,7), (5,8), (4,7), (4,8), (2,7), (2,8)\}$

Question 4:

State whether each of the following statement are true or false. If the statement is false, rewrite the given statement correctly.





```
(ii) If A and B are non-empty sets, then A \times B is a non-empty set of ordered pairs (x, y)
such that x \in A and y \in B.
(iii) If A = \{1, 2\}, B = \{3, 4\}, then A \times (B \cap \Phi) = \Phi.
Answer
 (i) False
If P = \{m, n\} and Q = \{n, m\}, then
P \times Q = \{(m, m), (m, n), (n, m), (n, n)\}
(ii) True
(iii) True
Ouestion 5:
If A = \{-1, 1\}, find A \times A \times A.
Answer
It is known that for any non-empty set A, A \times A \times A is defined as
A \times A \times A = \{(a, b, c): a, b, c \in A\}
It is given that A = \{-1, 1\}
\therefore A \times A \times A = \{(-1, -1, -1), (-1, -1, 1), (-1, 1, -1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1), (-1, 1, 1
(1, -1, -1), (1, -1, 1), (1, 1, -1), (1, 1, 1)
Ouestion 6:
If A × B = \{(a, x), (a, y), (b, x), (b, y)\}. Find A and B.
Answer
It is given that A \times B = \{(a, x), (a, y), (b, x), (b, y)\}
We know that the Cartesian product of two non-empty sets P and Q is defined as P \times Q
= \{(p, q): p \in P, q \in Q\}
.. A is the set of all first elements and B is the set of all second elements.
Thus, A = \{a, b\} and B = \{x, y\}
Question 7:
Let A = \{1, 2\}, B = \{1, 2, 3, 4\}, C = \{5, 6\} and D = \{5, 6, 7, 8\}. Verify that
(i) A \times (B \cap C) = (A \times B) \cap (A \times C)
(ii) A \times C is a subset of B \times D
Answer
  (i) To verify: A \times (B \cap C) = (A \times B) \cap (A \times C)
We have B \cap C = {1, 2, 3, 4} \cap {5, 6} = \Phi
\thereforeL.H.S. = A × (B \cap C) = A × \Phi = \Phi
A \times B = \{(1, 1), (1, 2), (1, 3), (1, 4), (2, 1), (2, 2), (2, 3), (2, 4)\}
A \times C = \{(1, 5), (1, 6), (2, 5), (2, 6)\}
\therefore R.H.S. = (A × B) \cap (A × C) = \Phi
∴L.H.S. = R.H.S
Hence, A \times (B \cap C) = (A \times B) \cap (A \times C)
(ii) To verify: A \times C is a subset of B \times D
A \times C = \{(1, 5), (1, 6), (2, 5), (2, 6)\}
B \times D = \{(1, 5), (1, 6), (1, 7), (1, 8), (2, 5), (2, 6), (2, 7), (2, 8), (3, 5), (3, 6), (3, 7), (2, 8), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3, 1, 1), (3,
(3, 8), (4, 5), (4, 6), (4, 7), (4, 8)
We can observe that all the elements of set A \times C are the elements of set B \times D.
Therefore, A \times C is a subset of B \times D.
```

(i) If $P = \{m, n\}$ and $Q = \{n, m\}$, then $P \times Q = \{(m, n), (n, m)\}$.





Question 8:

Let $A = \{1, 2\}$ and $B = \{3, 4\}$. Write $A \times B$. How many subsets will $A \times B$ have? List them.

Answer

A =
$$\{1, 2\}$$
 and B = $\{3, 4\}$
 \therefore A × B = $\{(1, 3), (1, 4), (2, 3), (2, 4)\}$
 $\Rightarrow n(A \times B) = 4$

We know that if C is a set with n(C) = m, then $n[P(C)] = 2^m$.

Therefore, the set $A \times B$ has $2^4 = 16$ subsets. These are

Ouestion 9:

Let A and B be two sets such that n(A) = 3 and n(B) = 2. If (x, 1), (y, 2), (z, 1) are in A \times B, find A and B, where x, y and z are distinct elements.

It is given that n(A) = 3 and n(B) = 2; and (x, 1), (y, 2), (z, 1) are in $A \times B$. We know that A = Set of first elements of the ordered pair elements of $A \times B$ $A \times B$

Question 10:

The Cartesian product $A \times A$ has 9 elements among which are found (-1, 0) and (0, 1). Find the set A and the remaining elements of $A \times A$.

Answer

```
We know that if n(A) = p and n(B) = q, then n(A \times B) = pq.

\therefore n(A \times A) = n(A) \times n(A)

It is given that n(A \times A) = 9

\therefore n(A) \times n(A) = 9

\Rightarrow n(A) = 3
```

The ordered pairs (-1, 0) and (0, 1) are two of the nine elements of A \times A. We know that A \times A = {(a, a): $a \in$ A}. Therefore, -1, 0, and 1 are elements of A. Since n(A) = 3, it is clear that A = {-1, 0, 1}. The remaining elements of set A \times A are (-1, -1), (-1, 1), (0, -1), (0, 0), (1, -1), (1, 0), and (1, 1)