#### Class XI : Maths Chapter 3 : Trignometric Functions

#### Questions and Solutions | Exercise 3.3 - NCERT Books

**Question 1:** 

$$\sin^2\frac{\pi}{6} + \cos^2\frac{\pi}{3} - \tan^2\frac{\pi}{4} = -\frac{1}{2}$$

Answer

L.H.S. = 
$$\frac{\sin^2 \frac{\pi}{6} + \cos^2 \frac{\pi}{3} - \tan^2 \frac{\pi}{4}}{=\left(\frac{1}{2}\right)^2 + \left(\frac{1}{2}\right)^2 - (1)^2}$$

$$=\frac{1}{4}+\frac{1}{4}-1=-\frac{1}{2}$$

**Question 2:** 

Prove that 
$$2\sin^2\frac{\pi}{6} + \csc^2\frac{7\pi}{6}\cos^2\frac{\pi}{3} = \frac{3}{2}$$

Answer

L.H.S. = 
$$2\sin^2 \frac{\pi}{6} + \cos ec^2 \frac{7\pi}{6} \cos^2 \frac{\pi}{3}$$
  
=  $2\left(\frac{1}{2}\right)^2 + \csc^2\left(\pi + \frac{\pi}{6}\right)\left(\frac{1}{2}\right)^2$   
=  $2 \times \frac{1}{4} + \left(-\cos ec \frac{\pi}{6}\right)^2 \left(\frac{1}{4}\right)$   
=  $\frac{1}{2} + \left(-2\right)^2 \left(\frac{1}{4}\right)$   
=  $\frac{1}{2} + \frac{4}{4} = \frac{1}{2} + 1 = \frac{3}{2}$   
= R.H.S.

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**Question 3:** 

Prove that 
$$\cot^2 \frac{\pi}{6} + \csc \frac{5\pi}{6} + 3\tan^2 \frac{\pi}{6} = 6$$
  
Answer

L.H.S. = 
$$\cot^2 \frac{\pi}{6} + \csc \frac{5\pi}{6} + 3\tan^2 \frac{\pi}{6}$$
  
=  $(\sqrt{3})^2 + \csc \left(\pi - \frac{\pi}{6}\right) + 3\left(\frac{1}{\sqrt{3}}\right)^2$   
=  $3 + \csc \frac{\pi}{6} + 3 \times \frac{1}{3}$   
=  $3 + 2 + 1 = 6$   
= R.H.S

**Question 4:** 

Prove that 
$$2\sin^2\frac{3\pi}{4} + 2\cos^2\frac{\pi}{4} + 2\sec^2\frac{\pi}{3} = 10$$
  
Answer

L.H.S = 
$$2\sin^2 \frac{3\pi}{4} + 2\cos^2 \frac{\pi}{4} + 2\sec^2 \frac{\pi}{3}$$
  
=  $2\left\{\sin\left(\pi - \frac{\pi}{4}\right)\right\}^2 + 2\left(\frac{1}{\sqrt{2}}\right)^2 + 2(2)^2$   
=  $2\left\{\sin\frac{\pi}{4}\right\}^2 + 2 \times \frac{1}{2} + 8$   
=  $2\left(\frac{1}{\sqrt{2}}\right)^2 + 1 + 8$   
=  $10$   
= R.H.S



**Question 5:** Find the value of: (i) sin 75° (ii) tan 15° Answer (i)  $\sin 75^\circ = \sin (45^\circ + 30^\circ)$ = sin 45° cos 30° + cos 45° sin 30°  $[\sin (x + y) = \sin x \cos y + \cos x \sin y]$  $= \left(\frac{1}{\sqrt{2}}\right) \left(\frac{\sqrt{3}}{2}\right) + \left(\frac{1}{\sqrt{2}}\right) \left(\frac{1}{2}\right)$  $=\frac{\sqrt{3}}{2\sqrt{2}}+\frac{1}{2\sqrt{2}}=\frac{\sqrt{3}+1}{2\sqrt{2}}$ (ii) tan 15° = tan (45° - 30°)  $=\frac{\tan 45^\circ - \tan 30^\circ}{1 + \tan 45^\circ \tan 30^\circ}$  $\tan(x-y) = \frac{\tan x - \tan y}{1 + \tan x \tan y}$  $=\frac{1-\frac{1}{\sqrt{3}}}{1+1\left(\frac{1}{\sqrt{3}}\right)}=\frac{\frac{\sqrt{3}-1}{\sqrt{3}}}{\frac{\sqrt{3}+1}{\sqrt{3}}}$  $=\frac{\sqrt{3}-1}{\sqrt{3}+1}=\frac{\left(\sqrt{3}-1\right)^2}{\left(\sqrt{3}+1\right)\left(\sqrt{3}-1\right)}=\frac{3+1-2\sqrt{3}}{\left(\sqrt{3}\right)^2-\left(1\right)^2}$  $=\frac{4-2\sqrt{3}}{3-1}=2-\sqrt{3}$ 

**Question 6:** 

Prove that: 
$$\cos\left(\frac{\pi}{4} - x\right)\cos\left(\frac{\pi}{4} - y\right) - \sin\left(\frac{\pi}{4} - x\right)\sin\left(\frac{\pi}{4} - y\right) = \sin(x+y)$$
  
Answer  
 $\cos\left(\frac{\pi}{4} - x\right)\cos\left(\frac{\pi}{4} - y\right) - \sin\left(\frac{\pi}{4} - x\right)\sin\left(\frac{\pi}{4} - y\right)$   
 $= \frac{1}{2}\left[2\cos\left(\frac{\pi}{4} - x\right)\cos\left(\frac{\pi}{4} - y\right)\right] + \frac{1}{2}\left[-2\sin\left(\frac{\pi}{4} - x\right)\sin\left(\frac{\pi}{4} - y\right)\right]$   
 $= \frac{1}{2}\left[\cos\left\{\left(\frac{\pi}{4} - x\right) + \left(\frac{\pi}{4} - y\right)\right\} + \cos\left\{\left(\frac{\pi}{4} - x\right) - \left(\frac{\pi}{4} - y\right)\right\}\right]$   
 $+ \frac{1}{2}\left[\cos\left\{\left(\frac{\pi}{4} - x\right) + \left(\frac{\pi}{4} - y\right)\right\} - \cos\left\{\left(\frac{\pi}{4} - x\right) - \left(\frac{\pi}{4} - y\right)\right\}\right]$   
 $\left[\because 2\cos A\cos B = \cos(A + B) + \cos(A - B)\right]$   
 $= 2 \times \frac{1}{2}\left[\cos\left\{\left(\frac{\pi}{4} - x\right) + \left(\frac{\pi}{4} - y\right)\right\}\right]$   
 $= \cos\left[\frac{\pi}{2} - (x+y)\right]$   
 $= \sin(x+y)$   
 $= R.H.S$ 

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**Question 7:** 

$$\frac{\tan\left(\frac{\pi}{4}+x\right)}{\tan\left(\frac{\pi}{4}-x\right)} = \left(\frac{1+\tan x}{1-\tan x}\right)^2$$

Prove that:

#### Answer

It is known that  $\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$  and  $\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$ 

$$\frac{\tan\left(\frac{\pi}{4}+x\right)}{\tan\left(\frac{\pi}{4}-x\right)} = \frac{\left(\frac{\tan\frac{\pi}{4}+\tan x}{1-\tan\frac{\pi}{4}\tan x}\right)}{\left(\frac{\tan\frac{\pi}{4}-\tan x}{1+\tan\frac{\pi}{4}\tan x}\right)} = \frac{\left(\frac{1+\tan x}{1-\tan x}\right)}{\left(\frac{1-\tan x}{1+\tan x}\right)^2} = \text{R.H.S.}$$
  
L.H.S. =

**Question 8:** 

$$\frac{\cos(\pi + x)\cos(-x)}{\sin(\pi - x)\cos\left(\frac{\pi}{2} + x\right)} = \cot^2 x$$
  
Prove that

Answer

L.H.S. = 
$$\frac{\cos(\pi + x)\cos(-x)}{\sin(\pi - x)\cos\left(\frac{\pi}{2} + x\right)}$$
$$= \frac{\left[-\cos x\right]\left[\cos x\right]}{(\sin x)(-\sin x)}$$
$$= \frac{-\cos^2 x}{-\sin^2 x}$$
$$= \cot^2 x$$
$$= R.H.S.$$

**Question 9:** 

$$\cos\left(\frac{3\pi}{2}+x\right)\cos\left(2\pi+x\right)\left[\cot\left(\frac{3\pi}{2}-x\right)+\cot\left(2\pi+x\right)\right]=1$$

Answer

L.H.S. = 
$$\cos\left(\frac{3\pi}{2} + x\right)\cos\left(2\pi + x\right)\left[\cot\left(\frac{3\pi}{2} - x\right) + \cot\left(2\pi + x\right)\right]$$

$$= \sin x \cos x \left[ \tan x + \cot x \right]$$
$$= \sin x \cos x \left( \frac{\sin x}{\cos x} + \frac{\cos x}{\sin x} \right)$$
$$= \left( \sin x \cos x \right) \left[ \frac{\sin^2 x + \cos^2 x}{\sin x \cos x} \right]$$
$$= 1 = \text{R.H.S.}$$

**Question 10:** 

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Prove that  $\sin(n + 1)x \sin(n + 2)x + \cos(n + 1)x \cos(n + 2)x = \cos x$ Answer

L.H.S. = sin (n + 1)x sin(n + 2)x + cos (n + 1)x cos(n + 2)x

$$= \frac{1}{2} \Big[ 2\sin(n+1)x\sin(n+2)x + 2\cos(n+1)x\cos(n+2)x \Big]$$
  
= 
$$\frac{1}{2} \Big[ \cos\{(n+1)x - (n+2)x\} - \cos\{(n+1)x + (n+2)x\} + \cos\{(n+1)x - (n+2)x\} \Big]$$
  
= 
$$\frac{1}{2} \sum_{n=1}^{\infty} -2\sin A \sin B = \cos(A+B) - \cos(A-B) \Big]$$
  
= 
$$\frac{1}{2} \sum_{n=1}^{\infty} 2\cos A \cos B = \cos(A+B) + \cos(A-B) \Big]$$
  
= 
$$\frac{1}{2} \sum_{n=1}^{\infty} 2\cos \{(n+1)x - (n+2)x\} = \cos(-x) = \cos x = R.H.S.$$

**Question 11:** 

Prove that  $\cos\left(\frac{3\pi}{4} + x\right) - \cos\left(\frac{3\pi}{4} - x\right) = -\sqrt{2}\sin x$ Answer

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It is known that 
$$\cos A - \cos B = -2\sin\left(\frac{A+B}{2}\right).\sin\left(\frac{A-B}{2}\right)$$
  
 $\therefore L.H.S. = \cos\left(\frac{3\pi}{4} + x\right) - \cos\left(\frac{3\pi}{4} - x\right)$   
 $= -2\sin\left\{\frac{\left(\frac{3\pi}{4} + x\right) + \left(\frac{3\pi}{4} - x\right)}{2}\right\}.sin\left\{\frac{\left(\frac{3\pi}{4} + x\right) - \left(\frac{3\pi}{4} - x\right)}{2}\right\}$   
 $= -2\sin\left(\frac{3\pi}{4}\right)sin x$   
 $= -2sin\left(\pi - \frac{\pi}{4}\right)sin x$   
 $= -2sin\left(\pi - \frac{\pi}{4}\right)sin x$   
 $= -2sin\frac{\pi}{4}sin x$   
 $= -2x \cdot \frac{1}{\sqrt{2}} \times sin x$   
 $= -2x \cdot \frac{1}{\sqrt{2}} \times sin x$   
 $= -\sqrt{2}sin x$   
 $= R.H.S.$   
Question 12:  
Prove that  $\sin^2 6x - \sin^2 4x = \sin 2x \sin 10x$   
Answer  
It is known that  
 $sin A + \sin B = 2sin\left(\frac{A+B}{2}\right)cos\left(\frac{A-B}{2}\right), sin A - sin B = 2cos\left(\frac{A+B}{2}\right)sin\left(\frac{A-B}{2}\right)$   
 $\therefore L.H.S. = sin^{2}6x - sin^{2}4x$   
 $= (sin 6x + sin 4x) (sin 6x - sin 4x)$   
 $= \left[2sin\left(\frac{6x + 4x}{2}\right)cos\left(\frac{6x - 4x}{2}\right)\right]\left[2cos\left(\frac{6x + 4x}{2}\right).sin\left(\frac{6x - 4x}{2}\right)\right]$   
 $= (2 sin 5x cos x) (2 cos 5x sin x)$   
 $= (2 sin 5x cos 5x) (2 sin x cos x)$   
 $= sin 10x sin 2x$ 

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= R.H.S.**Question 13:** Prove that  $\cos^2 2x - \cos^2 6x = \sin 4x \sin 8x$ Answer It is known that  $\cos A + \cos B = 2\cos\left(\frac{A+B}{2}\right)\cos\left(\frac{A-B}{2}\right), \ \cos A - \cos B = -2\sin\left(\frac{A+B}{2}\right)\sin\left(\frac{A-B}{2}\right)$  $\therefore L.H.S. = \cos^2 2x - \cos^2 6x$  $= (\cos 2x + \cos 6x) (\cos 2x - 6x)$  $= \left[2\cos\left(\frac{2x+6x}{2}\right)\cos\left(\frac{2x-6x}{2}\right)\right] \left[-2\sin\left(\frac{2x+6x}{2}\right)\sin\left(\frac{2x-6x}{2}\right)\right]$  $= \left\lceil 2\cos 4x \cos(-2x) \right\rceil \left\lceil -2\sin 4x \sin(-2x) \right\rceil$ =  $[2 \cos 4x \cos 2x] [-2 \sin 4x (-\sin 2x)]$  $= (2 \sin 4x \cos 4x) (2 \sin 2x \cos 2x)$  $= \sin 8x \sin 4x$ = R.H.S. **Question 14:** Prove that  $\sin 2x + 2\sin 4x + \sin 6x = 4\cos^2 x \sin 4x$ Answer L.H.S. =  $\sin 2x + 2 \sin 4x + \sin 6x$  $= [\sin 2x + \sin 6x] + 2 \sin 4x$ [(2x+6x)(2x-6x)]

$$= \left[ 2\sin\left(\frac{A+B}{2}\right) \left(\frac{A+B}{2}\right) \right] + 2\sin 4x$$

$$\left[ \because \sin A + \sin B = 2\sin\left(\frac{A+B}{2}\right) \cos\left(\frac{A-B}{2}\right) \right]$$

$$= 2\sin 4x \cos(-2x) + 2\sin 4x$$

$$= 2\sin 4x \cos 2x + 2\sin 4x$$

$$= 2\sin 4x (\cos 2x + 1)$$

$$= 2\sin 4x (2\cos^2 x - 1 + 1)$$

$$= 2 \sin 4x (2 \cos^2 x)$$

 $= 4\cos^2 x \sin 4x$ = R.H.S. **Ouestion 15:** Prove that  $\cot 4x (\sin 5x + \sin 3x) = \cot x (\sin 5x - \sin 3x)$ Answer  $L.H.S = \cot 4x (\sin 5x + \sin 3x)$  $=\frac{\cot 4x}{\sin 4x}\left[2\sin\left(\frac{5x+3x}{2}\right)\cos\left(\frac{5x-3x}{2}\right)\right]$  $\because \sin A + \sin B = 2\sin\left(\frac{A+B}{2}\right)\cos\left(\frac{A-B}{2}\right)$  $=\left(\frac{\cos 4x}{\sin 4x}\right)\left[2\sin 4x\cos x\right]$  $= 2 \cos 4x \cos x$ R.H.S. =  $\cot x (\sin 5x - \sin 3x)$  $=\frac{\cos x}{\sin x}\left[2\cos\left(\frac{5x+3x}{2}\right)\sin\left(\frac{5x-3x}{2}\right)\right]$  $\left[ \because \sin A - \sin B = 2 \cos \left( \frac{A + B}{2} \right) \sin \left( \frac{A - B}{2} \right) \right]$  $=\frac{\cos x}{\sin x}[2\cos 4x\sin x]$  $= 2 \cos 4x \cos x$ L.H.S. = R.H.S.**Question 16:** 

Prove that  $\frac{\cos 9x - \cos 5x}{\sin 17x - \sin 3x} = -\frac{\sin 2x}{\cos 10x}$ Answer It is known that

$$\cos A - \cos B = -2\sin\left(\frac{A+B}{2}\right)\sin\left(\frac{A-B}{2}\right), \ \sin A - \sin B = 2\cos\left(\frac{A+B}{2}\right)\sin\left(\frac{A-B}{2}\right)$$

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$$= \frac{\frac{\cos 9x - \cos 5x}{\sin 17x - \sin 3x}}{2 \cos \left(\frac{9x + 5x}{2}\right) \cdot \sin \left(\frac{9x - 5x}{2}\right)}$$
$$= \frac{-2 \sin \left(\frac{9x + 5x}{2}\right) \cdot \sin \left(\frac{9x - 5x}{2}\right)}{2 \cos \left(\frac{17x + 3x}{2}\right) \cdot \sin \left(\frac{17x - 3x}{2}\right)}$$
$$= \frac{-2 \sin 7x \cdot \sin 2x}{2 \cos 10x \cdot \sin 7x}$$
$$= -\frac{\sin 2x}{\cos 10x}$$
$$= \text{R.H.S.}$$

**Question 17:** 

Prove that  $\frac{\sin 5x + \sin 3x}{\cos 5x + \cos 3x} = \tan 4x$ 

Answer

It is known that

$$\sin A + \sin B = 2\sin\left(\frac{A+B}{2}\right)\cos\left(\frac{A-B}{2}\right), \ \cos A + \cos B = 2\cos\left(\frac{A+B}{2}\right)\cos\left(\frac{A-B}{2}\right)$$

 $\frac{\sin 5x + \sin 3x}{\cos 5x + \cos 3x}$ 

$$\therefore L.H.S. = \cos 3x + \cos 3x$$

$$=\frac{2\sin\left(\frac{5x+3x}{2}\right).\cos\left(\frac{5x-3x}{2}\right)}{2\cos\left(\frac{5x+3x}{2}\right).\cos\left(\frac{5x-3x}{2}\right)}$$
$$=\frac{2\sin 4x.\cos x}{2\cos 4x.\cos x}$$
$$=\frac{\sin 4x}{\cos 4x}$$

 $= \tan 4x = R.H.S.$ 

**Question 18:** 

Prove that 
$$\frac{\frac{\sin x - \sin y}{\cos x + \cos y} = \tan \frac{x - y}{2}}{2}$$

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#### Answer

It is known that

$$\sin A - \sin B = 2 \cos \left(\frac{A+B}{2}\right) \sin \left(\frac{A-B}{2}\right), \quad \cos A + \cos B = 2 \cos \left(\frac{A+B}{2}\right) \cos \left(\frac{A-B}{2}\right)$$
  
$$\therefore L.H.S. = \frac{\sin x - \sin y}{\cos x + \cos y}$$
$$= \frac{2 \cos \left(\frac{x+y}{2}\right) \cdot \sin \left(\frac{x-y}{2}\right)}{2 \cos \left(\frac{x+y}{2}\right) \cdot \cos \left(\frac{x-y}{2}\right)}$$
$$= \frac{\sin \left(\frac{x-y}{2}\right)}{\cos \left(\frac{x-y}{2}\right)}$$
$$= \tan \left(\frac{x-y}{2}\right) = R.H.S.$$

**Question 19:** 

Prove that  $\frac{\sin x + \sin 3x}{\cos x + \cos 3x} = \tan 2x$ 

Answer

It is known that

$$\sin A + \sin B = 2\sin\left(\frac{A+B}{2}\right)\cos\left(\frac{A-B}{2}\right), \ \cos A + \cos B = 2\cos\left(\frac{A+B}{2}\right)\cos\left(\frac{A-B}{2}\right)$$
$$\therefore L.H.S. = \frac{\sin x + \sin 3x}{\cos x + \cos 3x}$$

$$= \frac{2\sin\left(\frac{x+3x}{2}\right)\cos\left(\frac{x-3x}{2}\right)}{2\cos\left(\frac{x+3x}{2}\right)\cos\left(\frac{x-3x}{2}\right)}$$
$$= \frac{\sin 2x}{\cos 2x}$$
$$= \tan 2x$$
$$= R.H.S$$

Question 20:

Prove that  $\frac{\sin x - \sin 3x}{\sin^2 x - \cos^2 x} = 2\sin x$ 

Answer

It is known that

$$\sin A - \sin B = 2 \cos \left(\frac{A+B}{2}\right) \sin \left(\frac{A-B}{2}\right), \ \cos^2 A - \sin^2 A = \cos 2A$$
$$\sin x - \sin 3x$$

$$\therefore \text{L.H.S.} = \frac{1}{\sin^2 x - \cos^2 x}$$
$$= \frac{2\cos\left(\frac{x+3x}{2}\right)\sin\left(\frac{x-3x}{2}\right)}{-\cos 2x}$$
$$= \frac{2\cos 2x\sin(-x)}{-\cos 2x}$$
$$= -2 \times (-\sin x)$$

 $= 2 \sin x = R.H.S.$ 

**Question 21:** 

Prove that  $\frac{\cos 4x + \cos 3x + \cos 2x}{\sin 4x + \sin 3x + \sin 2x} = \cot 3x$ 

Answer

L.H.S. =  $\frac{\cos 4x + \cos 3x + \cos 2x}{\sin 4x + \sin 3x + \sin 2x}$ 

$$=\frac{2\cos\left(\frac{4x+2x}{2}\right)\cos\left(\frac{4x-2x}{2}\right)+\cos 3x}{2\sin\left(\frac{4x+2x}{2}\right)\cos\left(\frac{4x-2x}{2}\right)+\sin 3x}$$
  
$$\left[\because\cos A + \cos B = 2\cos\left(\frac{A+B}{2}\right)\cos\left(\frac{A-B}{2}\right), \quad \sin A + \sin B = 2\sin\left(\frac{A+B}{2}\right)\cos\left(\frac{A-B}{2}\right)\right]$$
  
$$=\frac{2\cos 3x\cos x + \cos 3x}{2\sin 3x\cos x + \sin 3x}$$
  
$$=\frac{\cos 3x(2\cos x + 1)}{\cos x + \sin 3x}$$

$$\sin 3x(2\cos x+1)$$

 $=\frac{(\cos 4x + \cos 2x) + \cos 3x}{(\sin 4x + \sin 2x) + \sin 3x}$ 

$$= \cot 3x = R.H.S.$$

**Question 22:** 

Prove that  $\cot x \cot 2x - \cot 2x \cot 3x - \cot 3x \cot x = 1$ 

Answer

 $L.H.S. = \cot x \cot 2x - \cot 2x \cot 3x - \cot 3x \cot x$ 

 $= \cot x \cot 2x - \cot 3x (\cot 2x + \cot x)$ 

 $= \cot x \cot 2x - \cot (2x + x) (\cot 2x + \cot x)$ 

$$= \cot x \cot 2x - \left[\frac{\cot 2x \cot x - 1}{\cot x + \cot 2x}\right] (\cot 2x + \cot x)$$
$$\left[\because \cot (A + B) = \frac{\cot A \cot B - 1}{\cot A + \cot B}\right]$$
$$= \cot x \cot 2x - (\cot 2x \cot x - 1)$$

= 1 = R.H.S.

**Question 23:** 

Prove that 
$$\tan 4x = \frac{4\tan x \left(1 - \tan^2 x\right)}{1 - 6\tan^2 x + \tan^4 x}$$
  
Answer

$$\tan 2A = \frac{2 \tan A}{1 - \tan^2 A}$$
 It is known that

 $\therefore$ L.H.S. = tan 4x = tan 2(2x) 2 tan 2 x  $1 - \tan^2(2x)$  $2\left(\frac{2\tan x}{2}\right)$  $1 - \tan^2 x$ \_ 2 tan x 1 - $1 - \tan^2 x$ 4 tan x  $1 - \tan^2 x$ =  $1 - \frac{4 \tan^2 x}{2}$  $(1 - \tan^2 x)^2$  $\left(\frac{4\tan x}{1-\tan^2 x}\right)$  $(1-\tan^2 x)^2 - 4\tan^2 x$  $(1-\tan^2 x)^2$ =  $\frac{4 \tan x \left(1 - \tan^2 x\right)}{4 \tan^2 x}$  $\overline{\left(1-\tan^2 x\right)^2-4\tan^2 x}$  $4 \tan x \left(1 - \tan^2 x\right)$  $=\frac{1}{1+\tan^4 x - 2\tan^2 x - 4\tan^2 x}$  $=\frac{4\tan x(1-\tan^2 x)}{1-6\tan^2 x+\tan^4 x}=R.H.S.$ 

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Question 24:
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Prove that  $\cos 4x = 1 - 8\sin^2 x \cos^2 x$ Answer L.H.S. =  $\cos 4x$ =  $\cos 2(2x)$ =  $1 - 2\sin^2 2x [\cos 2A = 1 - 2\sin^2 A]$ =  $1 - 2(2\sin x \cos x)^2 [\sin 2A = 2\sin A \cos A]$ =  $1 - 8\sin^2 x \cos^2 x$ = R.H.S.

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Question 25:
Prove that: \cos 6x = 32 \cos^6 x - 48 \cos^4 x + 18 \cos^2 x - 1
Answer
L.H.S. = \cos 6x
= \cos 3(2x)
= 4 \cos^3 2x - 3 \cos 2x [\cos 3A = 4 \cos^3 A - 3 \cos A]
= 4 \left[ (2 \cos^2 x - 1)^3 - 3 (2 \cos^2 x - 1) \left[ \cos 2x = 2 \cos^2 x - 1 \right] \right]
= 4 \left[ (2 \cos^2 x)^3 - (1)^3 - 3 (2 \cos^2 x)^2 + 3 (2 \cos^2 x) \right] - 6 \cos^2 x + 3
= 4 [8\cos^{6}x - 1 - 12\cos^{4}x + 6\cos^{2}x] - 6\cos^{2}x + 3
= 32 \cos^{6} x - 4 - 48 \cos^{4} x + 24 \cos^{2} x - 6 \cos^{2} x + 3
= 32\cos^6 x - 48\cos^4 x + 18\cos^2 x - 1
= R.H.S.
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