### **∛S**aral

### Class XII : Maths Chapter 12 : Linear Programming

Questions and Solutions | Exercise 12.1 - NCERT Books

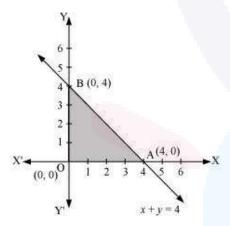
**Question 1:** 

Maximise Z = 3x + 4y

Subject to the constraints:  $x + y \le 4, x \ge 0, y \ge 0$ .

Answer

The feasible region determined by the constraints,  $x + y \le 4$ ,  $x \ge 0$ ,  $y \ge 0$ , is as follows.



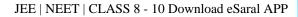
The corner points of the feasible region are O (0, 0), A (4, 0), and B (0, 4). The values of Z at these points are as follows.

Corner point	Z = 3x + 4y	
O(0, 0)	0	
A(4, 0)	12	
B(0, 4)	16	$\rightarrow$ Maximum

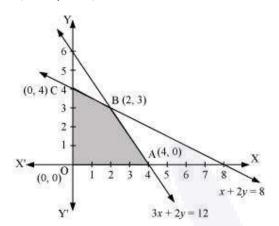
Therefore, the maximum value of Z is 16 at the point B (0, 4).

**Question 2:** 

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Minimise Z = -3x + 4y
subject to x+2y \le 8, 3x+2y \le 12, x \ge 0, y \ge 0.
Answer
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The feasible region determined by the system of constraints,  $x + 2y \le 8$ ,  $3x + 2y \le 12$ ,  $x \ge 0$ , and  $y \ge 0$ , is as follows.



The corner points of the feasible region are O (0, 0), A (4, 0), B (2, 3), and C (0, 4). The values of Z at these corner points are as follows.

Corner point	Z = -3x + 4y	
0(0, 0)	0	
A(4, 0)	-12	$\rightarrow$ Minimum
B(2, 3)	6	
C(0, 4)	16	

Therefore, the minimum value of Z is -12 at the point (4, 0).

#### **Question 3:**

Maximise Z = 5x + 3y

subject to  $3x + 5y \le 15$ ,  $5x + 2y \le 10$ ,  $x \ge 0$ ,  $y \ge 0$ .

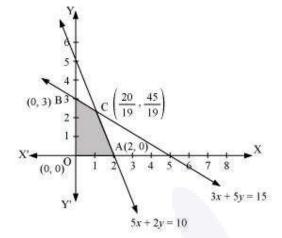
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The feasible region determined by the system of constraints,  $3x + 5y \le 15$ ,  $5x + 2y \le 10$ ,  $x \ge 0$ , and  $y \ge 0$ , are as follows.

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 $C\left(\frac{20}{19},\frac{45}{19}\right)$ The corner points of the feasible region are O(0, 0), A(2, 0), B(0, 3), and The values of Z at these corner points are as follows.

Corner point	Z = 5x + 3y	
0(0, 0)	0	
A(2, 0)	10	
B(0, 3)	9	
$C\left(\frac{20}{19},\frac{45}{19}\right)$	$\frac{235}{19}$	→ Maximum
Therefore, the	maximum value	e of Z is $\frac{235}{19}$ at

**Question 4:** 

Minimise Z = 3x + 5y

such that  $x + 3y \ge 3$ ,  $x + y \ge 2$ ,  $x, y \ge 0$ .

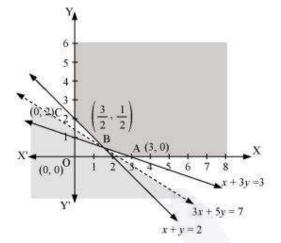
Answer

The feasible region determined by the system of constraints,  $x+3y \ge 3, x+y \ge 2$ , and x,  $y \ge 0$ , is as follows.

 $\frac{20}{19}, \frac{45}{19}$ 

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It can be seen that the feasible region is unbounded.

The corner points of the feasible region are A (3, 0),  $B\left(\frac{3}{2}, \frac{1}{2}\right)$ , and C (0, 2). The values of Z at these corner points are as follows.

Corner point	Z = 3x + 5y	
A(3, 0)	9	
$B\left(\frac{3}{2},\frac{1}{2}\right)$	7	$\rightarrow$ Smallest
C(0, 2)	10	

As the feasible region is unbounded, therefore, 7 may or may not be the minimum value of Z.

For this, we draw the graph of the inequality, 3x + 5y < 7, and check whether the resulting half plane has points in common with the feasible region or not.

It can be seen that the feasible region has no common point with 3x + 5y < 7 Therefore,

the minimum value of Z is 7 at 
$$\left(\frac{3}{2}, \frac{1}{2}\right)$$

Question 5:

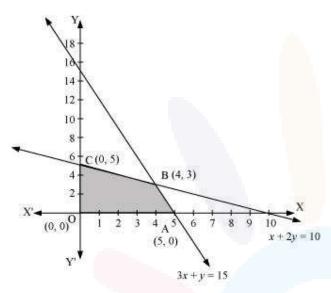
Maximise Z = 3x + 2y

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subject to  $x + 2y \le 10, 3x + y \le 15, x, y \ge 0$ .

#### Answer

The feasible region determined by the constraints,  $x + 2y \le 10$ ,  $3x + y \le 15$ ,  $x \ge 0$ , and  $y \ge 0$ , is as follows.



The corner points of the feasible region are A (5, 0), B (4, 3), and C (0, 5). The values of Z at these corner points are as follows.

Corner point	Z = 3x + 2y	
A(5, 0)	15	
B(4, 3)	18	$\rightarrow$ Maximum
C(0, 5)	10	

Therefore, the maximum value of Z is 18 at the point (4, 3).

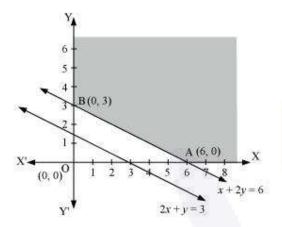
**Question 6:** 

Minimise Z = x + 2y

subject to  $2x + y \ge 3$ ,  $x + 2y \ge 6$ ,  $x, y \ge 0$ . Answer



The feasible region determined by the constraints,  $2x + y \ge 3$ ,  $x + 2y \ge 6$ ,  $x \ge 0$ , and  $y \ge 0$ , is as follows.



The corner points of the feasible region are A (6, 0) and B (0, 3). The values of Z at these corner points are as follows.

Corner point	Z=x+2y
A(6, 0)	6
B(0, 3)	6

It can be seen that the value of Z at points A and B is same. If we take any other point such as (2, 2) on line x + 2y = 6, then Z = 6

Thus, the minimum value of Z occurs for more than 2 points.

Therefore, the value of Z is minimum at every point on the line, x + 2y = 6

#### **Question 7:**

Minimise and Maximise Z = 5x + 10y

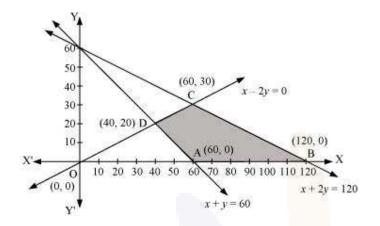
subject to  $x + 2y \le 120, x + y \ge 60, x - 2y \ge 0, x, y \ge 0$ .

Answer

The feasible region determined by the constraints,  $x + 2y \le 120$ ,  $x + y \ge 60$ ,  $x - 2y \ge 0$ ,  $x \ge 0$ , and  $y \ge 0$ , is as follows.

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The corner points of the feasible region are A (60, 0), B (120, 0), C (60, 30), and D (40, 20).

Corner point	Z = 5x + 10y	
A(60, 0)	300	→ Minimum
B(120, 0)	600	$\rightarrow$ Maximum
C(60, 30)	600	$\rightarrow$ Maximum
D(40, 20)	400	

The values of Z at these corner points are as follows.

The minimum value of Z is 300 at (60, 0) and the maximum value of Z is 600 at all the points on the line segment joining (120, 0) and (60, 30).

#### **Question 8:**

Minimise and Maximise Z = x + 2y

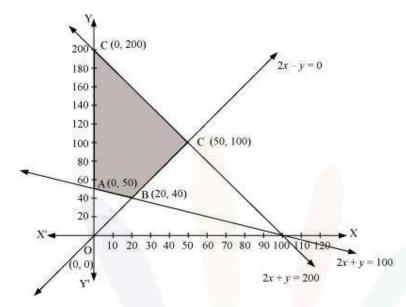
subject to  $x + 2y \ge 100$ ,  $2x - y \le 0$ ,  $2x + y \le 200$ ;  $x, y \ge 0$ .

Answer

The feasible region determined by the constraints,  $x + 2y \ge 100$ ,  $2x - y \le 0$ ,  $2x + y \le 200$ ,  $x \ge 0$ , and  $y \ge 0$ , is as follows.

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The corner points of the feasible region are A(0, 50), B(20, 40), C(50, 100), and D(0, 200).

The values of Z at these corner points are as follows.

Corner point	Z = x + 2y	
A(0, 50)	100	→ Minimum
B(20, 40)	100	→ Minimum
C(50, 100)	250	
D(0, 200)	400	→ Maximum

The maximum value of Z is 400 at (0, 200) and the minimum value of Z is 100 at all the points on the line segment joining the points (0, 50) and (20, 40).

#### **Question 9:**

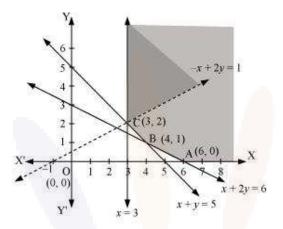
Maximise Z = -x + 2y, subject to the constraints:  $x \ge 3$ ,  $x + y \ge 5$ ,  $x + 2y \ge 6$ ,  $y \ge 0$ 

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The feasible region determined by the constraints,  $x \ge 3$ ,  $x + y \ge 5$ ,  $x + 2y \ge 6$ , and  $y \ge 0$ , is as follows.



It can be seen that the feasible region is unbounded.

The values of Z at corner points A (6, 0), B (4, 1), and C (3, 2) are as follows.

Corner point	Z = -x + 2y
A(6, 0)	Z = - 6
B(4, 1)	Z = - 2
C(3, 2)	Z = 1

As the feasible region is unbounded, therefore, Z = 1 may or may not be the maximum value.

For this, we graph the inequality, -x + 2y > 1, and check whether the resulting half plane has points in common with the feasible region or not.

The resulting feasible region has points in common with the feasible region.

Therefore, Z = 1 is not the maximum value. Z has no maximum value.

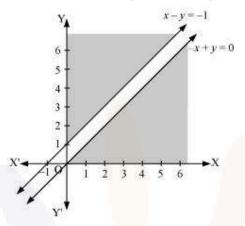
**Question 10:** 

Maximise Z = x + y, subject to  $x - y \le -1$ ,  $-x + y \le 0$ ,  $x, y \ge 0$ . Answer

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The region determined by the constraints,  $x - y \le -1$ ,  $-x + y \le 0$ ,  $x, y \ge 0$ , is as follows.



There is no feasible region and thus, Z has no maximum value.