



Class XII : Physics
Chapter 11 : Dual Nature Of Radiation And Matter

Questions and Solutions | Exercises - NCERT Books

Question 1:

Find the

maximum frequency, and

minimum wavelength of X-rays produced by 30 kV electrons.

Answer

Potential of the electrons, $V = 30 \text{ kV} = 3 \times 10^4 \text{ V}$

Hence, energy of the electrons, $E = 3 \times 10^4 \text{ eV}$

Where,

$e =$ Charge on an electron $= 1.6 \times 10^{-19} \text{ C}$

(a) Maximum frequency produced by the X-rays $= \nu$

The energy of the electrons is given by the relation:

$$E = h\nu$$

Where,

$h =$ Planck's constant $= 6.626 \times 10^{-34} \text{ Js}$

$$\therefore \nu = \frac{E}{h}$$

$$= \frac{1.6 \times 10^{-19} \times 3 \times 10^4}{6.626 \times 10^{-34}} = 7.24 \times 10^{18} \text{ Hz}$$

Hence, the maximum frequency of X-rays produced is $7.24 \times 10^{18} \text{ Hz}$.

(b) The minimum wavelength produced by the X-rays is given as:



$$\lambda = \frac{c}{\nu}$$
$$= \frac{3 \times 10^8}{7.24 \times 10^{18}} = 4.14 \times 10^{-11} \text{ m} = 0.0414 \text{ nm}$$

Hence, the minimum wavelength of X-rays produced is 0.0414 nm.

Question 2:

The work function of caesium metal is 2.14 eV. When light of frequency 6×10^{14} Hz is incident on the metal surface, photoemission of electrons occurs. What is the

maximum kinetic energy of the emitted electrons,

Stopping potential, and

maximum speed of the emitted photoelectrons?

Answer

Work function of caesium metal, $\phi_0 = 2.14 \text{ eV}$

Frequency of light, $\nu = 6.0 \times 10^{14} \text{ Hz}$

(a) The maximum kinetic energy is given by the photoelectric effect as:

$$K = h\nu - \phi_0$$

Where,

$h = \text{Planck's constant} = 6.626 \times 10^{-34} \text{ Js}$

$$\therefore K = \frac{6.626 \times 10^{-34} \times 6 \times 10^{14}}{1.6 \times 10^{-19}} - 2.14$$

$$= 2.485 - 2.140 = 0.345 \text{ eV}$$



Hence, the maximum kinetic energy of the emitted electrons is 0.345 eV.

(b) For stopping potential V_0 , we can write the equation for kinetic energy as:

$$K = eV_0$$

$$\therefore V_0 = \frac{K}{e}$$

$$= \frac{0.345 \times 1.6 \times 10^{-19}}{1.6 \times 10^{-19}} = 0.345 \text{ V}$$

Hence, the stopping potential of the material is 0.345 V.

(c) Maximum speed of the emitted photoelectrons = v

Hence, the relation for kinetic energy can be written as:

$$K = \frac{1}{2}mv^2$$

Where,

m = Mass of an electron = 9.1×10^{-31} kg

$$v^2 = \frac{2K}{m}$$

$$= \frac{2 \times 0.345 \times 1.6 \times 10^{-19}}{9.1 \times 10^{-31}} = 0.1104 \times 10^{12}$$

$$\therefore v = 3.323 \times 10^5 \text{ m/s} = 332.3 \text{ km/s}$$

Hence, the maximum speed of the emitted photoelectrons is 332.3 km/s.

Question 3:

The photoelectric cut-off voltage in a certain experiment is 1.5 V. What is the maximum kinetic energy of photoelectrons emitted?

Answer



Photoelectric cut-off voltage, $V_0 = 1.5 \text{ V}$

The maximum kinetic energy of the emitted photoelectrons is given as:

$$K_e = eV_0$$

Where,

$e =$ Charge on an electron $= 1.6 \times 10^{-19} \text{ C}$

$$\begin{aligned}\therefore K_e &= 1.6 \times 10^{-19} \times 1.5 \\ &= 2.4 \times 10^{-19} \text{ J}\end{aligned}$$

Therefore, the maximum kinetic energy of the photoelectrons emitted in the given experiment is $2.4 \times 10^{-19} \text{ J}$.

Question 4:

Monochromatic light of wavelength 632.8 nm is produced by a helium-neon laser. The power emitted is 9.42 mW .

Find the energy and momentum of each photon in the light beam,

How many photons per second, on the average, arrive at a target irradiated by this beam? (Assume the beam to have uniform cross-section which is less than the target area), and

How fast does a hydrogen atom have to travel in order to have the same momentum as that of the photon?

Answer

Wavelength of the monochromatic light, $\lambda = 632.8 \text{ nm} = 632.8 \times 10^{-9} \text{ m}$

Power emitted by the laser, $P = 9.42 \text{ mW} = 9.42 \times 10^{-3} \text{ W}$



Planck's constant, $h = 6.626 \times 10^{-34}$ Js

Speed of light, $c = 3 \times 10^8$ m/s

Mass of a hydrogen atom, $m = 1.66 \times 10^{-27}$ kg

(a) The energy of each photon is given as:

$$E = \frac{hc}{\lambda}$$
$$= \frac{6.626 \times 10^{-34} \times 3 \times 10^8}{632.8 \times 10^{-9}} = 3.141 \times 10^{-19} \text{ J}$$

The momentum of each photon is given as:

$$P = \frac{h}{\lambda}$$
$$= \frac{6.626 \times 10^{-34}}{632.8} = 1.047 \times 10^{-27} \text{ kg m s}^{-1}$$

(b) Number of photons arriving per second, at a target irradiated by the beam = n

Assume that the beam has a uniform cross-section that is less than the target area.

Hence, the equation for power can be written as:

$$P = nE$$
$$\therefore n = \frac{P}{E}$$
$$= \frac{9.42 \times 10^{-3}}{3.141 \times 10^{-19}} \approx 3 \times 10^{16} \text{ photon/s}$$

(c) Momentum of the hydrogen atom is the same as the momentum of the photon,

$$p = 1.047 \times 10^{-27} \text{ kg m s}^{-1}$$

Momentum is given as:

$$p = mv$$

Where,

v = Speed of the hydrogen atom



$$\therefore v = \frac{p}{m}$$

$$= \frac{1.047 \times 10^{-27}}{1.66 \times 10^{-27}} = 0.621 \text{ m/s}$$

Question 5:

In an experiment on photoelectric effect, the slope of the cut-off voltage versus frequency of incident light is found to be $4.12 \times 10^{-15} \text{ V s}$. Calculate the value of Planck's constant.

Answer

The slope of the cut-off voltage (V) versus frequency (ν) of an incident light is given as:

$$\frac{V}{\nu} = 4.12 \times 10^{-15} \text{ Vs}$$

V is related to frequency by the equation:

$$h\nu = eV$$

Where,

$$e = \text{Charge on an electron} = 1.6 \times 10^{-19} \text{ C}$$

h = Planck's constant

$$\therefore h = e \times \frac{V}{\nu}$$

$$= 1.6 \times 10^{-19} \times 4.12 \times 10^{-15} = 6.592 \times 10^{-34} \text{ Js}$$

Therefore, the value of Planck's constant is $6.592 \times 10^{-34} \text{ Js}$.



Question 6:

The threshold frequency for a certain metal is 3.3×10^{14} Hz. If light of frequency 8.2×10^{14} Hz is incident on the metal, predict the cutoff voltage for the photoelectric emission.

Answer

Threshold frequency of the metal, $\nu_0 = 3.3 \times 10^{14}$ Hz

Frequency of light incident on the metal, $\nu = 8.2 \times 10^{14}$ Hz

Charge on an electron, $e = 1.6 \times 10^{-19}$ C

Planck's constant, $h = 6.626 \times 10^{-34}$ Js

Cut-off voltage for the photoelectric emission from the metal = V_0

The equation for the cut-off energy is given as:

$$eV_0 = h(\nu - \nu_0)$$

$$V_0 = \frac{h(\nu - \nu_0)}{e}$$

$$= \frac{6.626 \times 10^{-34} \times (8.2 \times 10^{14} - 3.3 \times 10^{14})}{1.6 \times 10^{-19}} = 2.0292 \text{ V}$$

Therefore, the cut-off voltage for the photoelectric emission is 2.0292 V.

Question 7:

The work function for a certain metal is 4.2 eV. Will this metal give photoelectric emission for incident radiation of wavelength 330 nm?

Answer



No

Work function of the metal, $\phi_0 = 4.2 \text{ eV}$

Charge on an electron, $e = 1.6 \times 10^{-19} \text{ C}$

Planck's constant, $h = 6.626 \times 10^{-34} \text{ Js}$

Wavelength of the incident radiation, $\lambda = 330 \text{ nm} = 330 \times 10^{-9} \text{ m}$

Speed of light, $c = 3 \times 10^8 \text{ m/s}$

The energy of the incident photon is given as:

$$\begin{aligned} E &= \frac{hc}{\lambda} \\ &= \frac{6.626 \times 10^{-34} \times 3 \times 10^8}{330 \times 10^{-9}} = 6.0 \times 10^{-19} \text{ J} \\ &= \frac{6.0 \times 10^{-19}}{1.6 \times 10^{-19}} = 3.76 \text{ eV} \end{aligned}$$

It can be observed that the energy of the incident radiation is less than the work function of the metal. Hence, no photoelectric emission will take place.

Question 8:

Light of frequency $7.21 \times 10^{14} \text{ Hz}$ is incident on a metal surface. Electrons with a maximum speed of $6.0 \times 10^5 \text{ m/s}$ are ejected from the surface. What is the threshold frequency for photoemission of electrons?

Answer

Frequency of the incident photon, $\nu = 488 \text{ nm} = 488 \times 10^{-9} \text{ m}$

Maximum speed of the electrons, $v = 6.0 \times 10^5 \text{ m/s}$



Planck's constant, $h = 6.626 \times 10^{-34}$ Js

Mass of an electron, $m = 9.1 \times 10^{-31}$ kg

For threshold frequency ν_0 , the relation for kinetic energy is written as:

$$\begin{aligned}\frac{1}{2}mv^2 &= h(\nu - \nu_0) \\ \nu_0 &= \nu - \frac{mv^2}{2h} \\ &= 7.21 \times 10^{14} - \frac{(9.1 \times 10^{-31}) \times (6 \times 10^5)^2}{2 \times (6.626 \times 10^{-34})} \\ &= 7.21 \times 10^{14} - 2.472 \times 10^{14} \\ &= 4.738 \times 10^{14} \text{ Hz}\end{aligned}$$

Therefore, the threshold frequency for the photoemission of electrons is 4.738×10^{14} Hz.

Question 9:

Light of wavelength 488 nm is produced by an argon laser which is used in the photoelectric effect. When light from this spectral line is incident on the emitter, the stopping (cut-off) potential of photoelectrons is 0.38 V. Find the work function of the material from which the emitter is made.

Answer

Wavelength of light produced by the argon laser, $\lambda = 488$ nm

$$= 488 \times 10^{-9} \text{ m}$$

Stopping potential of the photoelectrons, $V_0 = 0.38$ V

$$1\text{eV} = 1.6 \times 10^{-19} \text{ J}$$

$$\therefore V_0 = \frac{0.38}{1.6 \times 10^{-19}} \text{ eV}$$

Planck's constant, $h = 6.6 \times 10^{-34}$ Js



Charge on an electron, $e = 1.6 \times 10^{-19}$ C

Speed of light, $c = 3 \times 10^8$ m/s

From Einstein's photoelectric effect, we have the relation involving the work function ϕ_0 of the material of the emitter as:

$$eV_0 = \frac{hc}{\lambda} - \phi_0$$

$$\phi_0 = \frac{hc}{\lambda} - eV_0$$

$$= \frac{6.6 \times 10^{-34} \times 3 \times 10^8}{1.6 \times 10^{-19} \times 488 \times 10^{-9}} - \frac{1.6 \times 10^{-19} \times 0.38}{1.6 \times 10^{-19}}$$

$$= 2.54 - 0.38 = 2.16 \text{ eV}$$

Therefore, the material with which the emitter is made has the work function of 2.16 eV.



Question 10:

What is the de Broglie wavelength of

a bullet of mass 0.040 kg travelling at the speed of 1.0 km/s,

a ball of mass 0.060 kg moving at a speed of 1.0 m/s, and

a dust particle of mass 1.0×10^{-9} kg drifting with a speed of 2.2 m/s?

Answer

(a) Mass of the bullet, $m = 0.040$ kg

Speed of the bullet, $v = 1.0$ km/s = 1000 m/s

Planck's constant, $h = 6.6 \times 10^{-34}$ Js

De Broglie wavelength of the bullet is given by the relation:

$$\begin{aligned}\lambda &= \frac{h}{mv} \\ &= \frac{6.6 \times 10^{-34}}{0.040 \times 1000} = 1.65 \times 10^{-35} \text{ m}\end{aligned}$$

Mass of the ball, $m = 0.060$ kg

Speed of the ball, $v = 1.0$ m/s

De Broglie wavelength of the ball is given by the relation:

$$\begin{aligned}\lambda &= \frac{h}{mv} \\ &= \frac{6.6 \times 10^{-34}}{0.060 \times 1} = 1.1 \times 10^{-32} \text{ m}\end{aligned}$$

(c) Mass of the dust particle, $m = 1 \times 10^{-9}$ kg

Speed of the dust particle, $v = 2.2$ m/s

De Broglie wavelength of the dust particle is given by the relation:

$$\lambda = \frac{h}{mv} = \frac{6.6 \times 10^{-34}}{2.2 \times 1 \times 10^{-9}} = 3.0 \times 10^{-25} \text{ m}$$



Question 11:

Show that the wavelength of electromagnetic radiation is equal to the de Broglie wavelength of its quantum (photon).

Answer

The momentum of a photon having energy ($h\nu$) is given as:

$$p = \frac{h\nu}{c} = \frac{h}{\lambda}$$

$$\lambda = \frac{h}{p} \quad \dots (i)$$

Where,

λ = Wavelength of the electromagnetic radiation

c = Speed of light

h = Planck's constant

De Broglie wavelength of the photon is given as:

$$\lambda = \frac{h}{mv}$$

$$\text{But } p = mv$$

$$\therefore \lambda = \frac{h}{p} \quad \dots (ii)$$

Where,

m = Mass of the photon

v = Velocity of the photon

Hence, it can be inferred from equations (i) and (ii) that the wavelength of the electromagnetic radiation is equal to the de Broglie wavelength of the photon.