FINAL JEE-MAIN EXAMINATION - AUGUST, 2021THAL JEE-MAIN EXAMINATION - AUGUST, 2021THE INPAL JEE-MAIN EXAMINATION - AUGUST, 2021THE INPAL JEE-MAIN EXAMINATION - AUGUST, 2021TIME : 3 : 00 PM to 6 : 00 PMSECTION-AINDE : 3 : 00 PM to 6 : 00 PMSECTION-ASECTION-ASol.
$$\lambda = \frac{h}{mv} = \frac{h}{\sqrt{2mE}}$$
, $mv = \sqrt{2mE}$ INDE : 3 : 00 PM to 6 : 00 PMSECTION-AINDE : 3 : 00 PM to 6 : 00 PMSECTION-AINDE : 3 : 00 PM to 6 : 00 PMSECTION-AINDE : 3 : 00 PM to 6 : 00 PMSECTION-AINDE : 3 : 00 PM to 6 : 00 PMSECTION-AINDE : 3 : 00 PM to 6 : 00 PMINDE : 3 : 00 PM to 6 : 00 PMINDE : 3 : 00 PM to 6 : 00 PMINDE : 3 : 00 PM to 6 : 00 PMINDE : 3 : 00 PM to 6 : 00 PMINDE : 3 : 00 PM to 6 : 00 PMINDE : 3 : 00 PM to 6 : 00 PMINDE : 3 : 00 PM to 6 : 00 PMINDE : 3 : 00 PM to 6 : 00 PMINDE : 3 : 00 PM to 6 : 00 PMINDE : 3 : 00 PM to 6 : 00 PMINDE : 3 : 00 PM to 6 : 00 PMINDE : 3 : 00 PM to 6 : 00 PMINDE : 3 : 00 PM to 6 : 00 PMINDE : 3 : 00 PM to 6 : 00 PMINDE : 3 : 00 PM to 6 : 00 PM

Final JEE-Main Exam August, 2021/26-08-2021/Even

A cylindrical container of volume $4.0 \times 10^{-3} \text{ m}^3$ 4. contains one mole of hydrogen and two moles of carbon dioxide. Assume the temperature of the mixture is 400 K. The pressure of the mixture of gases is :

[Take gas constant as 8.3 J mol⁻¹ K⁻¹]

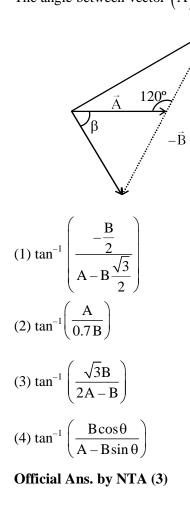
(1) 249×10^1 Pa (2) 24.9×10^3 Pa (3) 24.9×10^5 Pa (4) 24.9 Pa

Official Ans. by NTA (3)

Sol. $V = 4 \times 10^{-3} \text{ m}^3$ n = 3 moles T = 400K $PV = nRT \implies P = \frac{nRT}{V}$ $P = \frac{3 \times 8.3 \times 400}{4 \times 10^{-3}}$ $= 24.9 \times 10^5$ Pa

The angle between vector (\vec{A}) and $(\vec{A} - \vec{B})$ is : 5.

Ans 3



Sol. B 120 (60° **(**60° Angle between \vec{A} and \vec{B} , $\theta = 60^{\circ}$ Angle betwenn \vec{A} and $\vec{A} - \vec{B}$ $\tan \alpha = \frac{B\sin \theta}{A - B\cos \theta}$ $=\frac{B\sqrt{\frac{3}{2}}}{A-B\times\frac{1}{2}2}$ $\tan \alpha = \frac{\sqrt{3}B}{2A - P}$ Ans 3 A light beam is described by $E = 800 \sin \omega \left(t - \frac{x}{c} \right)$.An electron is allowed to move normal to the propagation of light beam with a speed of 3×10^7 ms⁻¹. What is the maximum magnetic force exerted on the electron ? (1) 1.28×10^{-18} N (2) 1.28×10^{-21} N (3) 12.8×10^{-17} N

(4) 12.8×10^{-18} N

Official Ans. by NTA (4)

Sol.
$$\frac{E_0}{C} = B_0$$

 $F_{max} = eB_0 V$
 $= 1.6 \times 10^{-19} \times \frac{800}{3 \times 10^8} \times 3 \times 10^7$
 $= 12.8 \times 10^{-18} N$
Ans. 4

6.

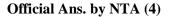
The two thin coaxial rings, each of radius 'a' and having charges +Q and -Q respectively are separated by a distance of 's'. The potential difference between the centres of the two rings is :

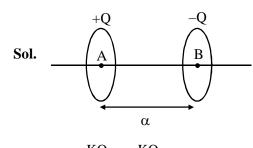
$$(1) \frac{Q}{2\pi\varepsilon_{0}} \left[\frac{1}{a} + \frac{1}{\sqrt{s^{2} + a^{2}}} \right]$$

$$(2) \frac{Q}{4\pi\varepsilon_{0}} \left[\frac{1}{a} + \frac{1}{\sqrt{s^{2} + a^{2}}} \right]$$

$$(3) \frac{Q}{4\pi\varepsilon_{0}} \left[\frac{1}{a} - \frac{1}{\sqrt{s^{2} + a^{2}}} \right]$$

$$(4) \frac{Q}{2\pi\varepsilon_{0}} \left[\frac{1}{a} - \frac{1}{\sqrt{s^{2} + a^{2}}} \right]$$



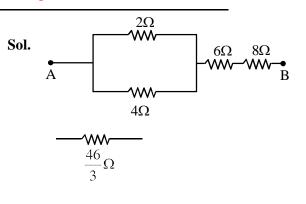


$$V_{A} = \frac{KQ}{a} - \frac{KQ}{\sqrt{a^{2} + s^{2}}}$$
$$V_{B} = \frac{-KQ}{a} + \frac{KQ}{\sqrt{a^{2} + s^{2}}}$$
$$V_{A} - V_{B} = \frac{2KQ}{a} - \frac{2KQ}{\sqrt{a^{2} + s^{2}}}$$
$$= \frac{Q}{2\pi\epsilon_{0}} \left(\frac{1}{a} - \frac{1}{s^{2} + a^{2}}\right)$$

Ans 4

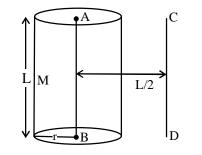
8. If you are provided a set of resistances 2Ω , 4Ω , 6Ω and 8Ω . Connect these resistances so as to obtain an equivalent resistance of $\frac{46}{3}\Omega$.

(1) 4Ω and 6Ω are in parallel with 2Ω and 8 Ω in series
 (2) 6Ω and 8Ω are in parallel with 2Ω and 4Ω in series
 (3) 2Ω and 6Ω are in parallel with 4Ω and 8 Ω in series
 (4) 2Ω and 4Ω are in parallel with 6Ω and 8Ω in series
 Official Ans. by NTA (4)



Ans 4

9. The solid cylinder of length 80 cm and mass M has a radius of 20 cm. Calculate the density of the material used if the moment of inertia of the cylinder about an axis CD parallel to AB as shown in figure is 2.7 kg m².



(1) 14.9 kg / m³
(2)
$$7.5 \times 10^{1}$$
 kg / m³
(3) 7.5×10^{2} kg/m³
(4) 1.49×10^{2} kg / m³

Official Ans. by NTA (4)

Sol. Parallel axis theorem

$$I = I_{CM} + Md^{2}$$

$$I = \frac{Mr^{2}}{2} + M\left(\frac{L}{2}\right)^{2}$$

$$2.7 = M\frac{(0.2)^{2}}{2} + M\left(\frac{0.8}{2}\right)^{2}$$

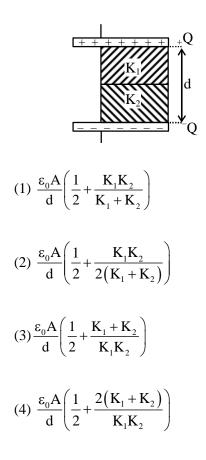
$$2.7 = M\left[\frac{2}{100} + \frac{16}{100}\right]$$

$$M = 15kg$$

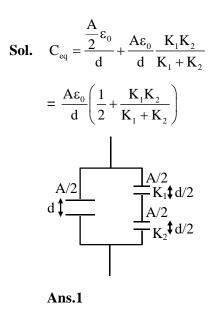
$$\Rightarrow \rho = \frac{M}{\pi r^{2}L} = \frac{15}{\pi (0.2)^{2} \times 0.8}$$

$$= 0.1492 \times 10^{3}$$
Ans. 4

10. A parallel - plate capacitor with plate area A has separation d between the plates. Two dielectric slabs of dielectric constant K₁ and K₂ of same area A/2 and thickness d/2 are inserted in the space between the plates. The capacitance of the capacitor will be given by :

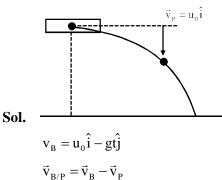


Official Ans. by NTA (1)



- 11. A bomb is dropped by fighter plane flying horizontally. To an observer sitting in the plane, the trajectory of the bomb is a :(1) hyperbola
 - (2) parabola in the direction of motion of plane
 - (3) straight line vertically down the plane

(4) parabola in a direction opposite to the motion of plane Official Ans. by NTA (3)

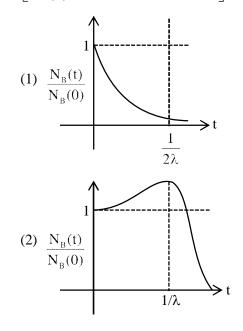


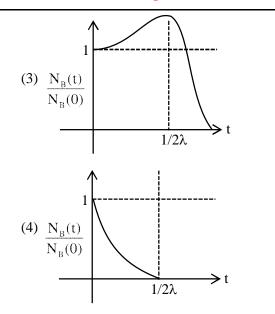
 $\vec{v}_{B/P} = -8t\hat{j}$ straight line vertically down

Ans.3

12. At time t = 0, a material is composed of two radioactive atoms A and B, where $N_A(0) = 2N_B(0)$. The decay constant of both kind of radioactive atoms is λ . However, A disintegrates to B and B disintegrates to C. Which of the following figures represents the evolution of $N_B(t) / N_B(0)$ with respect to time t ?

$$\begin{bmatrix} N_{A}(0) = \text{No. of A atoms at } t = 0 \\ N_{B}(0) = \text{No. of B atoms at } t = 0 \end{bmatrix}$$









$$A \rightarrow B, B \rightarrow C$$

$$\frac{dN_{B}}{dt} = \lambda N_{A} - \lambda N_{B}$$

$$\frac{dN_{B}}{dt} = 2\lambda N_{B_{0}} e^{-\lambda t} - \lambda N_{B}$$

$$e^{-\lambda t} \left(\frac{dN_{B}}{dt} + \lambda N_{B}\right) = 2\lambda N_{B_{0}} e^{-\lambda t} \times e^{\lambda t}$$

$$\frac{d}{dt} \left(N_{B} e^{\lambda t}\right) = 2\lambda N_{B_{0}}, \text{ on integrating}$$

$$N_{B} e^{\lambda t} = 2\lambda t N_{B_{0}} + N_{B_{0}}$$

$$N_{B} = N_{B_{0}} [1 + 2\lambda t] e^{-\lambda t}$$

$$\frac{dN_{B}}{dt} = 0 \text{ at } -\lambda [1 + 2\lambda t] e^{-\lambda t} + 2\lambda e^{-\lambda t} = 0$$

$$N_{B_{max}} \text{ at } t = \frac{1}{2\lambda}$$

13. A transmitting antenna at top of a tower has a height of 50 m and the height of receiving antenna is 80 m. What is range of communication for Line of Sight (LoS) mode ?
[use radius of earth = 6400 km]
(1) 45.5 km
(2) 80.2 km

(3) 144.1 km	(4) 57.28 km

Official Ans. by NTA (4)

Sol.
$$h_{1} \underbrace{\begin{matrix} d_{1} & d_{2} \\ R & h_{2} \\ d_{t} = \sqrt{2Rh_{1}} + \sqrt{2Rh_{2}} \\ = \sqrt{2R} \left(\sqrt{h_{1}} + \sqrt{h_{2}} \right) \\ = (2 \times 6400 \times 10^{3})^{1/2} \left(\sqrt{50} + \sqrt{80} \right) \\ = 3578 (7.07 + 8.94) \\ = 57.28 \text{ Km}$$

14. A refrigerator consumes an average 35 W power to operate between temperature -10°C to 25°C. If there is no loss of energy then how much average heat per second does it transfer ?

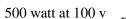
(1) 263 J/s (2) 298 J/s (3) 350 J/s (4) 35 J/s **Official Ans. by NTA (1)**

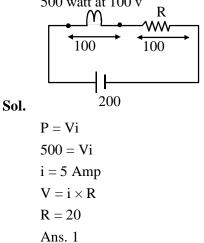
Sol.
$$\frac{T_{L}}{T_{H} - T_{L}} = C.O.P. = \frac{\frac{dH}{dt}}{\frac{dW}{dt}}$$
$$\frac{263}{35} \times 35 = \frac{dH}{dt}$$
$$\frac{dH}{dt} = 263 \text{ watts}$$
Ans.1

15. An electric bulb of 500 watt at 100 volt is used in a circuit having a 200 V supply. Calculate the resistance R to be connected in series with the bulb

so that the power delivered by the bulb is 500 W. (1) 20Ω (2) 30Ω (3) 5Ω (4) 10Ω

Official Ans. by NTA (1)

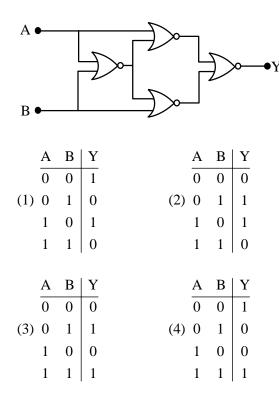




5

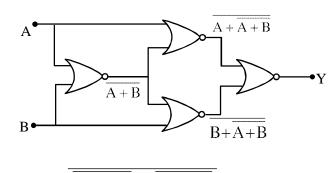
16. Four NOR gates are connected as shown in figure.

The truth table for the given figure is :



Official Ans. by NTA (4)

Sol.



$$y = (A + \overline{A + B}) + (B + \overline{A + B})$$

$$y = (A + \overline{A + B}).(B + \overline{A + B})$$

Α	В	у
0	0	1
0	1	0
1	0	0
1	1	1

Ans.4

17. Match List–I with List–II.

List-I		List-II	
(a)	Magnetic Induction	(i)	$ML^2T^{-2}A^{-1}$
(b)	Magnetic Flux	(ii)	$M^0L^{-1}A$
(c)	Magnetic	(iii)	$\mathbf{M}\mathbf{T}^{-2}\mathbf{A}^{-1}$
	Permeability		
(d)	Magnetization	(iv)	$MLT^{-2}A^{-2}$

Choose the most appropriate answer from the options given below :

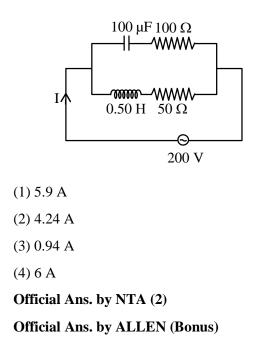
- (1) (a)-(ii), (b)-(iv), (c)-(i), (d)-(iii)
- (2) (a)-(ii), (b)-(i), (c)-(iv), (d)-(iii)
- (3) (a)-(iii), (b)-(ii), (c)-(iv), (d)-(i)
- (4) (a)-(iii), (b)-(i), (c)-(iv), (d)-(ii)

Official Ans. by NTA (4)

- **Sol.** (a) Magnetic Induction = $MT^{-2}A^{-1}$
 - (b) Magnetic Flux = $ML^2T^{-2}A^{-1}$
 - (c) Magnetic Permeability = $MLT^{-2}A^{-2}$
 - (d) Magnetization = $M^0 L^{-1} A$

Ans. 4

18. In the given circuit the AC source has $\omega = 100 \text{ rad s}^{-1}$. Considering the inductor and capacitor to be ideal, what will be the current I flowing through the circuit?



Sol.
$$Z_{c} = \sqrt{\left(\frac{1}{\omega C}\right)^{2} + R^{2}}$$

 $= \sqrt{\left(\frac{1}{100 \times 100 \times 10^{-6}}\right)^{2} + 100^{2}}$
 $Z_{c} = \sqrt{(100)^{2} + (100)^{2}}$
 $= 100\sqrt{2}$
 $Z_{L} = \sqrt{(\omega L)^{2} + R^{2}}$
 $\sqrt{(100 \times 0.5)^{2} + 80^{2}}$
 $= 50\sqrt{2}$
 $i_{c} = \frac{200}{z_{c}} = \frac{200}{100\sqrt{2}} = \sqrt{2}$
 $i_{L} = \frac{200}{z_{L}} = \frac{200}{50\sqrt{2}} = 2\sqrt{2}$
 $\cos\phi_{1} = \frac{100}{10\sqrt{2}} = \frac{1}{\sqrt{2}} \Rightarrow \phi_{1} = 45^{\circ}$
 $\cos\phi_{2} = \frac{50}{50\sqrt{2}} = \frac{1}{\sqrt{2}} \Rightarrow \phi_{2} = 45^{\circ}$
 I_{L}
 $I = \sqrt{I_{c}^{2} + I_{L}^{2}}$
 $= \sqrt{10}$
 $I = 3.16 \text{ A}$
Ans. 3.16
19. If the length of the pendulum in pendulum clock increases by 0.1%, then the error in time per day is:
(1) 86.4 s

(2) 4.32 s

- (3) 43.2 s
- (4) 8.64 s

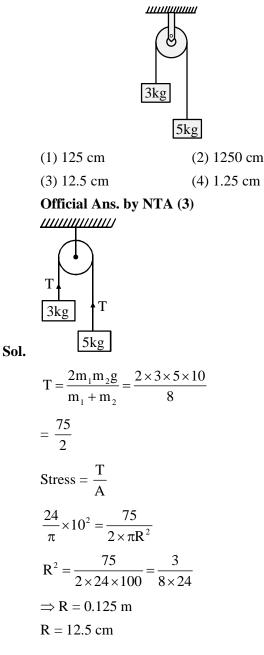
Official Ans. by NTA (3)

Sol.
$$T = 2\pi \sqrt{\frac{\ell}{g}}$$

 $\frac{\Delta T}{T} = \frac{1}{2} \frac{\Delta \ell}{\ell}$
 $\Delta T = \frac{1}{2} \times \frac{0.1}{100} \times 24 \times 3600$
 $\Delta T = 43.2$
Ans. 3

Two blocks of masses 3 kg and 5 kg are connected 20. by a metal wire going over a smooth pulley. The breaking stress of the metal is $\frac{24}{\pi} \times 10^2$ Nm⁻². What is the minimum radius of the wire?

 $(Take g = 10 ms^{-2})$



7

pendulum clock

Final JEE-Main Exam August, 2021/26-08-2021/Eve

SECTION-B

1. Two waves are simultaneously passing through a string and their equations are :

> $y_1 = A_1 \sin k(x-vt), y_2 = A_2 \sin k(x-vt + x_0)$. Given amplitudes $A_1 = 12$ mm and $A_2 = 5$ mm, $x_0 = 3.5$ cm and wave number k = 6.28 cm⁻¹. The amplitude of resulting wave will be mm.

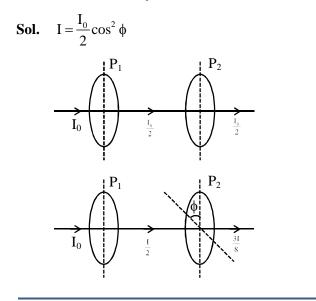
Official Ans. by NTA (7)

Sol.
$$y_1 = A_1 \sin k(x - vt)$$

 $y_1 = 12 \sin 6.28 (x - vt)$
 $y_2 = 5 \sin 6.28 (x - vt + 3.5)$
 $\Delta \phi = \frac{2\pi}{\lambda} (\Delta x)$
 $= K(\Delta x)$
 $= 6.28 \times 3.5 = \frac{7}{2} \times 2\pi = 7\pi$
 $A_{net} = \sqrt{A_1^2 + A_2^2 + 2A_1A_2 \cos \phi}$
 $A_{net} = \sqrt{(12)^2 + (5)^2 + 2(12)(5)\cos(7\pi)}$
 $= \sqrt{144 + 25 - 120}$
Ans. 7

2. A source of light is placed in front of a screen. Intensity of light on the screen is I. Two Polaroids P_1 and P_2 are so placed in between the source of light and screen that the intensity of light on screen is I/2. P₂ should be rotated by an angle of (degrees) so that the intensity of light on the screen becomes $\frac{3I}{8}$.

Official Ans. by NTA (30)



$$\frac{I}{2}\cos^2\phi = \frac{3I}{8}$$
$$\cos^2\phi = \frac{3}{4}$$
$$\cos^2\phi = \frac{\sqrt{3}}{2}$$
$$\Rightarrow \phi = 30$$
Ans. 30

3. If the maximum value of accelerating potential provided by a ratio frequency oscillator is 12 kV. The number of revolution made by a proton in a cyclotron to achieve one sixth of the speed of light is

$$[m_p = 1.67 \times 10^{-27} \text{ kg}, e = 1.6 \times 10^{-19} \text{ C},$$

Speed of light = 3×10^8 m/s]

Official Ans. by NTA (543)

Sol. V = 12 kV

> Number of revolution = n $n \big[2 \times q_{\scriptscriptstyle P} \times V \big] \!=\! \frac{1}{2} m_{\scriptscriptstyle P} \times v_{\scriptscriptstyle P}^2$ $n[2 \times 1.6 \times 10^{-19} \times 12 \times 10^{3}]$ $=\frac{1}{2} \times 1.67 \times 10^{-27} \times \left[\frac{3 \times 10^8}{6}\right]^2$ $n(38.4 \times 10^{-16}) = 0.2087 \times 10^{-11}$ n = 543.4Ans. 543

The acceleration due to gravity is found upto an

4.

accuracy of 4% on a planet. The energy supplied to a simple pendulum to known mass 'm' to undertake oscillations of time period T is being estimated. If time period is measured to an accuracy of 3%, the accuracy to which E is known as%

Official Ans. by NTA (14)

Sol.
$$T = 2\pi \sqrt{\frac{\ell}{g}} \implies \ell = \frac{T^2 g}{4\pi^2}$$

 $E = mg\ell \frac{\theta^2}{2} = mg^2 \frac{T^2 \theta^2}{8\pi^2}$
 $\frac{dE}{E} = 2\left(\frac{dg}{g} + \frac{dT}{T}\right)$
 $= (4+3) = 14\%$

Official Ans. by NTA (60)

Sol. Maximum emf $\varepsilon = N \omega AB$

N = 20, ω = 50, B = 3 ×10⁻²T ε = 20 × 50 × π × (0.08)² × 3 × 10⁻² = 60.28 × 10⁻² Rounded off to nearest integer = 60

Ans.60

6. Two simple harmonic motions are represented by the equations

$$x_1 = 5 \sin \left(2\pi t + \frac{\pi}{4}\right)$$
 and $x_2 = 5\sqrt{2}$ (sin $2\pi t + \cos 2\pi t$).

The amplitude of second motion is times the amplitude in first motion.

Official Ans. by NTA (2)

Sol.
$$x_2 = 5\sqrt{2} \left(\frac{1}{\sqrt{2}} \sin 2\pi t + \frac{1}{\sqrt{2}} \cos 2\pi t \right) \sqrt{2}$$

$$= 10 \sin \left(2\pi t + \frac{\pi}{4} \right)$$
$$\therefore \frac{A_2}{A_1} = \frac{10}{5} = 2$$

Ans. 2

7. A coil in the shape of an equilateral triangle of side 10 cm lies in a vertical plane between the pole pieces of permanent magnet producing a horizontal magnetic field 20 mT. The torque acting on the coil when a current of 0.2 A is passed through it and its plane becomes parallel to the magnetic field will be $\sqrt{x} \times 10^{-5}$ Nm. The value of x is......

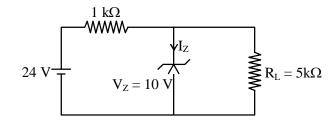
Official Ans. by NTA (3)

Sol.
$$\overrightarrow{B}$$
 $\overrightarrow{10 \text{ cm}}$
 $\vec{\tau} = \vec{M} \times \vec{B} = \text{MBsin90}^{\circ}$
 $= \text{MB} = \frac{i\sqrt{3}\ell^2}{4}\text{B}$
 $= \sqrt{3} \times 10^{-5} \text{N} - \text{m}$
Ans. 3

8.

Λ

For the given circuit, the power across zener diode is mW.



Sol.

$$24 V \downarrow V_{z} = 10$$

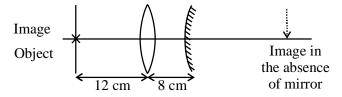
$$i = \frac{10V}{5k\Omega} = 2mA$$

$$I = \frac{14V}{1k\Omega} = 14mA$$

$$\therefore I_{z} = 12mA$$

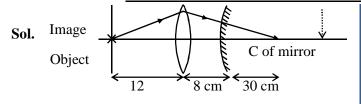
$$\therefore P = I_{z}V_{z} = 120 \text{ mW}$$
Ans. 120
9. An object is placed at a distance of 12 cm from the second s

An object is placed at a distance of 12 cm from a convex lens. A convex mirror of focal length 15 cm is placed on other side of lens at 8 cm as shown in the figure. Image of object coincides with the object.



When the convex mirror is removed, a real and inverted image is formed at a position. The distance of the image from the object will be(cm)

Official Ans. by NTA (50)

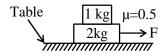


For the object to coincide with image, the light must fall perpendicularly to mirror. Which means that the light will have to converge at C of mirror. Without the mirror also, the light would coverage at C.

So the distance is : 12 + 8 + 30 = 50 cm

10. The coefficient of static friction between two blocks is 0.5 and the table is smooth. The maximum horizontal force that can be applied to move the blocks together isN.

 $(take g = 10 ms^{-2})$



≯F

....(i)

Official Ans. by NTA (15)

Table µ=0.5 1 kg 2kg Sol.

F = 3a (For system)

 $fs_{max} = 1a$ (for 1kg block)(ii)

 $\mu \times 1 \times g = a$

 \Rightarrow 5 = a

F = 15N