

**FINAL JEE-MAIN EXAMINATION – JANUARY, 2023**

**(Held On Wednesday 01<sup>st</sup> February, 2023)**

**TIME : 3 : 00 PM to 6 : 00 PM**

**PHYSICS**

**TEST PAPER WITH SOLUTION**

**SECTION-A**

1. A Carnot engine operating between two reservoirs has efficiency  $\frac{1}{3}$ . When the temperature of cold reservoir raised by  $x$ , its efficiency decreases to  $\frac{1}{6}$ .

The value of  $x$ , if the temperature of hot reservoir is  $99^\circ\text{C}$ , will be:

- (1) 16.5 K                      (2) 33 K
- (3) 66 K                        (4) 62 K

**Official Ans. by NTA (4)**

**Ans. (4)**

**Sol.**  $T_H = 99^\circ\text{C} = 99 + 273$   
 $= 372\text{ K}$ .

$$1 - \frac{T_C}{T_H} = \frac{1}{3}$$

$$\frac{T_C}{T_H} = \frac{2}{3} \quad \text{---(1)} \Rightarrow T_C = \frac{2}{3} \times 372$$

$$= 2 \times 124 = 248\text{ K}$$

$$1 - \frac{T_C + X}{T_H} = \frac{1}{6}$$

$$\frac{5}{6} = \frac{T_C + X}{T_H}$$

$$\frac{5}{6} = \frac{248 + X}{372}$$

$$248 + X = 5 \times 62$$

$$X = 310 - 248 = 62\text{K}$$

2. Given below are two statements : One is labelled as **Assertion A** and the other is labelled as **Reason R**.

**Assertion A :** Two metallic spheres are charged to the same potential. One of them is hollow and another is solid, and both have the same radii. Solid sphere will have lower charge than the hollow one.

**Reason R :** Capacitance of metallic spheres depend on the radii of spheres.

In the light of the above statements, choose the correct answer from the options given below.

- (1) **A** is false but **R** is true
- (2) Both **A** and **R** are true and **R** is the correct explanation of **A**
- (3) **A** is true but **R** is false
- (4) Both **A** and **R** are true but **R** is not the correct explanation of **A**

**Official Ans. by NTA (1)**

**Ans. (1)**

**Sol.** Potential of a conducting sphere is

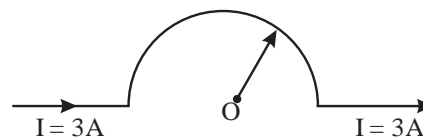
$$V = \frac{KQ}{R} \quad (\text{Solid as well as hollow})$$

$$V_1 = V_2 \text{ and } R_1 = R_2$$

$$\therefore Q_1 = Q_2$$

3. As shown in the figure, a long straight conductor with semicircular arc of radius  $\frac{\pi}{10}\text{ m}$  is carrying current  $I = 3\text{A}$ . The magnitude of the magnetic field. at the center  $O$  of the arc is:

(The permeability of the vacuum =  $4\pi \times 10^{-7}\text{ NA}^{-2}$ )



- (1)  $6\mu\text{T}$                                       (2)  $1\mu\text{T}$
- (3)  $4\mu\text{T}$                                       (4)  $3\mu\text{T}$

**Official Ans. by NTA (4)**

**Ans. (4)**

**Sol.**  $B_C = \frac{\mu_0 I}{4\pi R} (\pi)$  (B at centre of circular arc)

$$= \frac{\mu_0 I}{4R} = \frac{4\pi \times 10^{-7} \times 3}{4 \times \frac{\pi}{10}}$$

$$= 3 \times 10^{-6}\text{ T} = 3\mu\text{T}$$



$$v_1 = 60 \text{ cm}$$

$$\frac{1}{v_2} + \frac{1}{(-25)} = \frac{1}{(-20)}$$

$$\frac{1}{v_2} = \frac{-1}{20} + \frac{1}{25}$$

$$= \frac{-5 + 4}{100} = \frac{-1}{100}$$

$$v_2 = -100 \text{ cm}$$

$$d = 60 + 100 = 160 \text{ cm}$$

8. The Young's modulus of a steel wire of length 6 m and cross-sectional area  $3 \text{ mm}^2$ , is  $2 \times 10^{11} \text{ N/m}^2$ . The wire is suspended from its support on a given planet. A block of mass 4 kg is attached to the free end of the wire. The acceleration due to gravity on the planet is  $\frac{1}{4}$  of its value on the earth. The elongation of wire is (Take  $g$  on the earth =  $10 \text{ m/s}^2$ ):

- (1) 1 cm                                      (2) 1 mm  
 (3) 0.1 mm                                    (4) 0.1 cm

Official Ans. by NTA (3)

Ans. (3)

Sol. Tension (F) = mg  
 $= 4 \times \frac{10}{4} = 10 \text{ N}$

$$\Delta L = \frac{FL}{AY}$$

$$= \frac{10 \times 6}{3 \times 10^{-6} \times 2 \times 10^{11}}$$

$$= 10^{-4} \text{ m} = 0.1 \text{ mm}$$

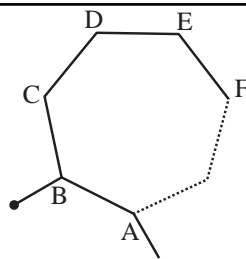
9. Equivalent resistance between the adjacent corners of a regular n-sided polygon of uniform wire of resistance R would be:

- (1)  $\frac{(n-1)R}{n^2}$                                       (2)  $\frac{(n-1)R}{(2n-1)}$   
 (3)  $\frac{n^2R}{n-1}$                                       (4)  $\frac{(n-1)R}{n}$

Official Ans. by NTA (1)

Ans. (1)

Sol.



Suppose resistance of each arm is r, then  $r = R/n$

$$R_{\text{eq}(AB)} = \frac{R_1 R_2}{R_1 + R_2}$$

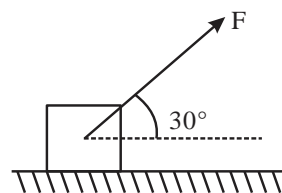
$$\frac{r(n-1)r}{r + (n-1)r}$$

$$= \frac{r(n-1)r}{nr}$$

$$= \frac{n-1}{n} r$$

$$= \frac{(n-1)R}{n^2}$$

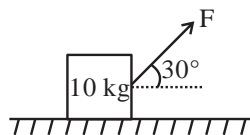
10. As shown in the figure a block of mass 10 kg lying on a horizontal surface is pulled by a force F acting at an angle  $30^\circ$ , with horizontal. For  $\mu_s = 0.25$ , the block will just start to move for the value of F: [Given  $g = 10 \text{ ms}^{-2}$ ]



- (1) 33.3 N                                      (2) 25.2 N  
 (3) 20 N                                        (4) 35.7 N

Official Ans. by NTA (2)

Ans. (2)



Sol.

$$N = Mg - F \sin 30^\circ$$

$$= mg - \frac{F}{2} = 100 - \frac{F}{2} = \frac{200 - F}{2}$$

$$F \cos 30^\circ = \mu N$$

$$\sqrt{3} \frac{F}{2} = 0.25 \times \left( \frac{200 - F}{2} \right)$$

$$4\sqrt{3}F = 200 - F$$

$$F = \frac{200}{4\sqrt{3} + 1} = 25.22$$



**Sol.**  $V_e = \sqrt{\frac{2GM}{R}} = \sqrt{\frac{2G\rho \frac{4}{3}\pi R^3}{R}} = C\sqrt{\rho}\cdot R$

$$\frac{V_{e1}}{V_{e2}} = \frac{R_1}{R_2} \sqrt{\frac{\rho_1}{\rho_2}} = \frac{1}{2}$$

$$\frac{R_1^2}{R_2^2} \times \frac{\rho_1}{\rho_2} = \frac{1}{4}$$

$$\frac{R_1}{R_2} = \frac{1}{3}$$

$$g = \frac{GM}{R^2} = \frac{G \frac{4}{3} \pi R^3 \times \rho}{R^2} = C \cdot \rho R$$

$$\frac{g_1}{g_2} = \frac{\rho_1 R_1}{\rho_2 R_2} = \frac{1}{4} \frac{R_2^2}{R_1^2} \times \frac{R_1}{R_2}$$

$$= \frac{1}{4} \times \frac{R_2}{R_1} = \frac{3}{4}$$

**15.** An electron of a hydrogen like atom, having  $Z = 4$ , jumps from 4<sup>th</sup> energy state to 2<sup>nd</sup> energy state, The energy released in this process, will be:

(Given  $Rch = 13.6 \text{ eV}$ )

Where  $R =$  Rydberg constant

$c =$  Speed of light in vacuum

$h =$  Planck's constant

(1) 13.6 eV

(2) 10.5 eV

(3) 3.4 eV

(4) 40.8 eV

**Official Ans. by NTA (4)**

**Ans. (4)**

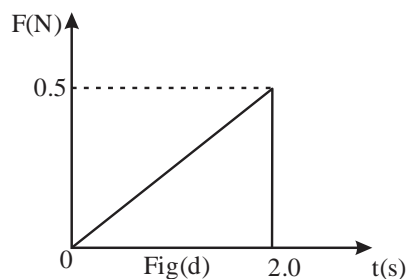
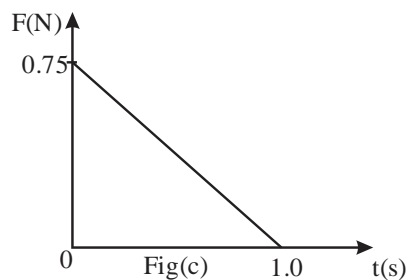
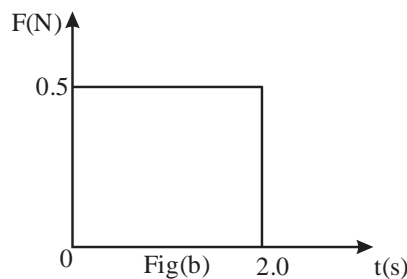
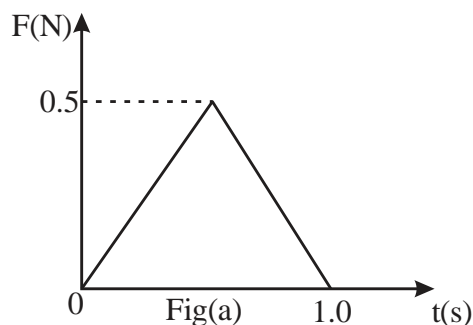
**Sol.**  $\Delta E = 13.6 Z^2 \left[ \frac{1}{2^2} - \frac{1}{4^2} \right] \text{eV}$

$$= 13.6 \times (4)^2 \left( \frac{1}{4} - \frac{1}{16} \right) \text{eV.}$$

$$= 13.6 [4 - 1] \text{eV}$$

$$= 13.6 \times 3 = 40.8 \text{ eV}$$

**16.** Figures (a), (b), (c) and (d) show variation of force with time.



The impulse is highest in figure.

(1) Fig (c)

(2) Fig (b)

(3) Fig (a)

(4) Fig (d)

**Official Ans. by NTA (2)**

**Ans. (2)**

**Sol.** Impulse = Area under  $F = t$  curve

(a)  $\frac{1}{2} \times 1 \times 0.5 = \frac{1}{4} \text{ N.s}$

(b)  $0.5 \times 2 = 1 \text{ N.s (maximum)}$

(c)  $\frac{1}{2} \times 1 \times 0.75 = \frac{3}{8} \text{ N.s}$

(d)  $\frac{1}{2} \times 2 \times 0.5 = \frac{1}{2} \text{ N.s}$

17. If the velocity of light  $c$ , universal gravitational constant  $G$  and planck's constant  $h$  are chosen as fundamental quantities. The dimensions of mass in the new system is:

- (1)  $\left[ h^{\frac{1}{2}} c^{\frac{1}{2}} G^1 \right]$  (2)  $\left[ h^1 c^1 G^{-1} \right]$   
 (3)  $\left[ h^{\frac{1}{2}} c^{\frac{1}{2}} G^{\frac{1}{2}} \right]$  (4)  $\left[ h^{\frac{1}{2}} c^{\frac{1}{2}} G^{-\frac{1}{2}} \right]$

Official Ans. by NTA (4)

Ans. (4)

Sol. Say dimensional formale of mass is  $H^x C^y G^z$

$$M^1 = (ML^2T^{-1})^x (LT^{-1}) (M^{-1}L^3T^{-2})^z$$

$$M^1 L^0 T^0 = M^{x-z} L^{2x+y+3z} T^{-x-y-2z}$$

on comparing both side

$$x - z = 1$$

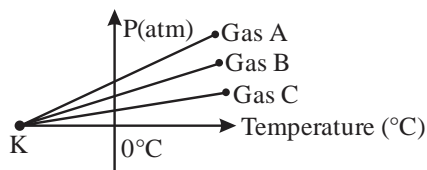
$$2x + y + 3z = 0$$

$$-x - y - 2z = 0$$

On solving above equations we get

$$x = \frac{1}{2} \quad y = \frac{1}{2} \quad z = -\frac{1}{2}$$

18. For three low density gases A, B, C pressure versus temperature graphs are plotted while keeping them at constant volume, as shown in the figure.



The temperature corresponding to the point 'K' is:

- (1)  $-273^\circ\text{C}$  (2)  $-100^\circ\text{C}$   
 (3)  $-373^\circ\text{C}$  (4)  $-40^\circ\text{C}$

Official Ans. by NTA (1)

Ans. (1)

Sol. For isochoric process

$$\frac{P}{T} = n \frac{R}{V} = \text{constan } t$$

$$P = \frac{nR}{V}(t + 273)$$

$$\text{If } P = 0 \Rightarrow t = -273^\circ\text{C}$$

19. The ratio of average electric energy density and total average energy density of electromagnetic wave is:

- (1) 2 (2) 1  
 (3) 3 (4)  $\frac{1}{2}$

Official Ans. by NTA (4)

Ans. (4)

$$\text{Sol. } \langle u_E \rangle = \langle u_B \rangle = \frac{1}{2} \langle u_{\text{total}} \rangle$$

$$\text{So } \frac{\langle u_E \rangle}{\langle u_{\text{total}} \rangle} = \frac{1}{2}$$

20. The threshold frequency of metal is  $f_0$ . When the light of frequency  $2f_0$  is incident on the metal plate, the maximum velocity of photoelectron is  $v_1$ . When the frequency of incident radiation is increased to  $5f_0$ . the maximum velocity of photoelectrons emitted is  $v_2$ . The ratio of  $v_1$  to  $v_2$  is:

- (1)  $\frac{v_1}{v_2} = \frac{1}{2}$  (2)  $\frac{v_1}{v_2} = \frac{1}{8}$   
 (3)  $\frac{v_1}{v_2} = \frac{1}{16}$  (4)  $\frac{v_1}{v_2} = \frac{1}{4}$

Official Ans. by NTA (1)

Ans. (1)

$$\text{Sol. } K_{\text{max}} = hf - hf_0$$

$$\text{For } f = 2f_0$$

$$\frac{1}{2} m V_1^2 = 2 h f_0 - h f_0 = h f_0$$

$$\text{For } f = 5 f_0$$

$$\frac{1}{2} m V_2^2 = 5 h f_0 - h f_0 = 4h f_0$$

$$\frac{V_1}{V_2} = \frac{1}{2}$$

SECTION-B

21. For a train engine moving with speed of  $20 \text{ ms}^{-1}$ . the driver must apply brakes at a distance of 500 m before the station for the train to come to rest at the station. If the brakes were applied at half of this distance, the train engine would cross the station with speed  $\sqrt{x} \text{ ms}^{-1}$ . The value of x is \_\_\_\_\_ (Assuming same retardation is produced by brakes)

**Official Ans. by NTA (200)**

**Ans. (200)**

- Sol.**  $u = 20 \text{ m/s}$ ,  $S_1 = 500 \text{ m}$ ,  $v = 0$

By third equation of motion

$$0 = (20)^2 - 2a \cdot 500 \Rightarrow a = \frac{4}{10} \text{ m/s}^2$$

$$u = 20 \text{ m/s}$$
,  $S_2 = 250 \text{ m}$ ,  $v = ?$

$$v^2 = (20)^2 - 2a \cdot 250$$

$$= v = \sqrt{200} \text{ m/s}$$

$$x = 200$$

22. A force  $F = (5 + 3y^2)$  acts on a particle in the y-direction, where F is newton and y is in meter. The work done by the force during a displacement from  $y = 2\text{m}$  to  $y = 5\text{m}$  is \_\_\_\_\_ J.

**Official Ans. by NTA (132)**

**Ans. (132)**

- Sol.**  $F = 5 + 3y^2$

$$W = \int_2^5 (5 + 3y^2) dy$$

$$= \left[ 5y + \frac{3y^3}{3} \right]_2^5$$

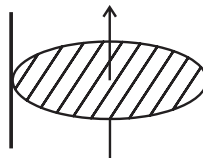
$$= 132 \text{ J}$$

23. Moment of inertia of a disc of mass M and radius 'R' about any of its diameter is  $\frac{MR^2}{4}$ . The moment of inertia of this disc about an axis normal to the disc and passing through a point on its edge will be,  $\frac{x}{2} MR^2$ . The value of x is \_\_\_\_\_.

**Official Ans. by NTA (3)**

**Ans. (3)**

**Sol.**



$$I = I_{cm} + Md^2$$

$$= \frac{MR^2}{2} + MR^2$$

$$= \frac{3}{2} MR^2$$

$$x = 3$$

24. Nucleus A having  $Z = 17$  and equal number of protons and neutrons has 1.2 MeV binding energy per nucleon.

Another nucleus B of  $Z = 12$  has total 26 nucleons and 1.8 MeV binding energy per nucleon.

The difference of binding energy of B and A will be \_\_\_\_\_ MeV.

**Official Ans. by NTA (6)**

**Ans. (6)**

- Sol.** For A mass number = 34

$$\text{Total binding energy} = 1.2 \times 34 = 40.8 \text{ MeV}$$

For B mass number = 26

$$\text{total binding energy} = 1.8 \times 26 \text{ MeV}$$

$$= 46.8 \text{ MeV}$$

Difference of BE = 6 MeV

25. A square shaped coil of area  $70 \text{ cm}^2$  having 600 turns rotates in a magnetic field of  $0.4 \text{ wbm}^{-2}$ , about an axis which is parallel to one of the side of the coil and perpendicular to the direction of field. If the coil completes 500 revolution in a minute, the instantaneous emf when the plane of the coil is inclined at  $60^\circ$  with the field, will be \_\_\_\_\_ V.

(Take  $\pi = \frac{22}{7}$ )

**Official Ans. by NTA (44)**

**Ans. (44)**

- Sol.**  $N = 600$ ,  $A = 70 \times 10^{-4} \text{ m}^2$ ,  $B = 0.4\text{T}$

$$\omega = \frac{500 \times 2\pi}{60} = \frac{100\pi}{6} \text{ rad/s}$$

$$E = NAB\omega \sin\omega t \quad \omega t \text{ is angle b/w } \vec{A} \text{ \& } \vec{B}$$

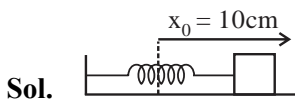
$$= 600 \times 70 \times 10^{-4} \times 0.4 \times \frac{100\pi}{6} \times \frac{1}{2}$$

$$= 44 \text{ V}$$

26. A block is fastened to a horizontal spring. The block is pulled to a distance  $x = 10$  cm from its equilibrium position (at  $x = 0$ ) on a frictionless surface from rest. The energy of the block at  $x = 5$  cm is 0.25 J. The spring constant of the spring is  $\underline{\hspace{2cm}} \text{Nm}^{-1}$ .

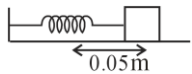
Official Ans. by NTA (50)

Ans. (67)



$$U_i = \frac{1}{2} kx_0^2$$

$$K_i = 0$$



$$U_f = \frac{1}{2} k \left( \frac{x_0}{2} \right)^2$$

$$K_f = 0.25 \text{ J}$$

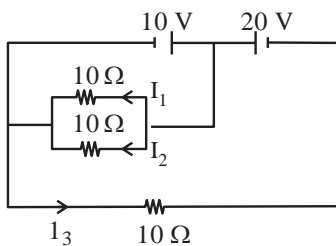
$$\frac{1}{2} kx_0^2 + 0 = \frac{1}{2} k \frac{x_0^2}{4} + 0.25$$

$$\frac{1}{2} kx_0^2 \frac{3}{4} = \frac{1}{4}$$

$$\frac{1}{2} k \frac{3}{100} = 1 \Rightarrow k = \frac{200}{3} \text{ N/m}$$

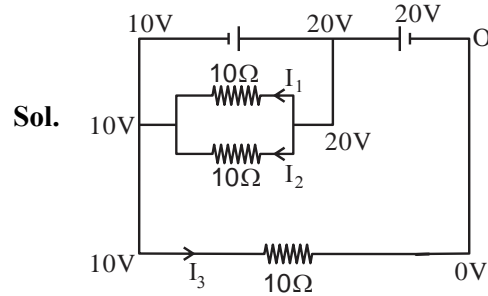
$$= 67 \text{ N/m}$$

27. In the given circuit the value of  $\left| \frac{I_1 + I_3}{I_2} \right|$  is:



Official Ans. by NTA (2)

Ans. (2)

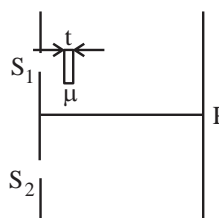


$$I_1 = I_2 = \frac{20 - 10}{10} = 1 \text{ A}$$

$$I_3 = 1 \text{ A}$$

$$\left| \frac{I_1 + I_3}{I_2} \right| = 2$$

28. As shown in the figure, in Young's double slit experiment, a thin plate of thickness  $t = 10 \mu\text{m}$  and refractive index  $\mu = 1.2$  is inserted in front of slit  $S_1$ . The experiment is conducted in air ( $\mu = 1$ ) and uses a monochromatic light of wavelength  $\lambda = 500 \text{ nm}$ . Due to the insertion of the plate, central maxima is shifted by a distance of  $x\beta_0$ .  $\beta_0$  is the fringe-width before the insertion of the plate. The value of the  $x$  is  $\underline{\hspace{2cm}}$ .



Official Ans. by NTA (4)

Ans. (4)

Sol. Fringe shift =  $\frac{t(\mu - 1)}{\lambda} B$

$$= \frac{10 \times 10^{-6} (1.2 - 1)}{5 \times 10^{-7}} B$$

$$= \frac{10^{-5} \times 0.2}{5 \times 10^{-7}} = 4$$

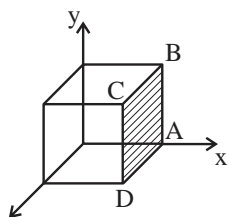


29. A cubical volume is bounded by the surfaces  $x = 0, x = a, y = 0, y = a, z = 0, z = a$ . The electric field in the region is given by  $\vec{E} = E_0 x \hat{i}$ . Where  $E_0 = 4 \times 10^4 \text{ NC}^{-1} \text{ m}^{-1}$ . If  $a = 2 \text{ cm}$ , the charge contained in the cubical volume is  $Q \times 10^{-14} \text{ C}$ . The value of  $Q$  is \_\_\_\_\_.

Take  $\epsilon_0 = 9 \times 10^{-12} \text{ C}^2/\text{Nm}^2$

Official Ans. by NTA (288)

Ans. (288)



Sol.

$$\vec{E} = E_0 x \hat{i}$$

$$\phi_{\text{net}} = \phi_{\text{ABCD}} = E_0 a \cdot a^2$$

$$\frac{q_{\text{en}}}{\epsilon_0} = E_0 a^3$$

$$q_{\text{en}} = E_0 \epsilon_0 a^3$$

$$= 4 \times 10^4 \times 9 \times 10^{-12} \times 8 \times 10^{-6}$$

$$= 288 \times 10^{-14} \text{ C}$$

$$Q = 288$$

Ans. 288

30. The surface of water in a water tank of cross section area  $750 \text{ cm}^2$  on the top of a house is  $h \text{ m}$ . above the tap level. The speed of water coming out through the tap of cross section area  $500 \text{ mm}^2$  is  $30 \text{ cm/s}$ . At that instant,  $\frac{dh}{dt}$  is  $x \times 10^{-3} \text{ m/s}$ . The value of  $x$  will be \_\_\_\_\_.

Official Ans. by NTA (2)

Ans. (2)

Sol.  $A_1 V_1 = A_2 V_2$

$$750 \times 10^{-4} V_1 = 500 \times 10^{-6} \times 0.3$$

$$V_1 = \frac{500 \times 3 \times 10^{-3}}{750} \text{ m/s}$$

$$= 2 \times 10^{-3} \text{ m/s}$$

$$\frac{dh}{dt} = -2 \times 10^{-3} \text{ m/s}$$