

FINAL JEE(Advanced) EXAMINATION – 2023**(Held On Sunday 04th June, 2023)****PAPER-1****TEST PAPER WITH SOLUTION****PHYSICS****SECTION-1 : (Maximum Marks : 12)**

- This section contains **THREE (03)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks : +4 **ONLY** if (all) the correct option(s) is(are) chosen;

Partial Marks : +3 If all the four options are correct but **ONLY** three options are chosen;

Partial Marks : +2 If three or more options are correct but **ONLY** two options are chosen, both of which are correct;

Partial Marks : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option;

Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);

Negative Marks : -2 In all other cases.

- For example, in a question, if (A), (B) and (D) are the **ONLY** three options corresponding to correct answers, then

choosing **ONLY** (A), (B) and (D) will get +4 marks;

choosing **ONLY** (A) and (B) will get +2 marks;

choosing **ONLY** (A) and (D) will get +2 marks;

choosing **ONLY** (B) and (D) will get +2 marks;

choosing **ONLY** (A) will get +1 marks;

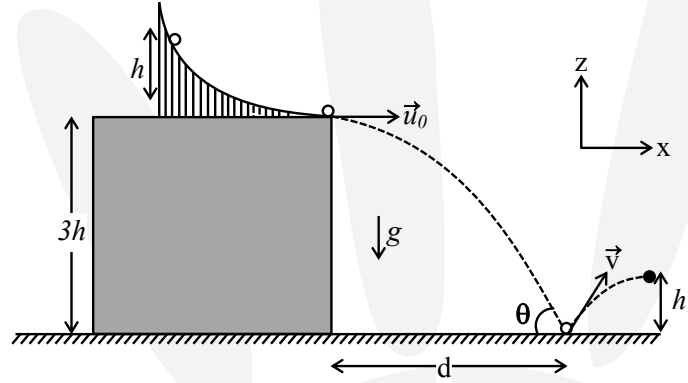
choosing **ONLY** (B) will get +1 marks;

choosing **ONLY** (D) will get +1 marks;

choosing no option (i.e. the question is unanswered) will get 0 marks; and

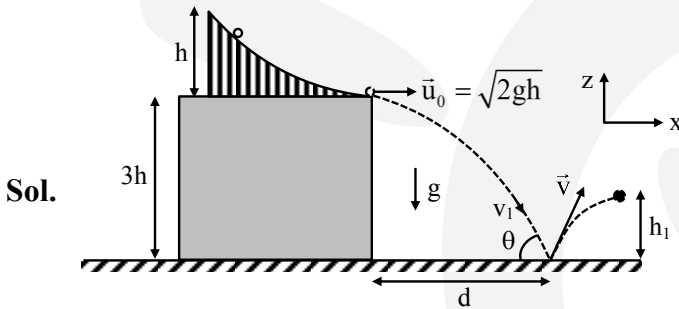
choosing any other combination of options will get -2 marks.

1. A slide with a frictionless curved surface, which becomes horizontal at its lower end, is fixed on the terrace of a building of height $3h$ from the ground, as shown in the figure. A spherical ball of mass m is released on the slide from rest at a height h from the top of the terrace. The ball leaves the slide with a velocity $\vec{u}_0 = u_0 \hat{x}$ and falls on the ground at a distance d from the building making an angle θ with the horizontal. It bounces off with a velocity \vec{v} and reaches a maximum height h_1 . The acceleration due to gravity is g and the coefficient of restitution of the ground is $1/\sqrt{3}$. Which of the following statement(s) is(are) correct?



- (A) $\vec{u}_0 = \sqrt{2gh} \hat{x}$ (B) $\vec{v} = \sqrt{2gh} (\hat{x} - \hat{z})$ (C) $\theta = 60^\circ$ (D) $d/h_1 = 2\sqrt{3}$

Ans. (A,C,D)



Sol.

$$\vec{v}_1 = \sqrt{2gh} \hat{i} - \sqrt{2g3h} \hat{k}$$

$$\vec{v} = \sqrt{2gh} \hat{i} + \sqrt{2g3h} \times \frac{1}{\sqrt{3}} \hat{k}$$

$$= \sqrt{2gh} \hat{i} + \sqrt{2gh} \hat{k}$$

$$\tan \theta = \frac{\sqrt{2g3h}}{\sqrt{2gh}} = \sqrt{3} \quad \theta = 60^\circ$$

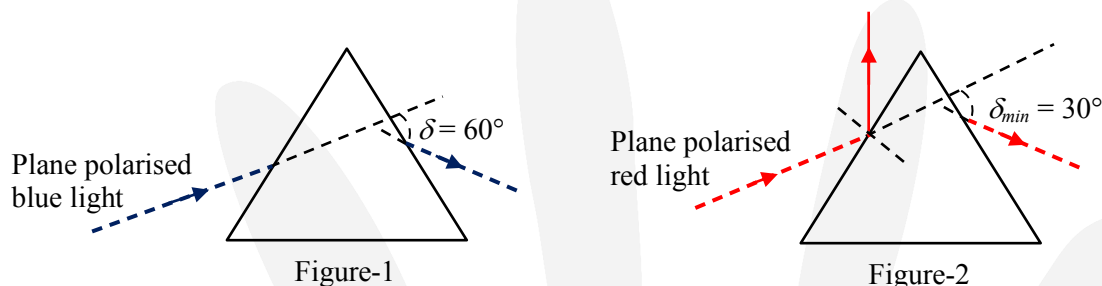
$$h_1 = \frac{v_{1y}^2}{2g} = \frac{2gh}{2g} = h$$

$$d = v_x t = \sqrt{2gh} \times \sqrt{\frac{2 \times 3h}{g}}$$

$$= \sqrt{2gh} \sqrt{\frac{6h}{g}} = 2\sqrt{3}h$$

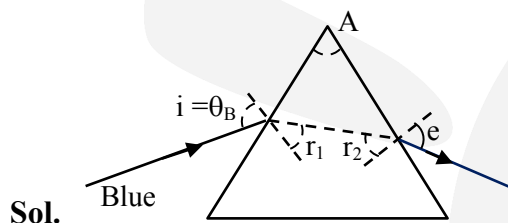
$$= \frac{d}{h_1} = 2\sqrt{3}$$

2. A plane polarized blue light ray is incident on a prism such that there is no reflection from the surface of the prism. The angle of deviation of the emergent ray is $\delta = 60^\circ$ (see Figure-1). The angle of minimum deviation for red light from the same prism is $\delta_{min} = 30^\circ$ (see Figure-2). The refractive index of the prism material for blue light is $\sqrt{3}$. Which of the following statement(s) is(are) correct?



- (A) The blue light is polarized in the plane of incidence.
 (B) The angle of the prism is 45° .
 (C) The refractive index of the material of the prism for red light is $\sqrt{2}$.
 (D) The angle of refraction for blue light in air at the exit plane of the prism is 60° .

Ans. (A,C,D)



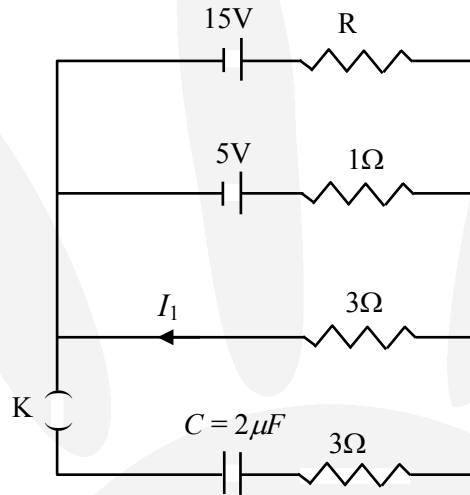
$$\begin{aligned} \tan \theta_B &= \mu_B = \sqrt{3} \\ i = \theta_B &= 60^\circ \\ 1 \sin 60^\circ &= \sqrt{3} \sin r_1 \\ r_1 &= 30^\circ \\ r_1 + r_2 &= A \\ \delta &= (i + e) - A \\ 60^\circ &= 60^\circ + e - A \\ e &= A \\ \sqrt{3} \sin r_2 &= 1 \sin e \\ \sqrt{3} \sin(A - 30) &= \sin A \end{aligned}$$

Solving
 $A = 60^\circ$
 $\therefore e = 60^\circ$
 For red light

$$\mu = \frac{\sin\left(\frac{A + \delta_{min}}{2}\right)}{\sin \frac{A}{2}} = \sqrt{2}$$

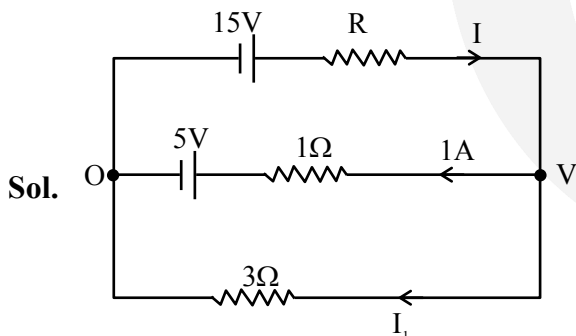
3. In a circuit shown in the figure, the capacitor C is initially uncharged and the key K is open. In this condition, a current of 1 A flows through the $1\ \Omega$ resistor. The key is closed at time $t = t_0$. Which of the following statement(s) is(are) correct?

[Given: $e^{-1} = 0.36$]



- (A) The value of the resistance R is $3\ \Omega$.
- (B) For $t < t_0$, the value of current I_1 is 2A.
- (C) At $t = t_0 + 7.2\ \mu\text{s}$, the current in the capacitor is 0.6 A.
- (D) For $t \rightarrow \infty$, the charge on the capacitor is $12\ \mu\text{C}$.

Ans. (A,B,C,D)



By writing voltage drop across $1\ \Omega$

$$\Rightarrow 0 + 5 + 1 \times 1 = V$$

$$V = 6$$

\Rightarrow Similarly across R

$$0 + 15 - I \times R = 6$$

$$IR = 9$$

\Rightarrow across 3Ω

$$6 - 3 I_1 = 0$$

$$I_1 = 2A$$

Hence option (B) is correct

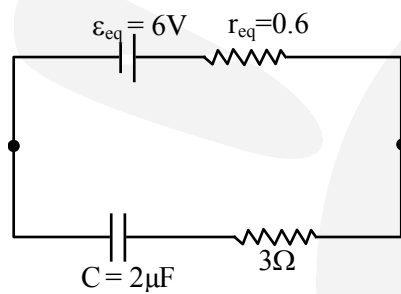
$$\Rightarrow I = 1 + 2 \quad (\text{by KCL})$$

$$I = 3$$

$$IR = 9$$

$$R = 3\Omega$$

Option (A) is correct



$$\varepsilon = \frac{\frac{15}{3} + \frac{5}{1} + \frac{0}{3}}{\frac{1}{3} + \frac{1}{1} + \frac{1}{3}} = 10 \times \frac{3}{5} = 6V$$

$$q_{\max} = 2 \times 6 = 12\mu C$$

$$i = \frac{6}{3.6} e^{-\frac{t}{\tau}}$$

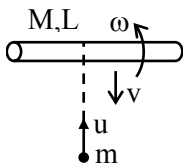
$$= \frac{5}{3} e^{-\frac{7.2}{7.2}} = \frac{5}{3} e^{-1} \approx 0.6A$$

SECTION-2 : (Maximum Marks : 12)

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:
Full Marks : +3 If **ONLY** the correct option is chosen;
Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);
Negative Marks : -1 In all other cases.

4. A bar of mass $M = 1.00$ kg and length $L = 0.20$ m is lying on a horizontal frictionless surface. One end of the bar is pivoted at a point about which it is free to rotate. A small mass $m = 0.10$ kg is moving on the same horizontal surface with 5.00 m s⁻¹ speed on a path perpendicular to the bar. It hits the bar at a distance $L/2$ from the pivoted end and returns back on the same path with speed v . After this elastic collision, the bar rotates with an angular velocity ω . Which of the following statement is correct?
- (A) $\omega = 6.98$ rad s⁻¹ and $v = 4.30$ m s⁻¹
 (B) $\omega = 3.75$ rad s⁻¹ and $v = 4.30$ m s⁻¹
 (C) $\omega = 3.75$ rad s⁻¹ and $v = 10.0$ m s⁻¹
 (D) $\omega = 6.80$ rad s⁻¹ and $v = 4.10$ m s⁻¹

Ans. (A)



Sol.

Applying angular momentum conservation about hinge

$$mv \frac{L}{2} + 0 = -mv \frac{L}{2} + \frac{ML^2}{3} \omega \dots(i)$$

Also from eq. of restitution

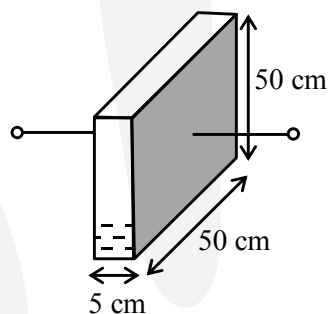
$$e = 1 = \frac{\omega \frac{L}{2} + V}{u} \Rightarrow u = \omega \frac{L}{2} + V \dots(ii)$$

Solving (i) & (ii)

$$\omega \approx 6.98 \text{ rad/sec} \ \& \ v = 4.30 \text{ m/s}$$

Hence option (A)

5. A container has a base of $50\text{ cm} \times 5\text{ cm}$ and height 50 cm , as shown in the figure. It has two parallel electrically conducting walls each of area $50\text{ cm} \times 50\text{ cm}$. The remaining walls of the container are thin and non-conducting. The container is being filled with a liquid of dielectric constant 3 at a uniform rate of $250\text{ cm}^3\text{ s}^{-1}$. What is the value of the capacitance of the container after 10 seconds? [Given: Permittivity of free space $\epsilon_0 = 9 \times 10^{-12}\text{ C}^2\text{ N}^{-1}\text{ m}^{-2}$, the effects of the non-conducting walls on the capacitance are negligible]



- (A) 27 pF (B) 63 pF (C) 81 pF (D) 135 pF

Ans. (B)

Sol. In $t = 10\text{ sec}$ volume of liquid is

$$V = 2500\text{ cc}$$

$$h = \frac{2500}{50 \times 5} = 10\text{ cm}$$

$$C_d = \frac{A_d \epsilon_0 k}{d}$$

$$= \frac{50 \times 10^{-2} \times 10 \times 10^{-2} \epsilon_0 \times 3}{5 \times 10^{-2}} = 3\epsilon_0$$

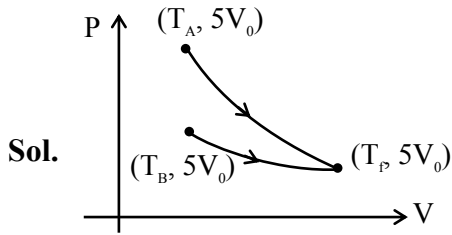
$$C_a = \frac{A_a \epsilon_0}{d} = \frac{50 \times 10^{-2} \times 40 \times 10^{-2} \epsilon_0}{5 \times 10^{-2}} = 4\epsilon_0$$

$$C = C_a + C_d = 7\epsilon_0$$

$$= 7 \times 9 \times 10^{-12} = 63\text{ Pf}$$

6. One mole of an ideal gas expands adiabatically from an initial state (T_A, V_0) to final state $(T_f, 5V_0)$. Another mole of the same gas expands isothermally from a different initial state (T_B, V_0) to the same final state $(T_f, 5V_0)$. The ratio of the specific heats at constant pressure and constant volume of this ideal gas is γ . What is the ratio T_A/T_B ?
- (A) $5^{\gamma-1}$ (B) $5^{1-\gamma}$ (C) 5^γ (D) $5^{1+\gamma}$

Ans. (A)



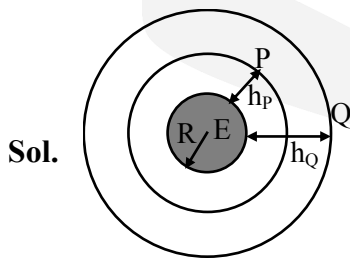
$$T_A V_0^{\gamma-1} = T_f (5V_0)^{\gamma-1}$$

$$\frac{T_A}{T_f} = 5^{\gamma-1} = \frac{T_A}{T_B}$$

7. Two satellites P and Q are moving in different circular orbits around the Earth (radius R). The heights of P and Q from the Earth surface are h_P and h_Q , respectively, where $h_P = R/3$. The accelerations of P and Q due to Earth's gravity are g_P and g_Q , respectively. If $g_P/g_Q = 36/25$, what is the value of h_Q ?

- (A) $3R/5$ (B) $R/6$ (C) $6R/5$ (D) $5R/6$

Ans. (A)



$$\frac{g_P}{g_Q} = \frac{\frac{GM}{r_P^2}}{\frac{GM}{r_Q^2}} = \left(\frac{r_Q}{r_P}\right)^2$$

$$\frac{36}{25} = \left(\frac{r_Q}{r_P}\right)^2$$

$$\frac{r_Q}{r_P} = \frac{6}{5}$$

$$r_Q = \frac{6}{5}r_P$$

$$R + h_Q = \frac{6}{5}\left(R + \frac{R}{3}\right)$$

$$h_Q = \frac{24}{15}R - R = \frac{9}{15}R = \frac{3}{5}R$$

SECTION-3 : (Maximum Marks : 24)

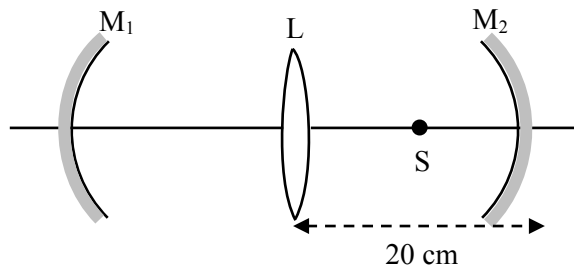
- This section contains **SIX (06)** questions.
- The answer to each question is a **NON-NEGATIVE INTEGER**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:
Full Marks : +4 If **ONLY** the correct integer is entered;
Zero Marks : 0 In all other cases.

8. A Hydrogen-like atom has atomic number Z . Photons emitted in the electronic transitions from level $n = 4$ to level $n = 3$ in these atoms are used to perform photoelectric effect experiment on a target metal. The maximum kinetic energy of the photoelectrons generated is 1.95 eV. If the photoelectric threshold wavelength for the target metal is 310 nm, the value of Z is _____.
 [Given: $hc = 1240$ eV-nm and $Rhc = 13.6$ eV, where R is the Rydberg constant, h is the Planck's constant and c is the speed of light in vacuum]

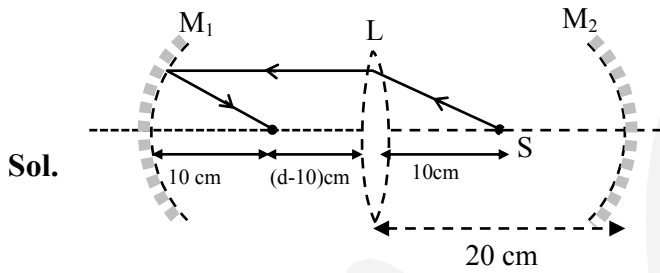
Ans. (3)

Sol. $n = 4$ $n = 3$
 $-1.51Z^2 \text{ eV}$ $-0.85 Z^2 \text{ eV}$
 $E = E_4 - E_3 = 0.66 Z^2 \text{ eV}$
 $K_{\text{max}} = E - W$
 $0.66 Z^2 - 1.95 + 4 = 5.95$
 $W = 0.66Z^2 - 1.95 = \frac{hc}{\lambda} = \frac{1240}{310}$
 $\therefore Z = 3$

9. An optical arrangement consists of two concave mirrors M_1 and M_2 , and a convex lens L with a common principal axis, as shown in the figure. The focal length of L is 10 cm. The radii of curvature of M_1 and M_2 are 20 cm and 24 cm, respectively. The distance between L and M_2 is 20 cm. A point object S is placed at the mid-point between L and M_2 on the axis. When the distance between L and M_1 is $n/7$ cm, one of the images coincides with S . The value of n is _____.



Ans. (80 or 150 or 220)



Two cases are possible if 1st refraction on lens :

Since object is at focus \Rightarrow light will become parallel.

1st reflection at M_1 :-

Light is parallel \Rightarrow Image will be at focus.

2nd refraction from L :-

$$u = -(d - 10)$$

$$f = 10 \text{ cm}$$

$$\frac{1}{v} - \frac{1}{\mu} = \frac{1}{f}$$

$$\frac{1}{v} + \frac{1}{d-10} = \frac{1}{10}$$

$$\frac{1}{v} = \frac{1}{10} - \frac{1}{(d-10)} \quad \dots (i)$$

This v will be object for M_2 , and image should be at 10 cm

$$\frac{1}{\mu} + \frac{1}{v_1} = \frac{1}{f}$$

$$-\frac{1}{(20-v)} - \frac{1}{10} = -\frac{1}{12}$$

$$\frac{1}{12} - \frac{1}{10} = \frac{1}{20-v}$$

$$-\frac{2}{120} = \frac{1}{20-v}$$

$$20 - v = -60$$

$$v = 80 \text{ cm}$$

From equation (i)

$$\frac{1}{80} = \frac{1}{10} - \frac{1}{d-10}$$

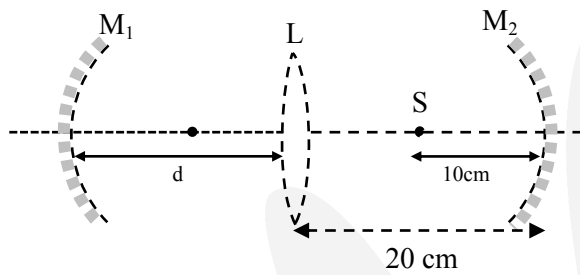
$$\frac{1}{d-10} = \frac{1}{10} - \frac{1}{80}$$

$$\frac{1}{d-10} = \frac{80-10}{800} = \frac{70}{800}$$

$$d-10 = \frac{80}{7} \Rightarrow d = 10 + \frac{80}{7} = \frac{150}{7}$$

$$\boxed{n = 150}$$

Case-2: If 1st reflection on mirror m_2



For m_2

$$\frac{1}{V_1} + \frac{1}{-10} = \frac{1}{-12}$$

$$V_1 = 60 \text{ cm}$$

Then refraction on lens L

$$u_2 = -80 \text{ cm}$$

$$\frac{1}{V_2} - \frac{1}{-60} = \frac{1}{10}$$

$$V_2 = \frac{80}{7}$$

Then reflection on m_2

Either V_2 is at centre (normal incidence)

$$d - \frac{80}{7} = 20$$

$$d = \frac{220}{7}$$

$$\frac{n}{7} = \frac{220}{7},$$

$$\boxed{n = 220}$$

V_2 is at pole of m_2

$$d - \frac{80}{7} = 0$$

$$d = \frac{80}{7}$$

$$\frac{n}{7} = \frac{80}{7}$$

$$\boxed{n = 80}$$

10. In an experiment for determination of the focal length of a thin convex lens, the distance of the object from the lens is 10 ± 0.1 cm and the distance of its real image from the lens is 20 ± 0.2 cm. The error in the determination of focal length of the lens is $n\%$. The value of n is _____.

Ans. (1)

Sol. $u = 10 \pm 0.1$ cm, $v = 20 \pm 0.2$ cm

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f} \Rightarrow \frac{1}{v^2} dv + \frac{1}{u^2} du = -\frac{1}{f^2} df$$

$$\frac{1}{20} + \frac{1}{10} = \frac{1}{f} \Rightarrow \frac{1}{f} = \frac{3}{20} \Rightarrow f = \frac{20}{3} \text{ cm}$$

$$\Rightarrow \frac{1}{(20)^2} (0.2) + \frac{1}{(10)^2} (0.1) = \frac{9}{400} df$$

$$df = \frac{1}{9} \left(\frac{400}{400} \times 0.2 + \frac{400}{100} \times 0.1 \right)$$

$$df = \frac{1}{9} (0.2 + 0.4) \Rightarrow df = \frac{0.6}{9}$$

$$\frac{df}{f} = \frac{0.6}{9} \times \frac{3}{20} = \frac{1}{100}$$

% error = 1 %

Sol. $\frac{1}{V} - \frac{1}{U} = \frac{1}{f}$; $+\frac{1}{20} + \frac{1}{10} = \frac{1}{f}$

$$-\frac{1}{V^2} dv + \frac{dU}{u^2} = -\frac{df}{f^2} \quad \frac{1+2}{20} = \frac{1}{f}; f = \frac{20}{3}$$

$$\frac{0.1}{100} + \frac{0.2}{400} = \frac{f\%}{f}$$

$$\frac{0.4+0.2}{400} = \frac{\Delta f}{f \left(\frac{20}{3} \right)}$$

$$\frac{0.6 \times 20}{400 \times 3} = \frac{\Delta f}{f}$$

$$\frac{1}{100} = \frac{\Delta f}{f}$$

% change in f is 1%

11. A closed container contains a homogeneous mixture of two moles of an ideal monatomic gas ($\gamma = 5/3$) and one mole of an ideal diatomic gas ($\gamma = 7/5$). Here, γ is the ratio of the specific heats at constant pressure and constant volume of an ideal gas. The gas mixture does a work of 66 Joule when heated at constant pressure. The change in its internal energy is _____ Joule.

Ans. (121)

Sol. At constant pressure

$$W = nR\Delta T = 66$$

$$\Delta U = n(C_V)_{\text{mix}}\Delta T$$

$$(C_V)_{\text{mix}} = \frac{n_1 C_{V_1} + n_2 C_{V_2}}{n_1 + n_2}$$

$$(C_V)_{\text{mix}} = \frac{2 \times \frac{3}{2}R + 1 \times \frac{5}{2}R}{3}$$

$$(C_V)_{\text{mix}} = \frac{11}{6}R$$

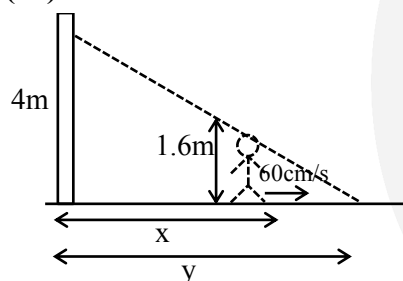
$$\Delta U = \frac{11}{6}(nR\Delta T)$$

$$\Delta U = \frac{11}{6} \times 66 = 121\text{J}$$

12. A person of height 1.6 m is walking away from a lamp post of height 4 m along a straight path on the flat ground. The lamp post and the person are always perpendicular to the ground. If the speed of the person is 60 cm s^{-1} , the speed of the tip of the person's shadow on the ground with respect to the person is _____ cm s^{-1} .

Ans. (40)

Sol.



$$\frac{4}{y} = \frac{1.6}{y-x}$$

$$4y - 4x = 1.6y$$

$$2.4y = 4x$$

$$x = 0.6y$$

$$\frac{dx}{dt} = 0.6 \times \frac{dy}{dt}$$

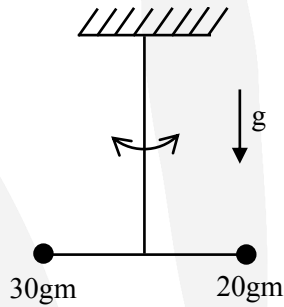
$$60 = 0.6 \times \frac{dy}{dt}$$

$$\therefore \frac{dy}{dt} = 100 \text{ cm/s}$$

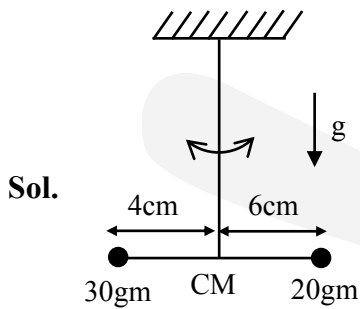
Speed of tip of person's

Shadow w.r.t person = $100 - 60 = 40 \text{ cm/s}$

13. Two point-like objects of masses 20 gm and 30 gm are fixed at the two ends of a rigid massless rod of length 10 cm. This system is suspended vertically from a rigid ceiling using a thin wire attached to its center of mass, as shown in the figure. The resulting torsional pendulum undergoes small oscillations. The torsional constant of the wire is $1.2 \times 10^{-8} \text{ N m rad}^{-1}$. The angular frequency of the oscillations in $n \times 10^{-3} \text{ rad s}^{-1}$. The value of n is _____.



Ans. (10)



$$T = \frac{2\pi}{\omega} = 2\pi \sqrt{\frac{I}{C}}$$

$$\Rightarrow \omega = \sqrt{\frac{C}{I}}$$

Where I = moment of inertia

$$I = (30)(4)^2 + (20)(6)^2$$

$$= 1200 \text{ gm-cm}^2$$

$$= 1.2 \times 10^{-4} \text{ kg-m}^2$$

$$\Rightarrow \omega = \sqrt{\frac{1.2 \times 10^{-8}}{1.2 \times 10^{-4}}}$$

$$\Rightarrow \omega = \sqrt{10^{-4}}$$

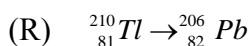
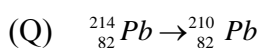
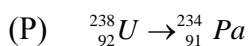
$$\omega = (10^{-2})$$

$$n \times 10^{-3} = 10^{-2} \Rightarrow n = 10$$

SECTION-4 : (Maximum Marks : 12)

- This section contains **FOUR (04)** Matching List Sets.
- Each set has **ONE** Multiple Choice Question.
- Each set has **TWO** lists : **List-I** and **List-II**.
- **List-I** has **Four** entries (P), (Q), (R) and (S) and **List-II** has **Five** entries (1), (2), (3), (4) and (5).
- **FOUR** options are given in each Multiple Choice Question based on **List-I** and **List-II** and **ONLY ONE** of these four options satisfies the condition asked in the Multiple Choice Question.
- Answer to each question will be evaluated according to the following marking scheme:
Full Marks : +3 **ONLY** if the option corresponding to the correct combination is chosen;
Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);
Negative Marks : -1 In all other cases.

14. List-I shows different radioactive decay processes and List-II provides possible emitted particles. Match each entry in List-I with an appropriate entry from List-II, and choose the correct option.

List-I

List-II

 (1) one α particle and one β^+ particle

 (2) three β^- particles and one α particle

 (3) two β^- particles and one α particle

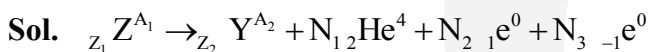
 (4) one α particle and one β^- particle

 (5) one α particle and two β^+ particles

 (A) $P \rightarrow 4, Q \rightarrow 3, R \rightarrow 2, S \rightarrow 1$

 (B) $P \rightarrow 4, Q \rightarrow 1, R \rightarrow 2, S \rightarrow 5$

 (C) $P \rightarrow 5, Q \rightarrow 3, R \rightarrow 1, S \rightarrow 4$

 (D) $P \rightarrow 5, Q \rightarrow 1, R \rightarrow 3, S \rightarrow 2$
Ans. (A)


Conservation of charge

$$Z_1 = Z_2 + 2N_1 + N_2 - N_3 \quad \dots \text{(i)}$$

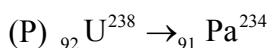
Conservation of nucleons.

$$A_1 = A_2 + 4N_1$$

$$N_1 = \frac{A_1 - A_2}{4} \quad \dots \text{(ii)}$$

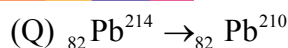
From (i) and (ii)

$$N_2 - N_3 = Z_1 - Z_2 - \left(\frac{A_1 - A_2}{2} \right)$$



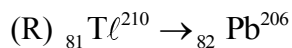
$$N_1 = \frac{238 - 234}{4} = 1 \rightarrow 1\alpha$$

$$N_2 - N_3 = (92 - 91) - \left(\frac{4}{2} \right) = -1 \rightarrow 1\beta^-$$



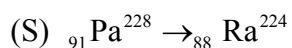
$$N_1 = \frac{214 - 210}{4} = 1 \rightarrow 1\alpha$$

$$N_2 - N_3 = (82 - 82) - \left(\frac{4}{2}\right) = -2 \rightarrow 2\beta^-$$



$$N_1 = \frac{210 - 206}{4} = 1 \rightarrow 1\alpha$$

$$N_2 - N_3 = (81 - 83) - \frac{4}{2} = -3 \rightarrow 3\beta^-$$



$$N_1 = \frac{228 - 224}{4} = 1\alpha$$

$$N_2 - N_3 = (91 - 88) - \frac{4}{2} = 1\beta^+$$

15. Match the temperature of a black body given in List-I with an appropriate statement in List-II, and choose the correct option.

[Given: Wien's constant as 2.9×10^{-3} m-K and $\frac{hc}{e} = 1.24 \times 10^{-6}$ V-m]

List-I

(P) 2000 K

(Q) 3000 K

(R) 5000 K

(S) 10000 K

List-II

- (1) The radiation at peak wavelength can lead to emission of photoelectrons from a metal of work function 4 eV
- (2) The radiation at peak wavelength is visible to human eye.
- (3) The radiation at peak emission wavelength will result in the widest central maximum of a single slit diffraction.
- (4) The power emitted per unit area is 1/16 of that emitted by a blackbody at temperature 6000 K.
- (5) The radiation at peak emission wavelength can be used to image human bones.

(A) $P \rightarrow 3, Q \rightarrow 5, R \rightarrow 2, S \rightarrow 3$

(B) $P \rightarrow 3, Q \rightarrow 2, R \rightarrow 4, S \rightarrow 1$

(C) $P \rightarrow 3, Q \rightarrow 4, R \rightarrow 2, S \rightarrow 1$

(D) $P \rightarrow 1, Q \rightarrow 2, R \rightarrow 5, S \rightarrow 3$

Ans. (C)

Sol. \Rightarrow For option (P) temperature is minimum hence λ_m will be maximum $\beta = \frac{\lambda D}{d} \Rightarrow \beta$ will also be

maximum

\Rightarrow For option (Q) $T = 3000$

$$\lambda_m = \frac{b}{T} = \frac{2.9 \times 10^{-3}}{30000}$$

$$\lambda_m = \frac{2.9}{3} \times 10^{-6}$$

$$= 0.96 \times 10^{-6}$$

$$= 966.6 \text{ nm}$$

$$P_{3000} = 6A (3000)^4$$

$$P_{6000} = 6A (6000)^4$$

$$\frac{P_{3000}}{P_{6000}} = \left(\frac{1}{2}\right)^4 = \frac{1}{16}$$

$$P_{3000} = \frac{1}{16} P_{6000}$$

Q – 4

\Rightarrow For (R) $T = 5000 \text{ K}$

$$\lambda_m = \frac{2.9 \times 10^{-3}}{5 \times 10^3} = 0.58 \times 10^{-6}$$

$$= 580 \text{ nm}$$

Visible to human eyes

R – 2

\Rightarrow For (S) $T = 10,000 \rightarrow$ maximum

Hence (3) is wrong as it has minimum (λ_m)

- 16.** A series LCR circuit is connected to a $45 \sin(\omega t)$ Volt source. The resonant angular frequency of the circuit is 10^5 rad s^{-1} and current amplitude at resonance is I_0 . When the angular frequency of the source is $\omega = 8 \times 10^4 \text{ rad s}^{-1}$, the current amplitude in the circuit is $0.05 I_0$. If $L = 50 \text{ mH}$, match each entry in List-I with an appropriate value from List-II and choose the correct option.

List-I

- (P) I_0 in mA
 (Q) The quality factor of the circuit
 (R) The bandwidth of the circuit in rad s^{-1}
 (S) The peak power dissipated at resonance in Watt

List-II

- (1) 44.4
 (2) 18
 (3) 400
 (4) 2250
 (5) 500

(A) $P \rightarrow 2, Q \rightarrow 3, R \rightarrow 5, S \rightarrow 1$

(B) $P \rightarrow 3, Q \rightarrow 1, R \rightarrow 4, S \rightarrow 2$

(C) $P \rightarrow 4, Q \rightarrow 5, R \rightarrow 3, S \rightarrow 1$

(D) $P \rightarrow 4, Q \rightarrow 2, R \rightarrow 1, S \rightarrow 5$

Ans. (B)

Sol. $V = 45 \sin \omega t$, $L = 50 \text{ mH}$

$$\omega_0 = 10^5 \text{ rad/s} = \frac{1}{\sqrt{LC}} \Rightarrow C = \frac{1}{L\omega_0^2} = \frac{1}{5 \times 10^{-2} \times 10^{10}}$$

$$= 2 \times 10^{-9} \text{ F}$$

$$I_0 = \frac{45}{R}$$

$$\omega = 8 \times 10^4 \text{ rad/s} = 0.8 \omega_0$$

$$I = 0.05 I_0 = \frac{I_0}{20} \Rightarrow Z = 20R$$

$$X_L = 8 \times 10^4 \times 5 \times 10^{-2} \Omega = 4 \text{ k}\Omega$$

$$X_C = \frac{1}{8 \times 10^4 \times 2 \times 10^{-9}} = \frac{1}{16} \times 10^5 \Omega = \frac{25}{4} \text{ k}\Omega$$

$$Z^2 = R^2 + (X_C - X_L)^2$$

$$400R^2 = R^2 + \left(\frac{9}{4} \text{ k}\Omega\right)^2$$

$$R = \frac{\frac{9}{4} \text{ k}\Omega}{\sqrt{399}} \approx \frac{9}{80} \text{ k}\Omega = \frac{900}{8} \Omega$$

$$I_0 = \frac{V_0}{R} = \frac{45 \times 8}{900} = \frac{8}{20} \text{ A} \approx 0.4 \text{ A} = 400 \text{ mA}$$

$$Q = \frac{1}{R} \sqrt{\frac{L}{C}} = \frac{8}{900} \sqrt{\frac{5 \times 10^{-2}}{2 \times 10^{-9}}} = \frac{8}{900} \sqrt{25 \times 10^6}$$

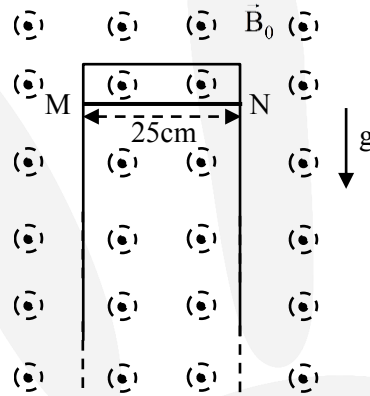
$$Q = \frac{8}{900} \times 5000 = 44.4$$

$$Q = \frac{\omega_0}{\Delta\omega} \Rightarrow \Delta\omega = \frac{\omega_0}{Q} = \frac{10^5}{44.4} = 2250.0$$

$$P_{\max} = I_0^2 R = \frac{45^2}{R^2} \times R = \frac{45^2}{R} = \frac{45^2}{900} \times 8 = 18.4 \text{ W}$$

17. A thin conducting rod MN of mass 20 gm, length 25 cm and resistance 10Ω is held on frictionless, long, perfectly conducting vertical rails as shown in the figure. There is a uniform magnetic field $B_0 = 4 \text{ T}$ directed perpendicular to the plane of the rod-rail arrangement. The rod is released from rest at time $t = 0$ and it moves down along the rails. Assume air drag is negligible. Match each quantity in List-I with an appropriate value from List-II, and choose the correct option.

[Given: The acceleration due to gravity $g = 10 \text{ ms}^{-2}$ and $e^{-1} = 0.4$]



List-I

List-II

- | | | |
|--|-----|------|
| (P) At $t = 0.2 \text{ s}$, the magnitude of the induced emf in Volt | (1) | 0.07 |
| (Q) At $t = 0.2 \text{ s}$, the magnitude of the magnetic force in Newton | (2) | 0.14 |
| (R) At $t = 0.2 \text{ s}$, the power dissipated as heat in Watt | (3) | 1.20 |
| (S) The magnitude of terminal velocity of the rod in m s^{-1} | (4) | 0.12 |
| | (5) | 2.00 |

(A) $P \rightarrow 5, Q \rightarrow 2, R \rightarrow 3, S \rightarrow 1$

(B) $P \rightarrow 3, Q \rightarrow 1, R \rightarrow 4, S \rightarrow 5$

(C) $P \rightarrow 4, Q \rightarrow 3, R \rightarrow 1, S \rightarrow 2$

(D) $P \rightarrow 3, Q \rightarrow 4, R \rightarrow 2, S \rightarrow 5$

Ans. (D)

Sol. From force equation

$$mg - Bi\ell = \frac{mdv}{dt}$$

$$mg - \frac{BBi\ell}{R} \times \ell = \frac{mdv}{dt}$$

$$\frac{mgR}{B^2\ell^2} - v = \frac{mR}{B^2\ell^2} \frac{dv}{dt}$$

$$\frac{B^2\ell^2}{mR} \int_{t=0}^t dt = \int_0^v \frac{dv}{\left(\frac{mgR}{B^2\ell^2} - v\right)}$$

$$\text{Now } \frac{mgR}{B^2 \ell^2} = \frac{20 \times 10^{-3} \times 10 \times 10}{16 \times \frac{1}{16}} = 2$$

$$\text{And } \frac{B^2 \ell^2}{mR} = \frac{16 \times \frac{1}{16}}{20 \times 10^{-3} \times 10} = \frac{1}{0.2} = 5$$

$$\therefore 5t = \left[-\ln(2-v) \right]_0^v$$

$$-5t = \ln \left[\frac{2-v}{v} \right]$$

$$\therefore v = 2(1 - e^{-5t})$$

$$\text{At } t = 0.2 \text{ sec} \quad v = 2(1 - e^{-5 \times 0.2})$$

$$v = 2(1 - 0.4)$$

$$v = 1.2 \text{ m/s}$$

(P) Now at $t = 0.2$ sec

The magnitude of the induced emf = $E = Bv\ell$

$$= 4 \times 1.2 \times \frac{1}{4} = 1.2 \text{ Volt}$$

(Q) At $t = 0.2$ sec, the magnitude of magnetic force = $BI\ell \sin\theta$

$$= B \times \frac{B\ell v}{R} \times \ell \times \sin 90^\circ$$

$$= \frac{4 \times 4 \times \frac{1}{4} \times 1.3 \times \frac{1}{4}}{10} = 0.12 \text{ Newton}$$

(R) At $t = 0.2$ sec, the power dissipated as heat

$$P = i^2 R = \frac{v^2}{R} = \frac{1.2 \times 1.2}{10}$$

$$P = 0.144 \text{ watt}$$

(S) Magnitude of terminal velocity

At terminal velocity, the net force become zero

$$\therefore mg = Bi\ell$$

$$mg = B \times \frac{B\ell v_t}{R} \times \ell$$

$$\therefore v_T = \frac{mgR}{B^2 \ell^2} = \frac{20 \times 10^{-3} \times 10 \times 10}{16 \times \frac{1}{16}}$$

$$v_T = 2 \text{ m/s}$$

Hence, Answer is (D)