



FINAL JEE–MAIN EXAMINATION – APRIL, 2023
Held On Tuesday 11th April, 2023
TIME : 09:00 AM to 12:00 PM

SECTION - A

- 31.** The radii of two planets 'A' and 'B' are 'R' and '4R' and their densities are ρ and $\rho/3$ respectively. The ratio of acceleration due to gravity at their surfaces ($g_A : g_B$) will be :
 (1) 1 : 16 (2) 3 : 16 (3) 3 : 4 (4) 4 : 3

Sol. (3)

$$g = \frac{4\pi}{3} GR\delta$$

$$g \propto \delta R$$

$$\frac{g_A}{g_B} = \frac{\delta_A R_A}{\delta_B R_B} = \frac{\delta \cdot R}{\frac{\delta}{3} \cdot 4R} = \frac{3}{4}$$

- 32.** A coin placed on a rotating table just slips when it is placed at a distance of 1 cm from the center. If the angular velocity of the table is halved, it will just slip when placed at a distance of _____ from the centre :
 (1) 8 cm (2) 4 cm (3) 2 cm (4) 1 cm

Sol. (2)

$$fr = m\omega^2 r$$

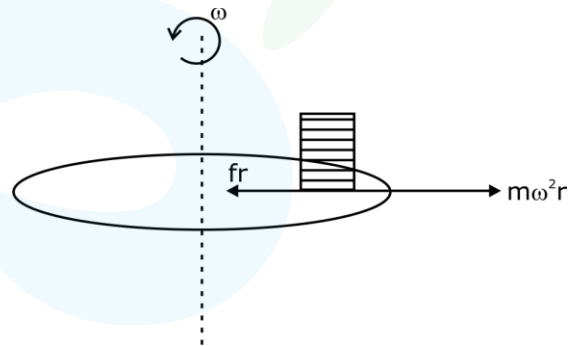
$$\mu mg = m\omega^2 r = \text{const.}$$

$$\omega^2 r = \text{const}$$

$$\omega_1^2 r_1 = \omega_2^2 r_2$$

$$\omega^2 (1) = \left(\frac{\omega}{2}\right)^2 r_2$$

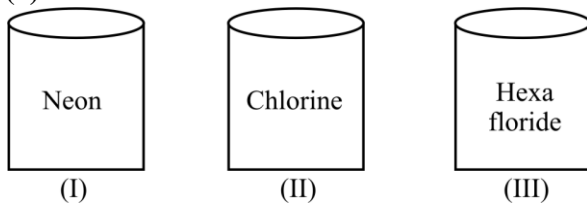
$$r_2 = 4\text{cm}$$



- 33.** Three vessels of equal volume contain gases at the same temperature and pressure. The first vessel contains neon (monoatomic), the second contains chlorine (diatomic) and third contains uranium hexafluoride (polyatomic). Arrange these on the basis of their root mean square speed (v_{rms}) and choose the correct answer from the options given below :

- (1) $V_{rms}(\text{mono}) > v_{rms}(\text{dia}) > v_{rms}(\text{poly})$ (2) $V_{rms}(\text{dia}) < v_{rms}(\text{poly}) < v_{rms}(\text{mono})$
 (3) $V_{rms}(\text{mono}) < v_{rms}(\text{dia}) < v_{rms}(\text{poly})$ (4) $V_{rms}(\text{mono}) = v_{rms}(\text{dia}) = v_{rms}(\text{poly})$

Sol. (1)



$$V_{RMS} = \sqrt{\frac{\gamma RT}{m}} \quad \dots(1)$$

$$\gamma = 1 + \frac{2}{f} \quad \text{SO } \gamma_{\text{monochromic}} > \gamma_{\text{diatomic}} > \gamma_{\text{poly.}}$$

$$V_{\text{mono}} > V_{\text{diatomic}} > V_{\text{poly.}} \quad \text{Ans.(1)}$$

- 34.** Two radioactive elements A and B initially have same number of atoms. The half life of A is same as the average life of B. If λ_A and λ_B are decay constants of A and B respectively, then choose the correct relation from the given options.

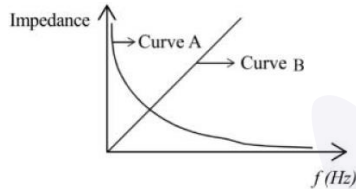
- (1) $\lambda_A = 2\lambda_B$ (2) $\lambda_A = \lambda_B$ (3) $\lambda_A \ln 2 = \lambda_B$ (4) $\lambda_A = \lambda_B \ln 2$

Sol. (4)

	A	B	T → half life
t = 0	N ₀	N ₀	τ → ang life
T _A = τ _B	→		given in question

Now $\frac{\ln(2)}{\lambda_A} = \frac{1}{\lambda_B} \Rightarrow \lambda_A = \lambda_B \cdot \ln(2)$

35.



As per the given graph, choose the correct representation for curve A and curve B.

{ Where X_C = reactance of pure capacitive circuit connected with A.C. source

X_L = reactance of pure inductive circuit connected with A.C. source

R = impedance of pure resistive circuit connected with A.C. source.

Z = impedance of the LCR series circuit }

- (1) A = X_L, B = R (2) A = X_L, B = Z (3) A = X_C, B = R (4) A = X_C, B = X_L

Sol. (4)

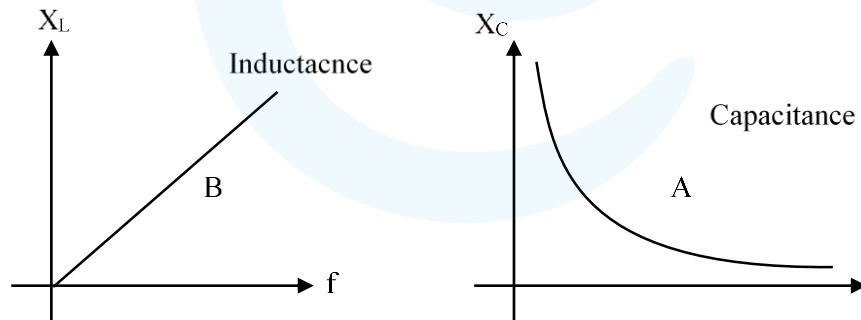
$$X_L = \omega L = 2\pi fL$$

$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi fC}$$

$$R = \text{const.}$$

$$A \rightarrow X_C$$

$$B \rightarrow X_L$$



36. A transmitting antenna is kept on the surface of the earth. The minimum height of receiving antenna required to receive the signal in line of sight at 4 km distance from it is $x \times 10^{-2}$ m. The value of x is _____.

(Let, radius of earth R = 6400 km)

- (1) 125 (2) 12.5 (3) 1250 (4) 1.25

Sol. (1)

$$d = \sqrt{2R \cdot h}$$

$$d^2 = 2Rh$$

$$(4)^2 = 2 \times 6400 \times h$$

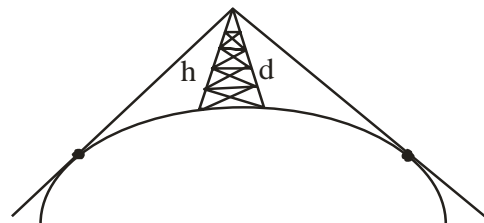
$$\frac{16}{2 \times 6400} = h = \frac{1}{800} \text{ km}$$

$$h = \frac{1000}{800} = \frac{5}{4} \text{ m}$$

$$x \times 10^{-2} = \frac{5}{4}$$

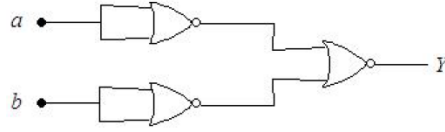
$$x = \frac{500}{4} = 125$$

Ans. Option → (1)





37. The logic performed by the circuit shown in figure is equivalent to :



- (1) NAND (2) NOR (3) AND (4) OR

Sol. (3)

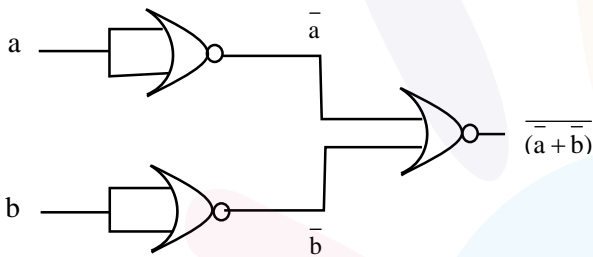
$$Y = \overline{\overline{a + b}}$$

$$Y = \overline{\overline{a \cdot b}}$$

$$\boxed{Y = a \cdot b}$$

Ans. → AND gate

Option → 3



38. The electric field in an electromagnetic wave is given as

$$\vec{E} = 20 \sin \omega \left(t - \frac{x}{c} \right) \hat{j} \text{ NC}^{-1}$$

where ω and c are angular frequency and velocity of electromagnetic wave respectively. the energy contained in a volume of $5 \times 10^{-4} \text{ m}^3$ will be (Given $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2 / \text{Nm}^2$)

- (1) $88.5 \times 10^{-13} \text{ J}$ (2) $17.7 \times 10^{-13} \text{ J}$ (3) $8.85 \times 10^{-13} \text{ J}$ (4) $28.5 \times 10^{-13} \text{ J}$

Sol. (3)

$$\vec{E} = 20 \sin \omega \left[t - \frac{x}{c} \right]$$

$E_0 = 20$

$$\text{Energy density} = \frac{1}{2} \epsilon_0 E_0^2$$

$$= \frac{1}{2} \times 8.85 \times 10^{-12} \times 400$$

$$= 200 \times 8.85 \times 10^{-12} \times 5 \times 10^{-4}$$

$$= 8.85 \times 10^{-12} \times 10^{-4} \times 1000$$

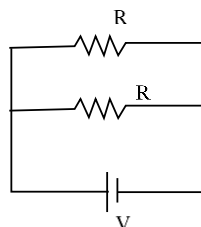
$$\text{Energy} = 8.85 \times 10^{-13} \text{ J} \qquad \text{option} \rightarrow (1)$$

39. Two identical heater filaments are connected first in parallel and then in series. At the same applied voltage, the ratio of heat produced in same time for parallel to series will be :

- (1) 1 : 2 (2) 4 : 1 (3) 1 : 4 (4) 2 : 1

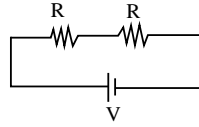
Sol. (2)

$$H_1 = \frac{V^2}{(R/2)} t = \frac{2V^2}{R} \dots \dots \dots (1)$$





$$H_2 = \frac{V^2}{2R} t \quad \dots\dots\dots (2)$$

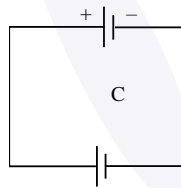


$$\frac{H_1}{H_2} = \left(\frac{2V^2 t}{R} \right) \times \frac{2R}{V^2 t} = \frac{4}{1}$$

- 40.** A parallel plate capacitor of capacitance 2 F is charged to a potential V, The energy stored in the capacitor is E_1 . The capacitor is now connected to another uncharged identical capacitor in parallel combination. The energy stored in the combination is E_2 . The ratio E_2/E_1 is :
- (1) 2 : 3 (2) 1 : 2 (3) 1 : 4 (4) 2 : 1

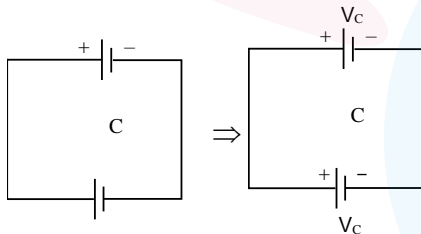
Sol. (4)

$$C = 2F$$



$$E_1 = \frac{1}{2} CV^2 \quad \dots\dots\dots (1)$$

Now



$$V_c = \frac{C_1 V_1 + C_2 V_2}{C_1 + C_2}$$

$$V_c = \frac{CV + 0}{2C} = \frac{V}{2}$$

$$E_2 = CV_c^2 = C \cdot \frac{V^2}{4} \quad \dots\dots\dots (2)$$

$$\frac{E_2}{E_1} = \frac{\left(\frac{CV^2}{4} \right)}{\left(\frac{CV^2}{2} \right)} = \frac{2}{1} \quad \text{option} \rightarrow (4)$$

- 41.** An average force of 125 N is applied on a machine gun firing bullets each of mass 10 g at the speed of 250 m/s to keep it in position. The number of bullets fired per second by the machine gun is :
- (1) 25 (2) 5 (3) 100 (4) 50

Sol. (4)

$$F = 125N$$

$$F = \frac{dp}{dt} \quad n \rightarrow \text{No. of bullets}$$

$$F = \frac{d(nmv)}{dt} = mv \frac{dn}{dt}$$

$$125 = \frac{10n}{1000} \times 250 \times \frac{dn}{dt}$$

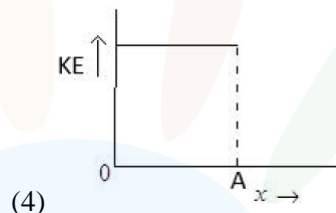
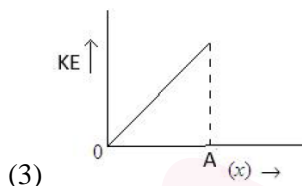
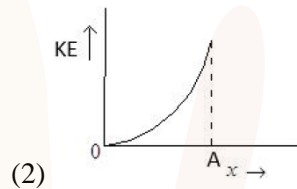
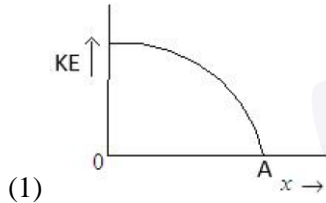


$$\frac{125 \times 1000}{2500} = \frac{dn}{dt}$$

$$\frac{dn}{dt} = 50$$

option \rightarrow (4)

42. The variation of kinetic energy (KE) of a particle executing simple harmonic motion with the displacement (x) starting from mean position to extreme position (A) is given by



Sol.

(1)

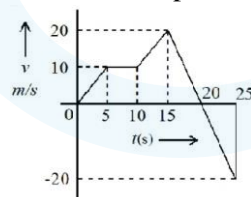
$$K \cdot E = T \cdot E - P \cdot E$$

$$K \cdot E = \frac{1}{2} KA^2 - \frac{1}{2} Kx^2$$

Graph b/w $K \cdot E$ and x will be parabola

Option \rightarrow (1)

43. From the $v - t$ graph shown, the ratio of distance to displacement in 25 s of motion is :



(1) $\frac{3}{5}$

(2) $\frac{1}{2}$

(3) $\frac{5}{3}$

(4) 1

Sol.

(3)

Displacement = Area of graph with sign

$$\text{Displacement} = \left(\frac{1}{2} \times 10 \times 5 \right) + (10 \times 5) + \left(\frac{1}{2} \times 5 \times 30 \right) + \left(\frac{1}{2} \times 5 \times 20 \right) - \frac{1}{2} (5)(20)$$

$$= 25 + 50 + 75 + 50 - 50$$

$$= 150 \text{ m}$$

Distance \rightarrow Area of graph with positive value

$$\text{Distance} = 25 + 50 + 75 + 50 = 250$$

$$\frac{\text{Distance}}{\text{Displacement}} = \frac{250}{150} = \frac{5}{3}$$

option \rightarrow (3)

44. On a temperature scale 'X', the boiling point of water is $65^\circ X$ and the freezing point is $-15^\circ X$. Assume that the X scale is linear. The equivalent temperature corresponding to $-95^\circ X$ on the Fahrenheit scale would be :

(1) $-63^\circ F$

(2) $-148^\circ F$

(3) $-48^\circ F$

(4) $-112^\circ F$



Sol. (3)

$$\frac{X_T - X_L}{X_H - X_L} = \frac{T_F - 32}{212 - 32}$$

$$\frac{-95^\circ - (-15^\circ)}{65^\circ - (-15^\circ)} = \frac{T_F - 32}{180}$$

$$\frac{-80^\circ}{80^\circ} = \frac{T_F - 32}{180^\circ}$$

$$-180 = T_F - 32$$

$$T_F = -180 + 32 = -148^\circ \text{ F}$$

Ans. option → (2)

45. The free space inside a current carrying toroid is filled with a material of susceptibility 2×10^{-2} . The percentage increase in the value of magnetic field inside the toroid will be
 (1) 0.2% (2) 1% (3) 2% (4) 0.1%

Sol. (3)

$$X = 2 \times 10^{-2}$$

$$\mu_r = 1 + X = 1 + 0.02 = 1.02$$

$B_0 \rightarrow$ magnetic field due to magnetic material
 $B_m \rightarrow$ magnetic field due to magnetic material
 $B_m = \mu_r B_0$

$$\Delta B = \frac{B_m - B_0}{B_0} \times 100 = \frac{\mu_r B_0 - B_0}{B_0} \times 100$$

$$\Delta B\% = \frac{(X+1)-1}{1} \times 100 = X \times 100$$

$$\Delta B\% = 2 \times 10^{-2} \times 100 = 2\%$$

Ans. Option (3)

46. The critical angle for a denser-rarer interface is 45° . The speed of light in rarer medium is 3×10^8 m/s. The speed of light in the denser medium is :
 (1) 2.12×10^8 m/s (2) 5×10^7 m/s (3) 3.12×10^7 m/s (4) $\sqrt{2} \times 10^8$ m/s

Sol. (1)

$$\sin i_c = \frac{\mu_r}{\mu_d} \Rightarrow \sin 45^\circ = \frac{\mu_r}{\mu_d}$$

$$\Rightarrow \frac{\mu_r}{\mu_d} = \frac{1}{\sqrt{2}} \dots\dots\dots(1)$$

We know

$$V \propto \frac{1}{\mu} \Rightarrow \frac{V_d}{V_r} = \frac{\mu_r}{\mu_d}$$

$$= \frac{V_d}{3 \times 10^8} = \frac{1}{\sqrt{2}}$$

$$V_d = \frac{3}{\sqrt{2}} \times 10^8 = 3 \times 0.7 \times 10^8$$

$$\boxed{V_d = 2.12 \times 10^8 \text{ m/sec}}$$

Ans. Option (1)

47. Given below are two statements :
 Statements I : Astronomical unit (Au), Parsec (Pc) and Light year (ly) are units for measuring astronomical distances.
 Statements II : Au < Parsec (Pc) < ly
 In the light of the above statements, choose the most appropriate answer from the options given below :
 (1) Both Statements I and Statements II are incorrect.
 (2) Both Statements I and Statements II are correct.
 (3) Statements I is incorrect but Statements II are correct.
 (4) Statements I is correct but Statements II are incorrect.



Sol. (4)
 A.V., Par sec and light year are the unit of distance
 Light year → distance travelled by light in one year
 $1 \text{ ly} = 9.5 \times 10^{15} \text{ m}$
 parcec = 3.262 light year
 $\text{A.V.} = 1.58 \times 10^{-5} \text{ light year}$
 $\text{A.V.} < 1 \text{ y} < \text{Parsec.}$
 Statement I correct and statement II incorrect.

48. The current sensitivity of moving coil galvanometer is increased by 25%. This increase is achieved only by changing in the number of turns of coils and area of cross section of the wire while keeping the resistance of galvanometer coil constant. The percentage change in the voltage sensitivity will be :
 (1) +25% (2) -25% (3) -50% (4) Zero

Sol. (1)
 $\tau = mB$ $A = \text{area of coil}$
 $K\theta = IANB$ $B = \text{magnetic field}$
 $\frac{\theta}{I} = \frac{ANB}{K}$ Current sensitivity
 $1.25 \left(\frac{\theta}{I}\right)_2 = \left(\frac{\theta}{I}\right)_1$ (1)
 $1.25 \left[\frac{AN_2B}{K}\right] = \left[\frac{AN_1B}{K}\right]$
 $1.25 = \frac{N_1}{N_2} = \frac{5}{4}$ (2)
 $\Rightarrow R = \frac{\delta l}{a} = \text{const.}$
 $\Rightarrow l = a$
 Voltage sensitivity = $\frac{\theta}{V} = \frac{\theta}{IR} = \frac{\text{Current sensitivity}}{R}$
 $R = \text{constant}$
 Voltage sensitivity \propto current sensitivity

Ans. option → (A)

49. A metallic surface is illuminated with radiation of wavelength λ , the stopping potential is V_0 . If the same surface is illuminated with radiation of wavelength 2λ , the stopping potential becomes $\frac{V_0}{4}$. The threshold wavelength for this metallic surface will be

- (1) $\frac{3}{2}\lambda$ (2) 4λ (3) 3λ (4) $\frac{\lambda}{4}$

Sol. (3)
 $E = \text{K.E} + \phi_0$
 Now
 $\frac{hc}{\lambda} = eV_0 + \phi_0$ (1)
 And $\frac{hc}{2\lambda} = \frac{eV_0}{4} + \phi_0$ (2)
 (2) $\times 4$ (1)
 $\frac{2hc}{\lambda} - \frac{hc}{\lambda} = 0 + (4\phi_0 - \phi_0)$

$$\frac{hc}{\lambda} = 3\phi_0$$

$$\frac{hc}{\lambda} = 3 \frac{hc}{\lambda_0}$$

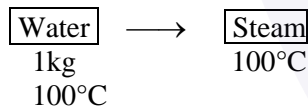
$$\lambda_0 = 3\lambda$$

50. 1 kg of water at 100°C is converted into steam at 100°C by boiling at atmospheric pressure. The volume of water changes from $1.00 \times 10^{-3} \text{ m}^3$ as a liquid to 1.671 m^3 as steam. The change in internal energy of the system during the process will be

(Given latent heat of vaporisation = 2257 kJ/kg, Atmospheric pressure = $1 \times 10^5 \text{ Pa}$)

- (1) +2476 kJ (2) -2426 kJ (3) -2090 kJ (4) +2090 kJ

Sol. (4)



Change in volume at constant pressure and temp →

$$\Delta V = V_2 - V_1 = 1.671 - 0.001$$

$$\Delta V = 1.67 \text{ m}^3 \quad \dots\dots (1)$$

$$\Delta Q = \Delta U + w$$

$$mL_v = \Delta U + (1.013 \times 10^5) (1.67)$$

$$\Delta U = (2257 - 170)10^3$$

$$\Delta U = 2090 \text{ kJ (approx.)}$$

Ans. Option → 4

51. The radius of curvature of each surface of a convex lens having refractive index 1.8 is 20 cm. The lens is now immersed in a liquid of refractive index 1.5. The ratio of power of lens in air to its power in the liquid will be x : 1. The value of x is _____

Sol. (4)

$$\frac{1}{f} = \left(\frac{\mu_l}{\mu_m} - 1 \right) \left(\frac{1}{R} - \frac{1}{-R} \right)$$

$$P_1 = \frac{2}{R} \left(\frac{1.8}{1} - 1 \right)$$

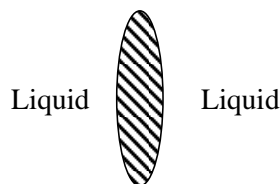
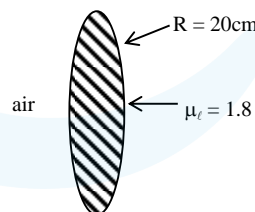
$$P_1 = \frac{2}{R} (0.8) = \frac{1.6}{R} \quad \dots (1)$$

Now,

$$P_2 = \frac{2}{R} \left[\frac{1.8}{1.5} - 1 \right]$$

$$P_2 = \frac{2}{R} \left[\frac{0.3}{1.5} \right] = \frac{2}{R} \times \frac{1}{5} = \frac{2}{5R}$$

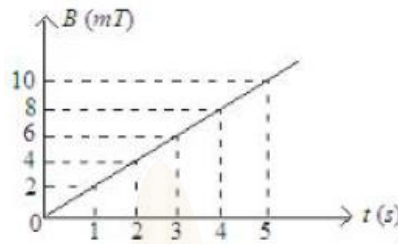
$$\frac{P_{\text{air}}}{P_{\text{liquid}}} = \frac{P_1}{P_2} = \frac{\left(\frac{1.6}{R} \right)}{\left(\frac{0.4}{R} \right)} = \frac{4}{1}$$



Ans. → 4



52. The magnetic field B crossing normally a square metallic plate of area 4 m^2 is changing with time as shown in figure. The magnitude of induced emf in the plate during $t = 2 \text{ s}$ to $t = 4 \text{ s}$, is _____ mV.



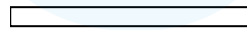
Sol. (8)

$$\begin{aligned} \text{emf} &= \frac{d\phi}{dt} \\ \text{Emf} &= \frac{dBA}{dt} = \frac{AdB}{dt} \\ \text{Emf} &= 4 \cdot \text{Slope of } B.t \text{ curve} \\ &= 4 \cdot \left[\frac{8-4}{4-2} \right] = 4 \times 2 \\ \boxed{\text{Emf} = 8 \text{ Volt}} \end{aligned}$$

53. The length of a wire becomes l_1 and l_2 when 100 N and 120 N tensions are applied respectively. If $10 l_2 = 11 l_1$, the natural length of wire will be $\frac{1}{x} l_1$. Here the value of x is _____.

Sol. (2)

$$F = kx$$



$l_0 = \text{natural length}$

$$F = \frac{YA}{l_0} \cdot x.$$

Sol when $F = 100 \text{ N}$

$$100 = k(l_1 - l_0) \quad \dots (1)$$

When $F = 120 \text{ N}$

$$120 = K((l_1 - l_0))$$

$$\text{Given that } 10l_2 = 11l_1$$

$$l_2 = 1.1 l_1$$

$$\text{So } 120 = K(1.1l_1 - l_0) \quad \dots (2)$$

Now (2)/(1)

$$\frac{120}{100} = \frac{K(1.1l_1 - l_0)}{K(l_1 - l_0)}$$

$$1.2 = \frac{1.1l_1 - l_0}{l_1 - l_0}$$

$$1.2l_1 - 1.2l_0 = 1.1l_1 - l_0$$

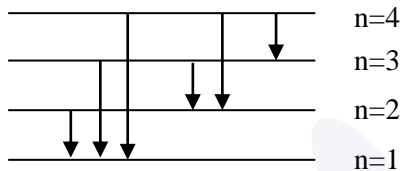
$$0.1l_1 = 0.2l_0$$

$$l_0 = \frac{l_1}{2} \text{ So } \boxed{x = 2} \text{ Ans.}$$

54. A monochromatic light is incident on a hydrogen sample in ground state. Hydrogen atoms absorb a fraction of light and subsequently emit radiation of six different wavelengths. The frequency of incident light is $x \times 10^{15}$ Hz. The value of x is _____.

(Given $h = 4.25 \times 10^{-15}$ eVs)

Sol. (3)



Total emission lines = 6 (given)

So electron absorbed energy and jump from $n = 1$ to $n = 4$

$$\Delta E = 13.6 \left[\frac{1}{1^2} - \frac{1}{4^2} \right] \text{ eV}$$

$$= 13.6 \left[1 - \frac{1}{16} \right] \text{ eV}$$

$$\Delta E = hf$$

$$12.75 = 4.25 \times 10^{-15} f$$

$$f = \frac{12.75}{4.25} \times 10^{15} = 3 \times 10^{15} \text{ Hz}$$

$x = 3$ Ans.

55. A force $\vec{F} = (2 + 3x)\hat{i}$ acts on a particle in the x direction where F is in newton and x is in meter. The work done by this force during a displacement from $x = 0$ to $x = 4$ m, is _____ J.

Sol. (32)

$$\vec{F} = (2 + 3x)\hat{i}$$

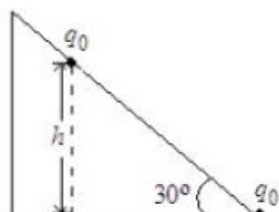
$$w = \int_0^4 F \cdot dx = \int_0^4 (2 + 3x) \cdot dx$$

$$w = \left(2x + \frac{3x^2}{2} \right) \Big|_0^4 = (8 + 24)$$

$w = 32\text{J}$

56. As shown in the figure, a configuration of two equal point charges ($q_0 = +2 \mu\text{C}$) is placed on an inclined plane. Mass of each point charge is 20 g. Assume that there is no friction between charge and plane. For the system of two point charges to be in equilibrium (at rest) the height $h = x \times 10^{-3}$ m. The value of x is _____.

(Take $\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ N m}^2 \text{ C}^{-2}$, $g = 10 \text{ ms}^{-2}$)



Sol. (300)

Point charge on equilibrium is at rest.

So $F_e = mg \sin \theta$

$$\frac{kq_0 \cdot q_0}{r^2} = mg \sin 30^\circ$$

$$\frac{kq_0^2}{\left(\frac{h}{\sin 30^\circ}\right)^2} = \frac{mg}{2}$$

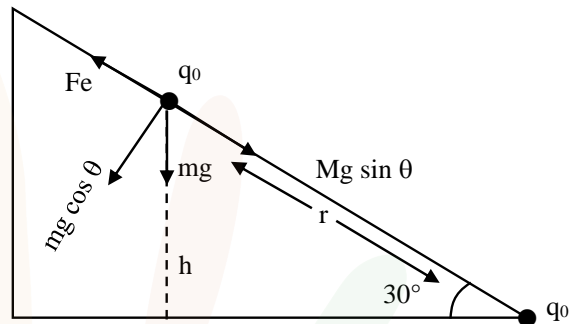
$$\frac{9 \times 10^9 \times (2 \times 10^{-6})^2}{4h^2} = \frac{20 \times 10^{-3} \times 10}{2}$$

$$\frac{9 \times 4 \times 10^9 \times 10^{-12}}{4h^2} = 10^{-1}$$

$$h^2 = 9 \times 10^{-2}$$

$$h = 0.3 \text{ m} = 300 \times 10^{-3} \text{ m}$$

x = 300 Ans.



57. A solid sphere of mass 500 g and radius 5 cm is rotated about one of its diameter with angular speed of 10 rad s⁻¹. If the moment of inertia of the sphere about its tangent is $x \times 10^{-2}$ times its angular momentum about the diameter. Then the value of x will be _____.

Sol. (35)

$$I_1 = \frac{2}{5} mR^2$$

$$I_2 = \frac{2}{5} mR^2 + mR^2 = \frac{7}{5} mR^2$$

Angular moment about diameter is

$$L_{com} = I_1 \omega = \frac{2}{5} mR^2 \omega$$

Now,

$$\frac{I_2}{L_{com}} = \frac{\frac{7}{5} mR^2}{\frac{2}{5} mR^2 \omega} = \frac{7}{2} \omega$$

$$\frac{I_2}{L_{com}} = \frac{7}{2 \times 10} = \frac{7}{20}$$

$$\text{Now } \frac{7}{20} = x \times 10^{-2}$$

$$x = \frac{7}{20} \times 100$$

x = 35 Ans.

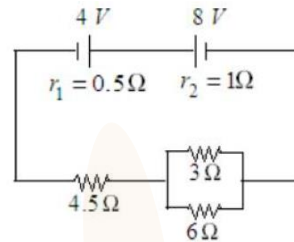
58. The equation of wave is given by $Y = 10^{-2} \sin 2\pi (160t - 0.5x + \pi/4)$ where x and Y are in m and t in s. The speed of the wave is _____ km h⁻¹.

Sol. (1152)

$$Y = 10^{-2} \sin 2\pi (160t - 0.5x + \pi/4)$$

$$\text{Speed of wave} = \frac{\omega}{k} = \frac{160}{0.5} = 320 \text{ m/sec} = 320 \times \frac{18}{5} = 1152 \text{ km/h} \quad \text{Ans.}$$

59. In the circuit diagram shown in figure given below, the current flowing through resistance $3\ \Omega$ is $\frac{x}{3}$ A. The value of x is _____



Sol. (1)

$$\text{Req.} = 0.5 + 1 + 4.5 + \left(\frac{3 \cdot 6}{9}\right)$$

$$\text{Req.} = 6 + 2 = 8\ \Omega$$

$$I = \frac{8 - 4}{8} = \frac{1}{2}\ \text{A} = 0.5\ \text{A}$$

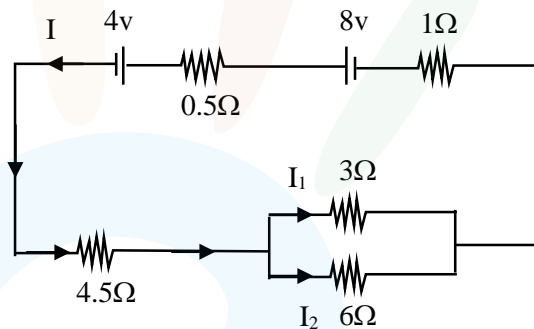
$$I_1 : I_2 = \frac{1}{3} : \frac{1}{6}$$

$$I_1 : I_2 = 2 : 1$$

$$\text{and } I_1 + I_2 = 0.5\ \text{A}$$

$$I_1 = \frac{2}{3} \times 0.5 = \frac{1}{3}\ \text{A}$$

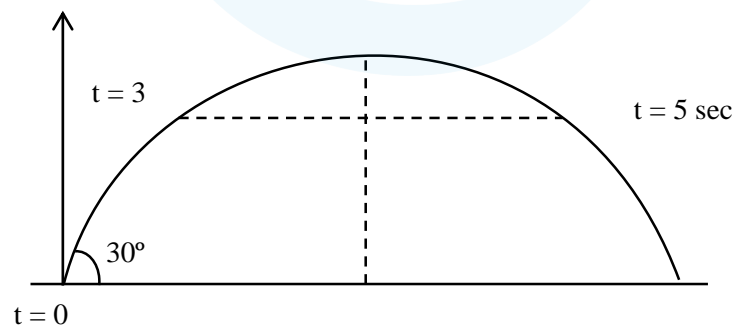
$$\text{So } \frac{1}{3} = \frac{x}{3} \Rightarrow \boxed{x = 1}$$



60. A projectile fired at 30° to the ground is observed to be at same height at time 3s and 5s after projection, during its flight. The speed of projection of the projectile is _____ ms^{-1} . (Given $g = 10\ \text{ms}^{-2}$)

Sol. (80)

$$\text{Time of flight} = 5 + 3 = 8\ \text{sec.}$$



$$\text{Now, } T = \frac{2u \sin \theta}{g}$$

$$8 = \frac{2u \cdot \sin 30^\circ}{10}$$

$$\Rightarrow \boxed{u = 80\ \text{m/sec}} \quad \text{Ans.}$$