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FINAL JEE-MAIN EXAMINATION - JULY, 2021 Held On Sunday 25th July, 2021 TIME: 3:00 PM to 06:00 PM

6.

7.

8.

9.

10.

SECTION-A

- The sum of all those terms which are rational 1. numbers in the expansion of $(2^{1/3} + 3^{1/4})^{12}$ is: (1) 89(2) 27(3) 35(4) 43Official Ans. by NTA (4)
- 2. The first of the two samples in a group has 100 items with mean 15 and standard deviation 3. If the whole group has 250 items with mean 15.6 and standard deviation $\sqrt{13.44}$, then the standard deviation of the second sample is :

$$(1) 8 (2) 6 (3) 4 (4) 5$$

Official Ans. by NTA (3)

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3. If
$$f(x) = \begin{cases} \int_{0}^{x} (5+|1-t|) dt, & x > 2\\ 5x+1, & x \le 2 \end{cases}$$
, then

(1) f(x) is not continuous at x = 2

- (2) f(x) is everywhere differentiable
- (3) f(x) is continuous but not differentiable at x = 2
- (4) f(x) is not differentiable at x = 1

Official Ans. by NTA (3)

4. If the greatest value of the term independent of 'x'

in the expansion of $\left(x\sin\alpha + a\frac{\cos\alpha}{x}\right)^{10}$ is $\frac{10!}{(5!)^2}$,

then the value of 'a' is equal to:

(1) - 1(2)1(3) - 2(4) 2Official Ans. by NTA (4)

- 5. Consider the statement "The match will be played only if the weather is good and ground is not wet". Select the correct negation from the following:
 - (1) The match will not be played and weather is not good and ground is wet.
 - (2) If the match will not be played, then either weather is not good or ground is wet.
 - (3) The match will be played and weather is not good or ground is wet.
 - (4) The match will not be played or weather is good and ground is not wet.

Official Ans. by NTA (3)

6. The value of
$$\cot \frac{\pi}{24}$$
 is:
(1) $\sqrt{2} + \sqrt{3} + 2 - \sqrt{6}$ (2) $\sqrt{2} + \sqrt{3} + 2 + \sqrt{6}$
(3) $\sqrt{2} - \sqrt{3} - 2 + \sqrt{6}$ (4) $3\sqrt{2} - \sqrt{3} - \sqrt{6}$
Official Ans. by NTA (2)
7. The lowest integer which is greater than
 $\left(1 + \frac{1}{10^{100}}\right)^{10^{00}}$ is ______.
(1) 3 (2) 4 (3) 2 (4) 1
Official Ans. by NTA (1)
8. The value of the integral $\int_{-1}^{1} \log(x + \sqrt{x^2 + 1}) dx$ is:
(1) 2 (2) 0 (3) -1 (4) 1
Official Ans. by NTA (2)
9. Let a, b and c be distinct positive numbers. If
the vectors $a\hat{i} + a\hat{j} + c\hat{k}, \hat{i} + \hat{k}$ and $c\hat{i} + c\hat{j} + b\hat{k}$ are
co-planar, then c is equal to:
(1) $\frac{2}{\frac{1}{4} + \frac{1}{b}}$ (2) $\frac{a + b}{2}$ (3) $\frac{1}{a} + \frac{1}{b}$ (4) \sqrt{ab}
Official Ans. by NTA (4)
10. If [x] be the greatest integer less than or equal to x,
then $\sum_{n=8}^{100} \left[\frac{(-1)^n n}{2}\right]$ is equal to:
(1) 0 (2) 4 (3) -2 (4) 2
Official Ans. by NTA (2)
11. The number of distinct real roots of
 $\begin{vmatrix} \sin x \cos x \cos x \\ \cos x \sin x \cos x \end{vmatrix} = 0$ in the interval
 $\cos x \cos x \sin x \end{vmatrix} = 0$ in the interval
 $\cos x \cos x \sin x \end{vmatrix}$
 $-\frac{\pi}{4} \le x \le \frac{\pi}{4}$ is:
(1) 4 (2) 1 (3) 2 (4) 3
Official Ans. by NTA (2)
12. If $|\vec{a}| = 2, |\vec{b}| = 5$ and $|\vec{a} \times \vec{b}| = 8$, then $|\vec{a} \cdot \vec{b}|$ is equal
to:

JEE Exam Solution

(1) 6

(2) 4

Official Ans. by NTA (1)

(4) 5

(3) 3

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The number of real solutions of the equation, 13. $x^{2} - |x| - 12 = 0$ is: (1) 2(2)3(4) 4(3)1Official Ans. by NTA (1) 14. Consider function $f: A \rightarrow B$ and $g: B \rightarrow C$ (A, B, C \subseteq **R**) such that $(gof)^{-1}$ exists, then: (1) f and g both are one-one (2) f and g both are onto (3) f is one-one and g is onto (4) f is onto and g is one-one Official Ans. by NTA (3) **15.** If $P = \begin{bmatrix} 1 & 0 \\ \frac{1}{2} & 1 \end{bmatrix}$, then P^{50} is: $(1)\begin{bmatrix}1&0\\25&1\end{bmatrix}$ $(2)\begin{bmatrix}1&50\\0&1\end{bmatrix}$ $(3)\begin{bmatrix} 1 & 25\\ 0 & 1 \end{bmatrix} \qquad (4)\begin{bmatrix} 1 & 0\\ 50 & 1 \end{bmatrix}$

Official Ans. by NTA (1)

16. Let x be a random variable such that the probability function of a distribution is given by

$$P(X = 0) = \frac{1}{2}, P(X = j) = \frac{1}{3^{j}}$$
 (j = 1, 2, 3, ..., ∞).

Then the mean of the distribution and P(X is positive and even) respectively are:

(1)
$$\frac{3}{8}$$
 and $\frac{1}{8}$
(2) $\frac{3}{4}$ and $\frac{1}{8}$
(3) $\frac{3}{4}$ and $\frac{1}{9}$
(4) $\frac{3}{4}$ and $\frac{1}{16}$

Official Ans. by NTA (2)

17. If a tangent to the ellipse $x^2 + 4y^2 = 4$ meets the tangents at the extremities of its major axis at B and C, then the circle with BC as diameter passes through the point :

(1)
$$(\sqrt{3},0)$$
 (2) $(\sqrt{2},0)$ (3) (1, 1) (4) (-1, 1)

Official Ans. by NTA (1)

18. Let the equation of the pair of lines, y = px and y = qx, can be written as (y - px) (y - qx) = 0. Then the equation of the pair of the angle bisectors of the lines $x^2 - 4xy - 5y^2 = 0$ is:

(1) $x^{2} - 3xy + y^{2} = 0$ (2) $x^{2} + 4xy - y^{2} = 0$ (3) $x^{2} + 3xy - y^{2} = 0$ (4) $x^{2} - 3xy - y^{2} = 0$ Official Ans. by NTA (3) Å

$$(1) 1 (2) 4 (3) 2 (4) 3$$

Official Ans. by NTA (3)

20. Let y = y(x) be the solution of the differential equation $xdy = (y + x^3 \cos x)dx$ with $y(\pi) = 0$, then

$$y\left(\frac{\pi}{2}\right)$$
 is equal to:

1)
$$\frac{\pi^2}{4} + \frac{\pi}{2}$$
 (2) $\frac{\pi^2}{2} + \frac{\pi}{4}$
3) $\frac{\pi^2}{2} - \frac{\pi}{4}$ (4) $\frac{\pi^2}{4} - \frac{\pi}{2}$

Official Ans. by NTA (1)

SECTION-B

1. Let $n \in \mathbf{N}$ and $[\mathbf{x}]$ denote the greatest integer less than or equal to \mathbf{x} . If the sum of (n + 1) terms ${}^{n}C_{0}, 3 \cdot {}^{n}C_{1}, 5 \cdot {}^{n}C_{2}, 7 \cdot {}^{n}C_{3}, \dots$ is equal to $2^{100} \cdot 101$,

then
$$2\left[\frac{n-1}{2}\right]$$
 is equal to _____.

Official Ans. by NTA (98)

2. Consider the function $f(x) = \frac{P(x)}{\sin(x-2)}, x \neq 2$ = 7, x = 2

> Where P(x) is a polynomial such that P''(x) is always a constant and P(3) = 9. If f(x) is continuous at x = 2, then P(5) is equal to

Official Ans. by NTA (39)

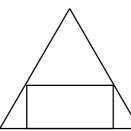
3. The equation of a circle is

 $\operatorname{Re}(z^2) + 2 (\operatorname{Im}(z))^2 + 2\operatorname{Re}(z) = 0$, where z = x + iy. A line which passes through the center of the given circle and the vertex of the parabola, $x^2 - 6x - y + 13 = 0$, has y-intercept equal to _____.

Official Ans. by NTA (1)

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If a rectangle is inscribed in an equilateral triangle 4. of side length $2\sqrt{2}$ as shown in the figure, then the square of the largest area of such a rectangle is



Official Ans. by NTA (3)

If $(\vec{a}+3\vec{b})$ is perpendicular to $(7\vec{a}-5\vec{b})$ and 5. $(\vec{a}-4\vec{b})$ is perpendicular to $(7\vec{a}-2\vec{b})$, then the angle between \vec{a} and \vec{b} (in degrees) is _____

Official Ans. by NTA (60)

6. Let a curve y = f(x) pass through the point $(2, (\log_2 2)^2)$ and have slope $\frac{2y}{x \log_2 x}$ for all positive real value of x. Then the value of f(e) is equal to_

Official Ans. by NTA (1)

If a + b + c = 1, ab + bc + ca = 2 and abc = 3, then 7. the value of $a^4 + b^4 + c^4$ is equal to _____.

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Official Ans. by NTA (13)

8. A fair coin is tossed n-times such that the probability of getting at least one head is at least 0.9. Then the minimum value of n is _____

Official Ans. by NTA (4)

If the co-efficient of x^7 and x^8 in the expansion of 9.

 $\left(2+\frac{x}{2}\right)^{n}$ are equal, then the value of n is equal to

Official Ans. by NTA (55)

10. If the lines
$$\frac{x-k}{1} = \frac{y-2}{2} = \frac{z-3}{3}$$
 and

 $\frac{x+1}{3} = \frac{y+2}{2} = \frac{z+3}{1}$ are co-planar, then the value of k is _____

Official Ans. by NTA (1)