

**MATHEMATICS**

1.  $\frac{dy}{dx} + 2y = \sin 2x$  and  $y(0) = \frac{3}{4}$  then value of  $y\left(\frac{\pi}{2}\right)$  is

**Ans.**  $\left(\frac{1}{4} + e^{-\pi}\right)$

**Sol.**  $\frac{dy}{dx} + 2y = \sin 2x$

$$\frac{d}{dx}(y \cdot e^{2x}) = e^{2x} \sin 2x$$

$$y \cdot e^{2x} = \int e^{2x} \sin 2x dx + c$$

$$y \cdot e^{2x} = \frac{1}{2} \left( \frac{e^{2x}(\sin 2x - \cos 2x)}{2} \right) + c$$

$$y(0) = \frac{3}{4}$$

$$\Rightarrow \frac{3}{4} = \frac{1}{4}[-1] + c$$

$$\boxed{c=1}$$

$$\therefore y = \frac{1}{4}(\sin 2x - \cos 2x) + e^{-2x}$$

$$y\left(\frac{\pi}{2}\right) = \frac{1}{4}(0 - (-1)) + e^{-2(\pi/2)}$$

$$y\left(\frac{\pi}{2}\right) = \frac{1}{4} + e^{-\pi}$$

2. Let  $f(x) = x^5 + x^4 + x^3 + 3x + 1$  and  $f(g(x)) = x$  then value of  $\frac{g(7)}{g'(7)}$  is

**Ans.** (15)

**Sol.**  $f(g(x)) = x$  ,  $f'(x) = 5x^4 + 4x^3 + 3x^2 + 3$

$$f'(g(x)) = \frac{1}{g'(x)} , f'(1) = 15$$

$$g'(7) = \frac{1}{f'(1)} = \frac{1}{15}$$

$$g(7) = 1$$

$$\therefore \frac{g(7)}{g'(7)} = 15$$

3. Find term independent of x in  $(1 - x + 2x^2) \left( 3x^2 + \frac{1}{x^3} \right)^9$

**Ans.**  $({}^9C_4 \times (3)^5 \times 2)$

**Sol.**  $T_{r+1} = {}^9C_r (3)^{9-r} \frac{x^{18-2r}}{x^{3r}}$



$$= {}^9C_r (3)^{9-r} x^{18-5r}$$

$$18 - 5r = 0,$$

$$5r = 18$$

$$18 - 5r = -1;$$

$$5r = 19$$

$$18 - 5r = -2$$

$$5r = 20$$

$$r = 4$$

$$\text{Term} = {}^9C_4 \times (3)^5 \times 2$$

4. Area bounded by  $Y = x^2 - 5x$  &  $Y = 7x - x^2$

Ans. 72

Sol.  $x^2 - 5x = 7x - x^2$

$$2x^2 - 12x = 0$$

$$x = 0, 6$$

$$\text{Area} = \left| \int_0^6 (x^2 - 5x - 7x + x^2) dx \right|$$

$$= \left| \int_0^6 2x^2 - 12x dx \right|$$

$$= \left| 2 \cdot \frac{x^3}{3} - \frac{12x^2}{2} \right|_0^6$$

$$= |2.36 \times 2 - 6.6^2|$$

$$= 6^2 \times 2$$

$$= 72$$

5. Given that  $\frac{1}{1.2} + \frac{1}{2.3} + \dots + \frac{1}{99.100} = n$  and  $\frac{1}{\sqrt{1+\sqrt{2}}} + \frac{1}{\sqrt{2+\sqrt{3}}} + \dots + \frac{1}{\sqrt{99+\sqrt{100}}} = m$  find  $(m, n)$

Ans.  $(9, \frac{100}{101})$

Sol.  $n = \sum \frac{1}{r(r+1)} = \sum_{r=1}^{100} \frac{1}{r} - \frac{1}{r+1}$

$$= 1 - \frac{1}{101} = \frac{100}{101}$$

$$m = \frac{\sqrt{2}-1}{1} + \frac{\sqrt{3}-\sqrt{2}}{1} + \dots + \frac{\sqrt{100}-\sqrt{99}}{1}$$

$$= \sqrt{100} - 1 = 9$$

$(9, \frac{100}{101})$

6. Find the value of  $|AA^T (\text{adj}4A)^{-1} (\text{adj}4B) (\text{adj}AB)^{-1}|$  if  $|A| = 2, |B| = 3$ . (Given A is  $3 \times 3$  matrix)

Ans.  $(\frac{1}{4})$

Sol.  $|AA^T (\text{adj}4A)^{-1} (\text{adj}4B) (\text{adj}AB)^{-1}|$

$$\Rightarrow |A|^2 \frac{1}{(4^2)^3 \cdot |A|^2} \cdot (4^2)^3 |B|^2$$



$$\frac{1}{|\text{adj}(AB)|}$$

$$= |B|^2 \times \frac{1}{|B|^2 |A|^2} = \frac{1}{4}$$

7. Find the value of I, if  $I = \int_{-\pi}^{\pi} \frac{2y \sin y}{1 + \cos^2 y} dy$

Ans.  $(\pi^2)$

Sol.  $I = \int_{-\pi}^{\pi} \frac{2y \sin y}{1 + \cos^2 y} dy = \int_0^{\pi} \frac{4y \sin y}{1 + \cos^2 y} dy$

$$I \Rightarrow \int_0^{\pi} \frac{4(\pi - y) \sin y}{1 + \cos^2 y} dy$$

$$2I = 4\pi \int_0^{\pi} \frac{\sin y}{1 + \cos^2 y} dy$$

$$2I = 4\pi \left( -\tan^{-1} \cos y \right) \Big|_0^{\pi}$$

$$I \Rightarrow -2\pi \left( \tan^{-1} \cos \pi - \tan^{-1} \cos 0 \right)$$

$$I \Rightarrow -2\pi \left( -\pi / 4 - \pi / 4 \right)$$

$$I \Rightarrow -2\pi \left( -\pi / 2 \right)$$

$$\boxed{I = \pi^2}$$

8.  $I = \int_0^{\pi/4} \frac{136 \sin x}{5 \sin x + 3 \cos x} dx$

Ans.  $\left( 5\pi - 6 \ln \left( \frac{32}{9} \right) \right)$

Sol.  $I = \frac{136}{34} \int_0^{\pi/4} \frac{5(5 \sin x + 3 \cos x) - 3(5 \cos x - 3 \sin x)}{5 \sin x + 3 \cos x} dx$

$$I = \frac{136}{34} \left( 5 \frac{\pi}{4} - 3 \ln |5 \sin x + 3 \cos x| \Big|_0^{\pi/4} \right)$$

$$= 4 \left( \frac{5\pi}{4} - 3 \ln \left( \frac{4\sqrt{2}}{3} \right) \right)$$

$$= 5\pi - 6 \ln \left( \frac{32}{9} \right)$$

9. If 4 dice are rolled, then find probability of their sum comes out to be 16.

Ans.  $\left( \frac{125}{6^4} \right)$

Sol.  $x + y + z + w = 16$

$$x' + y' + z' + w' = 12$$

$$\text{fav} = {}^{15}C_3 - ({}^9C_3 \times 4) + ({}^4C_2) \times 1$$



$$= \frac{15c_3 - 9c_3 \times 4 + 4^2 c_2}{6^4} = \frac{125}{6^4}$$

10. Let Set  $S = \{1, 2, 3, \dots, 8\}$  and there are multiple quadratic equation of the form of  $ax^2 + bx + c = 0$  where  $a, b, c \in S$ . Find the probability such that a randomly chosen quadratic equation have equal roots.

Ans.  $(\frac{1}{64})$

<b>Sol.</b>	a	b	c	
	1	2	2	$D = b^2 - 4ac$
	2	4	2	$P(A) = \frac{8}{8^3} = \frac{1}{64}$
	4	4	1	
	1	4	4	
	3	6	3	
	4	8	4	
	8	8	2	
	2	8	8	

11.  $|x||x - 2| - |x - 1| - 6 = 0$  and sum of real solution of x.

Ans. (2)

Sol.  $x \geq 2$ ;  
 $x(x-2) - x + 1 - 6 = 0$   
 $x^2 - 3x - 5 = 0$   
 $x = \frac{3 \pm \sqrt{29}}{2}$   
 $x_1 = \frac{3 + \sqrt{29}}{2}$

II.  $1 < x < 2$   
 $x(2-x) - x + 1 - 6 = 0$   
 $-x^2 + x - 5 = 0$   
 $x^2 - x + 5 = 0$   
 $D < 0$  (No Solution).

III.  $0 < x < 1$   
 $x(2 - x) + x - 1 - 6 = 0$   
 $2x - x^2 + x - 7 = 0$   
 $-x^2 + 3x - 7 = 0$   
 $x^2 - 3x + 7 = 0$   
 $D > 0$  (No Solution)

IV.  $x < 0$   
 $x^2 - x - 1 - 6 = 0$



$$x^2 - x - 7 = 0$$

$$x = \frac{+1 \pm \sqrt{29}}{2} \therefore x_2 = \frac{+1 - \sqrt{29}}{2},$$

Hence sum of solution

$$= x_1 + x_2$$

$$= \frac{3 + \sqrt{29} + 1 - \sqrt{29}}{2}$$

$$= 2$$

12.  $f(x) = \lim_{t \rightarrow x} \frac{t^2 f(x) - x^2 f(t)}{t - x}$ ,  $f(1) = 1$ , find the value of  $2f(2) + 3f(3)$

Ans. (20)

Sol.  $f'(x) = \lim_{t \rightarrow x} \frac{2tf(x) - x^2 f'(t)}{1}$

$$f'(x) = 2xf(x) - x^2 f'(x)$$

$$\Rightarrow f'(x) = \frac{2xf(x)}{1 + x^2}$$

$$\Rightarrow \int \frac{f'(x)}{f(x)} dx = \int \frac{2x}{1 + x^2} dx$$

$$\Rightarrow \ln(f(x)) = \ln|1 + x^2| + c$$

$$c = -\ln 2$$

$$\Rightarrow \ln(f(x)) = \ln\left(\frac{1 + x^2}{2}\right)$$

$$\Rightarrow \left\{ f(x) = \frac{1}{2}(1 + x^2) \right\}$$

$$\Rightarrow f(2) = 5/2, f(3) = \frac{10}{2}$$

$$\Rightarrow f(2) + 3f(3) = 5 + \frac{30}{2} = 20$$

13.  $f : A \rightarrow B, A = \{1, 2, 3, \dots, 8\}, B = \{1, 2, \dots, 8\}$ , find the number of one-one function from A to B such that  $f(1) + f(3) = 14$ .

Ans.  $(2 \times 6!)$

Sol.  $\{1, 2, \dots, 8\} \quad \{1, 2, \dots, 8\}$

$$f(1) + f(3) = 14$$

One One

$$8 \quad 6 \quad \rightarrow \quad 6!$$

$$7 \quad 7 \quad \rightarrow \quad \times$$

$$6 \quad 8 \quad \rightarrow \quad 6!$$

$$= 2 \times 6!$$

14. If lines  $\frac{x-3}{3} = \frac{2y-1}{4\lambda+1} = \frac{4-z}{1}$  and  $\frac{x-3}{3\mu} = \frac{1-2y}{-4} = \frac{z-4}{7}$  are perpendicular, then find value of  $9\mu + 4\lambda$ .



Ans. (6)

Sol. D.R's are  $\langle 3, \frac{4\lambda + 1}{2}, -1 \rangle$  &  
 $\langle 3\mu, 2, 7 \rangle$   
 $\Rightarrow 9\mu + 4\lambda + 1 - 7 = 0$   
 $9\mu + 4\lambda = 6$

15.  $f(x) = \sin 2x + c + \frac{2}{\pi}(x^2 + x), x \in \left[0, \frac{\pi}{2}\right]$

Statement-1:  $f(x)$  increasing in  $(0, \pi/2)$

Statement-2:  $f'(x)$  decreasing in  $(0, \pi/2)$ .

Ans. (1 is right; 2 is wrong)

Sol.  $f'(x) = 2\cos 2x + \frac{2}{\pi}(2x + 1) \rightarrow$  always positive in  $\left(0, \frac{\pi}{2}\right)$

$f''(x) = -4\sin 2x + \frac{4}{\pi}$

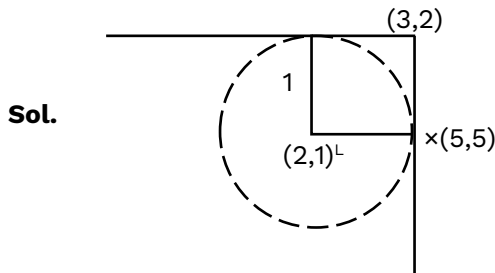
$= 4\left(\frac{1}{\pi} - \sin 2x\right) \rightarrow$  Can be positive or negative in  $\left(0, \frac{\pi}{2}\right)$

So, I<sup>st</sup> is right, II<sup>nd</sup> is wrong.

16. Given a circle of radius 1 such that it touches the normals drawn from (3, 2) to the coordinate axis. Find minimum distance of circle from point (5, 5)

- (1) 4                                      (2)  $7\sqrt{2}$                                       (3)  $4\sqrt{2}$                                       (4)  $5\sqrt{2}$

Ans. (1)



minimum distance  
 $= CP - r$   
 $= \sqrt{9 + 16} - 1$   
 $= 4$

17. Suppose  $\theta \in [0, \pi/4]$  is a solution of  $4\cos\theta - 3\sin\theta = 1$ , then  $\cos\theta =$

- (1)  $\frac{6 - \sqrt{6}}{3\sqrt{6} + 2}$                                       (2)  $\frac{4}{3\sqrt{6} + 2}$                                       (3)  $\frac{4}{3\sqrt{6} - 2}$                                       (4)  $\frac{4 - \sqrt{6}}{3\sqrt{6} + 2}$

Ans. (C)

Sol.  $4\cos\theta - 3\sin\theta = 1$   
 $(4\cos\theta - 1)^2 = (3\sin\theta)^2$   
 $16\cos^2\theta + 1 - 8\cos\theta = 9\sin^2\theta$   
 $16\cos^2\theta + 1 - 8\cos\theta = 9(1 - \cos^2\theta)$



$$25 \cos^2 \theta - 8 \cos \theta - 8 = 0$$

$$\cos \theta = \frac{8 \pm \sqrt{64 + 800}}{50}$$

$$\cos \theta = \frac{8 \pm \sqrt{864}}{50}$$

$$\cos \theta = \frac{8 + 12\sqrt{6}}{50}$$

$$\cos \theta = \frac{4 + 6\sqrt{6}}{25}$$

$$\cos \theta = \frac{-200}{25(4 - 6\sqrt{6})}$$

$$\cos \theta = \frac{4}{3\sqrt{6} - 2}$$

$$\cos \theta = \frac{8 - 12\sqrt{6}}{50}$$

$$\cos \theta = \frac{4 - 6\sqrt{6}}{25}$$

$$\cos \theta = \frac{-200}{25(4 + 6\sqrt{6})}$$

$$\cos \theta = \frac{-4}{2 + 3\sqrt{6}} \text{ Rejected}$$

18.  $f(x) = \frac{\sin 3x + \alpha \sin x - \beta \cos 3x}{x^3}; x \in \mathbb{R} - \{0\}$ .

If  $f(x)$  is continuous at  $x = 0$  then find  $|\alpha + \beta + f(0)|$ .

Ans. (7)

Sol. 
$$\lim_{x \rightarrow 0} \frac{\left(3x - \frac{27x^3}{3!}\right) + \left(\alpha x - \frac{\alpha x^3}{3!}\right) - \beta \left(1 - \frac{9x^2}{2!}\right)}{x^3}$$

$$3 + \alpha = 0 \quad \alpha = -3$$

$$\beta = 0$$

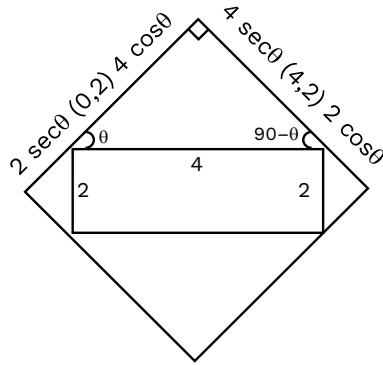
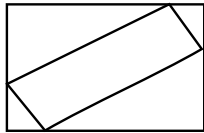
$$f(0) = \frac{-27}{6} + \frac{3}{6} = \frac{-24}{6} = -4$$

$$|-3 - 4| = 7$$

19. A rectangle ABCD is inscribed in another rectangle PQRS. Given the length and breadth of the ABCD are 2 & 4 respectively. The length and breadth of rectangle PQRS are  $a$  &  $b$  respectively. Find  $(a + b)^2$  so that area of PQRS is maximum.

Ans.  $(3\sqrt{2})$

Sol.



$$a = 4\sec\theta + 2\cos\theta, b = 4\cos\theta + 2\sec\theta$$

Area of PQRS(A)

$$= (4\sin\theta + 2\cos\theta) \times (4\cos\theta + 2\sin\theta)$$

$$= 8\cos 2\theta + 8\sin 2\theta + 20\cos\theta\sin\theta$$

$$= 8 + 10\sin 2\theta$$

For  $2\theta = 90^\circ$

$$A = 18 \qquad (a + b) = 6\sqrt{2}$$

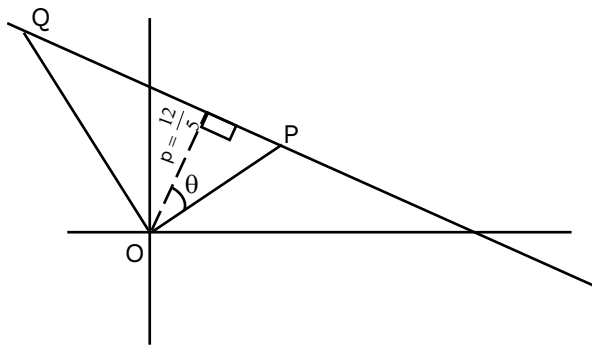
$$a = \frac{4}{\sqrt{2}} + \frac{2}{\sqrt{2}} = 3\sqrt{2} \qquad (a + b)^2 = 72$$

$$b = \frac{4}{\sqrt{2}} + \frac{2}{\sqrt{2}} = 3\sqrt{2}$$

20. If two lines passing through origin cuts the line  $3x + 4y = 12$ , at P & Q and POQ is right angle triangle, then minimum area is

Ans.  $(\frac{144}{25})$

Sol.



$$OP = \frac{12}{5}\sec\theta$$

$$OQ = \frac{12}{5}\operatorname{cosec}\theta$$

$$\text{Area of } \Delta OPQ = \frac{1}{2} \times \frac{12}{5} \times \frac{12}{5} \frac{1}{\cos\theta\sin\theta}$$

$$= \frac{144}{25\sin 2\theta}$$

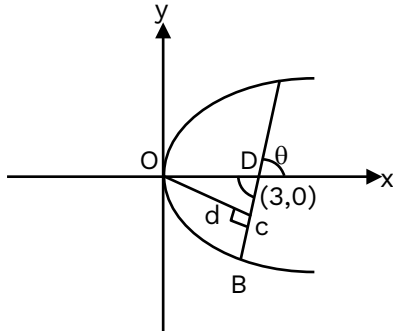
$$\text{Min area} = \frac{144}{25}$$



21. If the length of focal chord of  $y^2 = 12x$  is  $l$  and if the distance of the focal chord from origin is  $d$ , then  $ld^2$  is equal to

Ans. (108)

Sol.



length of focal chord  $\rightarrow 4a \operatorname{cosec}^2\theta$

$$4a \operatorname{cosec}^2\theta = l$$

$$12 \operatorname{cosec}^2\theta = l$$

$$\text{Focal chord equation} = \frac{y}{x-3} = \tan\theta$$

$$y = x \tan\theta - 3 \tan\theta$$

$$d = \left| \frac{3 \tan\theta}{\sqrt{1 + \tan^2\theta}} \right|$$

$$d = 3 \sin\theta$$

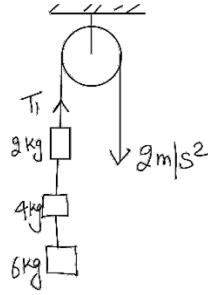
$$d^2 = 9 \sin^2\theta$$

$$ld^2 = 9 \operatorname{cosec}^2\theta \sin^2\theta \times 12$$

$$ld^2 = 108$$

PHYSICS

1. There is a pulley mass system, find tension in the string as shown in figure.



Ans. 144N

Sol.  $T_1 - 120 = 12 \times 2$   
 $T_1 = 144N$

2. Find ratio of electrostatic force and gravitational force between electron and proton.

Ans.  $2.27 \times 10^{39}$

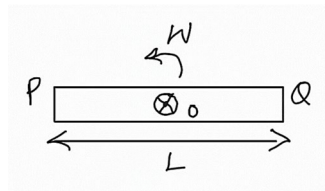
Sol.  $\frac{F_e}{F_g} = \frac{K.e^2}{G.m_e m_p}$   
 $= \frac{9 \times 10^9 \times (1.6 \times 10^{-19})^2}{6.67 \times 10^{-11} \times 9.1 \times 10^{-31} \times 1.67 \times 10^{-27}} = 2.27 \times 10^{39}$

3. If time period of pendulum at R distance from earth surface is 4 units. Find the time period of pendulum at 2R distance from earth's surface. (where R = radius of earth)

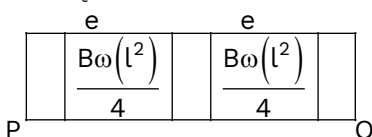
Ans. 6

Sol.  $T \propto \frac{1}{\sqrt{g}}$   
 $\frac{T_1}{T_2} = \sqrt{\frac{g_2}{g_1}} = \sqrt{\frac{g}{9} \times \frac{4}{g}} = \frac{2}{3}$   
 $T_2 = \frac{3T_1}{2} = \frac{3}{2} \times 4 = 6$

4. If magnetic field is perpendicular to the plane of rotation of rod then find potential difference between points P and Q in the given figure.

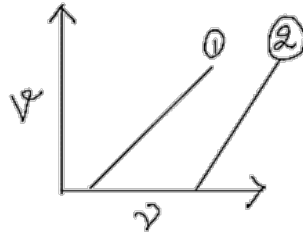


Ans. 0

Sol.  $V_P = V_Q$   
  
 $V_P = V_Q = 0$

5. **Statement-1:** slope is given by  $\frac{h}{e}$ .

**Statement-2:** comparison of kinetic energy ( $K_1 > K_2$ ) at constant frequency



**Ans.** So, statement -1 is correct.

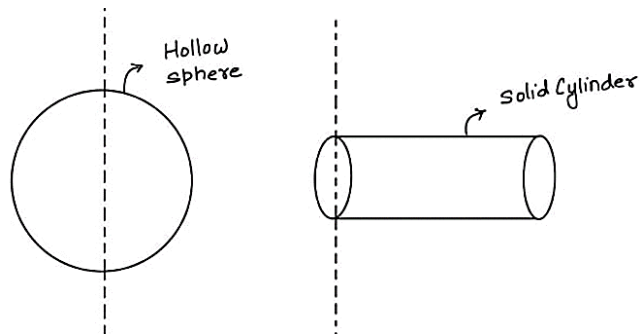
**Sol.**  $eV = h\nu - \phi$

$$V = \frac{h}{e}\nu - \phi$$

Slope of  $V$  vs  $\nu$  is  $h/e$

So, statement -1 is correct.

6. If the ratio of radius of gyration of hollow sphere and solid cylinder about the axis as shown in the figure is  $\sqrt{\frac{8}{x}}$ . Then value of  $x$  is:



**Ans.** 67

**Sol.**  $I_1 = \frac{2}{3}mR^2$

$$mk_1^2 = \frac{2}{3}mR^2$$

$$k_1 = \sqrt{\frac{2}{3}}R$$

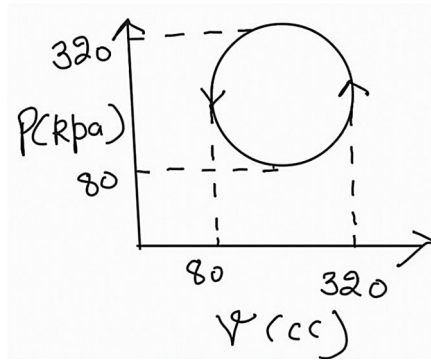
$$I_2 = \frac{mR^2}{4} + \frac{m(4R)^2}{3}$$

$$k_2 = \sqrt{\frac{67}{12}}R$$

$$\frac{k_1}{k_2} = \sqrt{\frac{8}{67}}$$

$$x = 67$$

7. An ideal gas undergoes a cyclic process given in the P-V curve. Find work done by gas in the given cyclic process.



Ans.  $\frac{144\pi}{10} \text{ J}$

Sol. Work done =  $\pi r^2$

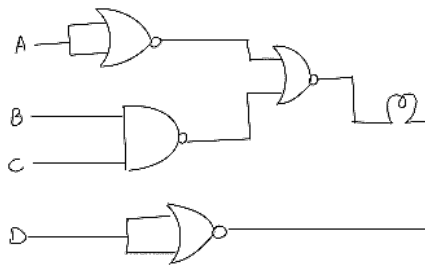
$$= \frac{\pi d^2}{4}$$

$$= \frac{(\pi)(240)^2}{4} (\text{kPa})(\text{cc})$$

$$= \frac{(\pi)(24)(24)(100)}{4} \text{kPa}(0.001)$$

$$= \frac{144\pi}{10} \text{ J}$$

8. Truth table for a logic gate system is given below. Choose the correct option for which bulb will glow.



	(a)	(b)	(c)	(d)
A	1	0	1	1
B	0	1	1	0
C	0	1	1	1
D	1	1	0	0

Ans. (D)

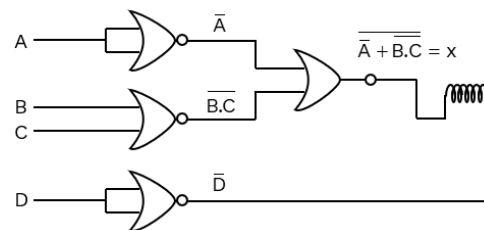
Sol. The bulb will glow if potential difference is 1

So, Potential difference =  $X - Y$

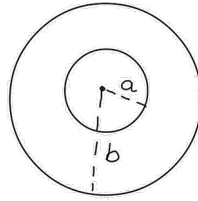
$$\text{Potential difference} = \overline{A + (B \cdot C)}$$

(Potential difference)<sub>D</sub> = 1

So, the bulb will glow in case (D).



9. There are two concentric conducting circular loops of radius  $a$  and  $b$ . If  $a \ll b$  then find the mutual inductance of the given system.



**Ans.**  $\frac{\mu_0}{2b} \cdot \pi a^2$

**Sol.**  $\phi = B \cdot \pi a^2$

$$\phi = \frac{\mu_0 \cdot i}{2b} \cdot \pi a^2$$

$$M i = \frac{\mu_0 \cdot i}{2b} \cdot \pi a^2$$

$$M = \frac{\mu_0}{2b} \cdot \pi a^2$$

10. In YDSE distance between two slits is 0.3 mm and distance of screen from plane of slits is 200 cm. If wavelength of light is used is  $5000\text{\AA}$  then find the distance of 3<sup>rd</sup> bright fringe from central maxima.

**Ans.** 1 cm

**Sol.**  $y = n \frac{D\lambda}{d}$

$$= \frac{3 \times 2 \times 5000 \times 10^{-10}}{0.3 \times 10^{-3}}$$

$$= 10^{-2} \text{m}$$

$$= 1 \text{ cm}$$

11. If a particle starts from rest with constant acceleration. Find the ratio of distance covered by particle in  $n^{\text{th}}$  second to the distance covered in  $(n - 1)^{\text{th}}$  second.

**Ans.**  $\frac{2n - 1}{2n - 3}$

**Sol.**  $u = 0, a = \text{constant}$

$$S_n = \frac{a}{2} (2n - 1)$$

$$S_{n-1} = \frac{a}{2} (2(n - 1) - 1)$$

$$\frac{S_n}{S_{n-1}} = \frac{2n - 1}{2n - 3}$$

12. If  $\mu$  represents energy density and  $G$  represents gravitational constant then find the dimension of  $\sqrt{\mu G}$ .

**Ans.**  $= LT^{-2}$

**Sol.**  $\sqrt{\frac{ML^2T^{-2}}{L^3} \cdot M^{-1} \cdot L^3 \cdot T^{-2}}$

$$= \sqrt{L^2 \cdot T^{-4}}$$

$$= LT^{-2}$$

**13.** There is a conducting wire of radius 4 mm whose resistance is given  $r = 2\Omega$ . Now radius is halved keeping the length of wire same, then find the resistance of new wire.

**Ans.**  $8\Omega$

**Sol.**  $r = 4 \text{ mm}$       $r = 2 \text{ mm}$

$$R = 2\Omega \quad \rho = \frac{\rho l}{\pi r^2}$$

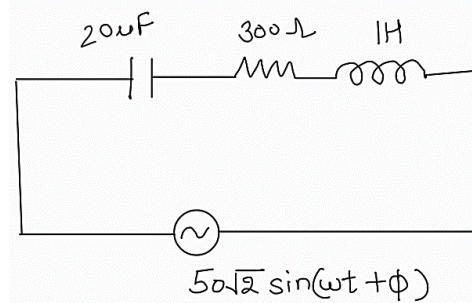
$$R = \frac{\rho l}{A}$$

$$R \propto \frac{1}{r^2}$$

$$\frac{R_1}{R_2} = \left(\frac{r_2}{r_1}\right)^2 = \left(\frac{2}{4}\right)^2$$

$$R_2 = 4R_1 = 8\Omega$$

**14.** In the given LCR circuit. Find the voltage across the capacitor. ( $\omega=100$ )



**Ans.** 50V

**Sol.**  $X_L = \omega L = 100 \times 1 = 100$

$$\omega = 100, \quad v_0 = 50\sqrt{2} \text{ (given)}$$

$$X_C = \frac{1}{\omega C} = \frac{10}{100 \times 200 \times 10^{-6}}$$

$$= 5 \times 10^2 = 500$$

$$I_0 = \frac{V_0}{Z}$$

$$Z = \sqrt{(100 - 500)^2 + (300)^2}$$

$$Z = \sqrt{400^2 + 300^2} = 500$$

$$I_0 = \frac{50\sqrt{2}}{500} = 0.141$$

$$V_{\text{rms(Cap)}} = \frac{I_0 \times C}{\sqrt{2}}$$

$$= \frac{(0.141)(500)}{\sqrt{2}}$$

$$= 50 \text{ V.}$$

15. **Statement-1:** Capillary tube is inserted in liquid and the level of liquid does not rise or fall then contact angle may be  $0^\circ$ .

**Statement-2:** Contact angle depends on property of liquid and solid.

- (1) Statement-1 and Statement-2 both are correct but 2<sup>nd</sup> statement is not correct explanation of 1<sup>st</sup> statement.
- (2) Statement-1 and Statement-2 both are correct but 2<sup>nd</sup> statement is correct explanation of 1<sup>st</sup> statement.
- (3) Statement-1 is correct and Statement-2 is wrong.
- (4) Statement-1 is incorrect and Statement-2 is correct.

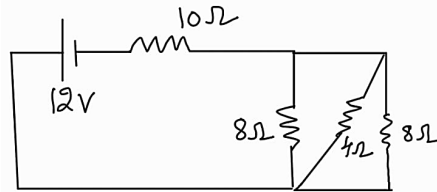
Ans. (4)

Sol. 
$$h = \frac{2T \cos \theta}{\rho r g}$$

If  $h = 0 \Rightarrow \cos \theta = 0$

$$\Rightarrow \theta = \frac{\pi}{2}$$

16. In the given circuit find equivalent resistance across the cell and current flowing through the cell (neglect internal resistance of cell).



Ans. 1A

Sol. 
$$\frac{1}{R_{eq'}} = \frac{1}{8} + \frac{1}{4} + \frac{1}{8}$$

$$\frac{1}{R_{eq'}} = \frac{4}{8}$$

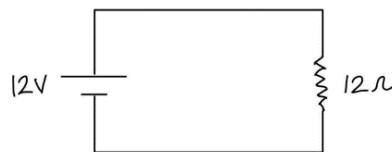
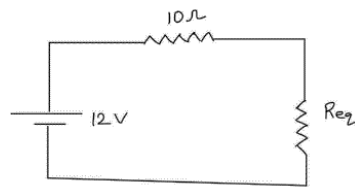
$$R_{eq'} = 2$$

$$R_{eq_{net}} = 12\Omega$$

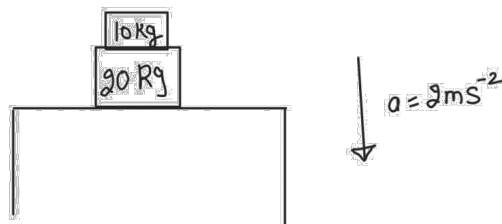
$$V = IR$$

$$\Rightarrow I = \frac{12}{12}$$

$$\Rightarrow I = 1A$$



17. There is a two-block system placed on a platform which is moving downward with an acceleration of  $2 \text{ m/s}^2$  then find the normal force on block by the platform.



Ans. 240 N

Sol. 
$$30 \text{ g} - N = (30 \times 2)$$

$$300 - N = 60$$

$$N = 240 \text{ N}$$

18. If  $2\vec{P} + 2\vec{Q} = \vec{r}_1$  and  $2\vec{Q} - 2\vec{P} = \vec{r}_2$  then angle between the resultant vector of  $\vec{r}_1 + \vec{r}_2$  and  $\vec{Q}$  is:

Ans. 0

Sol.  $\vec{r}_1 + \vec{r}_2 = 4\vec{Q}$

$(\vec{r}_1 + \vec{r}_2)$  is parallel to  $\vec{Q}$

Hence angle is  $= 0^\circ$

19. An electron is moving in an orbit, total energy of electron is E, then find the potential energy

Ans. 2E

Sol. T.E.  $= -\frac{kze^2}{2r}$

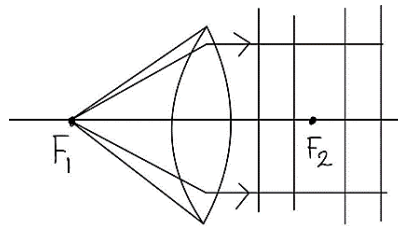
P.E.  $= -\frac{kze^2}{r}$

P.E.  $= 2$ T.E.

20. A point source is placed at the first principal focus of a convex lens. The shape of the wave front of light emerging from the convex lens is:

Ans. Planar wavefront

Sol. planar light emerging out of convex lens when a point source is placed at its focus.



21. Three capacitors having capacitance  $25\mu\text{F}$ ,  $45\mu\text{F}$  and  $30\mu\text{F}$  are connect in parallel and energy stored in the given combination is E.

Now the given capacitors are connected in series and energy stored in the given combination

is  $\frac{9E}{x}$ . Find the value of x (consider same power supply in both cases).

Ans. 86

Sol.  $E = \frac{1}{2}C_{\text{eq}}V^2$

For parallel combination,  $C_{\text{eq}} = 25 + 45 + 30 = 100 \mu\text{F}$

$E = \frac{1}{2} \times 100 \times V^2 = 50V^2 \mu\text{J}$

For series combination

$$\frac{1}{C_{\text{eq}}} = \frac{1}{25} + \frac{1}{45} + \frac{1}{30}$$

$$C_{\text{eq}} = \frac{450}{43}$$

$$E' = \frac{1}{2}C_{\text{eq}}V^2$$

$$E' = \frac{1}{2} \times \frac{450}{43} V^2$$

$$\frac{E'}{E} = \frac{450}{43 \times 100}$$



$$E' = \frac{9}{86}E$$

$$E' = \frac{9E}{x} \Rightarrow \boxed{x = 86}$$

**22.** Collision frequency of gas particles at 27°C is 2. What is the collision frequency of the gas particles at 127°C?

**Ans.**  $\frac{8}{\sqrt{3}}$

**Sol.**  $f \propto \sqrt{T}$

$$Z \propto \sqrt{300K}$$

$$Z' \propto \sqrt{400K}$$

$$\frac{Z}{Z'} = \frac{\sqrt{300}}{\sqrt{400}}$$

$$Z' = \frac{2}{\sqrt{3}} \times Z$$

**23.** Sun of mass  $M$  is at a distance  $a$  from earth surface. The mass and radius of earth are  $m$  and  $R$  respectively. Then chose the appropriate option. Match the column.

**Column-I**

**Column-II**

(1) Escape velocity

(a)  $-\frac{GMm}{2a}$

(2) Kinetic energy

(b)  $\frac{GMm}{2a}$

(3) Gravitational potential energy

(c)  $\sqrt{\frac{2GM}{a}}$

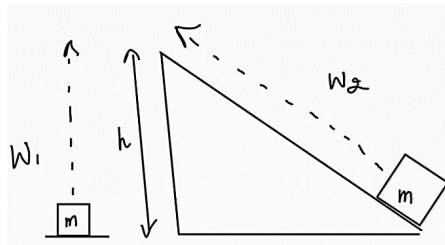
(4) Total energy

(d)  $-\frac{GMm}{a}$

**Ans.** (1)  $\rightarrow$  c, (2)  $\rightarrow$  a, (3)  $\rightarrow$  b, (4)  $\rightarrow$  d

**Sol.** Formula Based

**24.** A block is moved up on a smooth wedge inclined at 60° and another block is moved vertically upward upto same height, find the ratio of work done by gravitational force in both the cases.



**Ans.** 1

**Sol.**  $w_1 = mgh$

$$w_2 = mgh$$

$$\frac{w_1}{w_2} = 1$$



**25.** Potential difference between the plates of capacitor of capacitance  $12\mu\text{F}$  is  $40\text{V}$ . The frequency is  $40\text{KHz}$ . Find displacement current.

**Ans.**  $0.0381\text{A}$

**Sol.**  $C = 12\mu\text{f}$

$$V = 40\text{ V}$$

$$f = 40\text{kHz} = 40 \times 10^3\text{ Hz}$$

$$\frac{dv}{dt} = 2\pi fV$$

$$\frac{dv}{dt} = 2\pi \times 40 \times 10^3 \times 40$$

$$\frac{dv}{dt} = 3200\pi$$

$$I_d = c \frac{dv}{dt}$$

$$I_d = 12 \times 10^{-6} \times 3000\pi$$

$$I_d \approx 0.0381\text{A}$$

**26.** Find arithmetic mean of  $4.623$ ,  $4.6$ ,  $4.62$  and  $4.69$ . (Using significant figures)

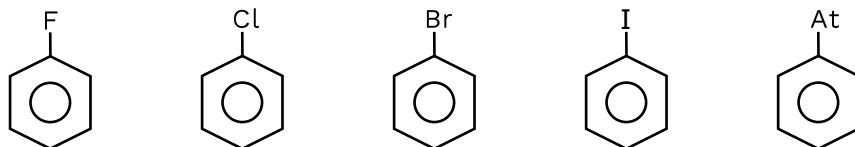
**Ans.**  $4.6$

**Sol.**  $\frac{4.623 + 4.6 + 4.62 + 4.69}{4} = 4.633$

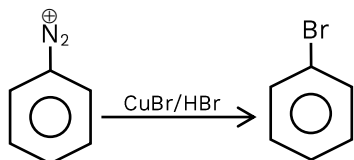
$= 4.6\text{ Ans.}$

CHEMISTRY

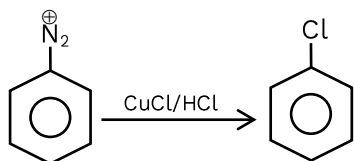
1. How many of the following can be prepared by Sandmeyer reaction:



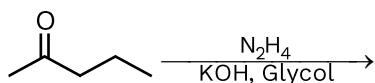
Ans. (02.00)



Sol.



2. Which of the following is the correct product for the given reaction



Ans. (1)

Sol. -Wolff- kishner reduction it reduces aldehyde & ketone into corresponding alkane.

3. Which of the following element show maximum oxidation state

- (1) Mn (2) Ti (3) Co (4) Na

Ans. (1)

Sol. Mn show maximum oxidation state +7.

4. Which of the following has lowest paramagnetic character in +2 oxidation state with water

- (1) Fe (2) Co (3) Ni (4) Mn

Ans. (3)

Sol.  $Fe^{2+} \rightarrow d^6$   $n = 4$

$Co^{2+} \rightarrow d^7$   $n = 3$

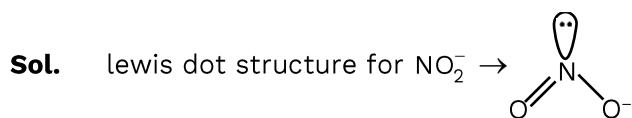
$Ni^{2+} \rightarrow d^8$   $n = 2$

$Mn^{2+} \rightarrow d^5$   $n = 5$

Where n is number of unpaired electrons. So,  $Ni^{2+}$  has lowest paramagnetic character.

5. In the lewis dot structure for  $NO_2^-$  total numbers of valance electron around nitrogen is:

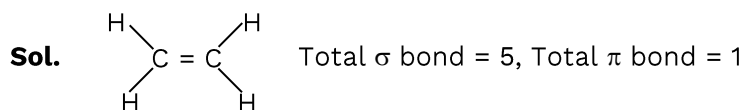
Ans. (08.00)



Total valance electron around nitrogen = 8

- 6.** Find the total numbers of  $\sigma$  and  $\pi$  bond in ethylene respectively  
 (1) 4,1 (2) 5,1 (3) 4,0 (4) 5,0

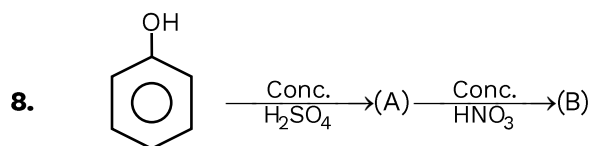
**Ans.** (06.00)



- 7.** Which of the following are correct statement(s) for given species.  
 $\text{O}^{2-}$ ,  $\text{F}^-$ ,  $\text{Na}^+$ ,  $\text{Mg}^{2+}$ .  
 (a)  $\text{O}^{2-}$  is largest in size  
 (b)  $\text{Mg}^{2+}$  is smallest in size  
 (c) All have same effective nuclear charge  
 (d) All are isoelectronic  
 (1) a, b and c (2) a, b and d (3) b,c and d (4) a, c and d

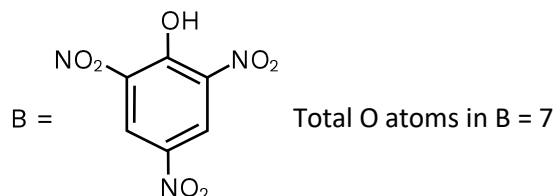
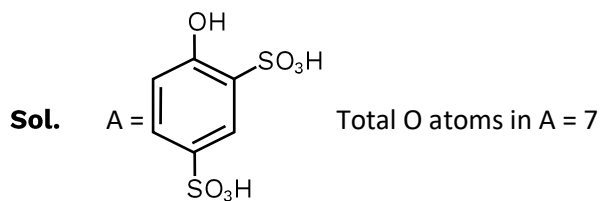
**Ans.** (2)

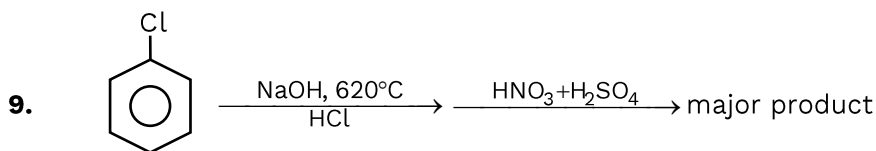
**Sol.** All have same number of electrons so they are isoelectronic  
 Order of ionic radii  $\text{O}^{2-} > \text{F}^- > \text{Na}^+ > \text{Mg}^{2+}$ .



Find sum of total number of O atom(s) in A and B

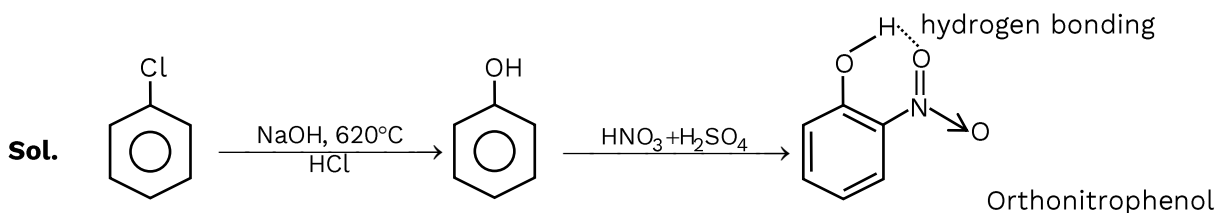
**Ans.** (14.00)





- (1) Orthonitrophenol (2) Paranitrophenol  
(3) Picric acid (4) Metanitrophenol

Ans. (1)



10. Which will give +ve Ninhydrin test

- (1) Cellulose (2) Starch  
(3) Polyvinyl chloride (4) Egg albumin

Ans. (4)

Sol. Ninhydrin test is given by amino acids and proteins.

- (1) Cellulose → Carbohydrate (2) Starch → Carbohydrate  
(3) Polyvinyl chloride → Polymer (4) Egg albumin → Protein

11. Correct order of boiling point for

- (P) Diethyl ether  
(Q) n-butanol  
(R) n-butane  
(S) ethylmethyl ketone  
(1) P > Q > R > S (2) Q > S > P > R (3) S > R > Q > P (4) S > Q > P > R

Ans. (2)

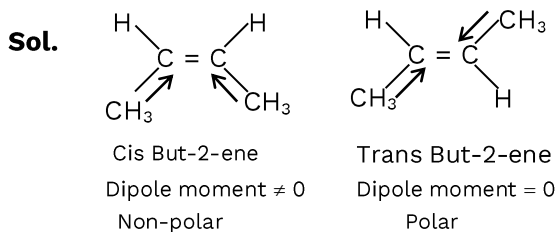
Sol. (P) Diethyl ether - dipole moment is not 0  
(Q) n-butanol - Hydrogen bonding  
(R) n-butane - dipole moment is 0  
(S) ethylmethyl ketone - dipole-dipole interaction

12. **Assertion:** Cis-but-2-ene is polar while trans but-2-ene is non polar.

**Reason:** Dipole moment of trans but-2-ene is zero.

- (1) Both A and R are correct and R is the correct explanation of A.  
(2) Both A and R are correct, but R is not the correct explanation of A.  
(3) A is correct but, R is incorrect.  
(4) R is correct but, A is incorrect.

Ans. (1)



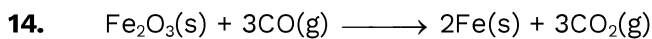
**13. Assertion :** For group 13 element stability of +1 oxidation state increases down the group

**Reason :** Atomic size of Ga is greater than Al.

- (1) Both, A and R, are true and R is the correct explanation of A
- (2) Both, A and R, are true but R is not the correct explanation of A
- (3) If A is true but R is false
- (4) If A is false but R is true

**Ans.** (3)

**Sol.** Due to inert pair effect +1 oxidation state increases down the group for group 13 element



Equilibrium does not shift according to Le-chatelier's principle

- (1) Removal of  $\text{CO}_2$
- (2) Addition of  $\text{CO}_2$
- (3) Removal of  $\text{CO}$
- (4) Addition of  $\text{Fe}_2\text{O}_3$

**Ans.** (4)

**Sol.** Equilibrium does not shift according to Le-chatelier's principle by Addition of  $\text{Fe}_2\text{O}_3$

**15.** Predict correct order of strength of ligands  $\text{Br}^-$ ,  $\text{F}^-$ ,  $\text{H}_2\text{O}$ ,  $\text{NH}_3$

- (1)  $\text{Br}^- < \text{H}_2\text{O} < \text{F}^- < \text{NH}_3$
- (2)  $\text{H}_2\text{O} < \text{Br}^- < \text{F}^- < \text{NH}_3$
- (3)  $\text{Br}^- < \text{F}^- < \text{H}_2\text{O} < \text{NH}_3$
- (4)  $\text{Br}^- < \text{H}_2\text{O} < \text{NH}_3 < \text{F}^-$

**Ans.** (3)

**Sol.** order of strength  $\text{Br}^- < \text{F}^- < \text{H}_2\text{O} < \text{NH}_3$

**16.** Molar conductivity of divalent cation and anion are 57 and 73  $\text{S cm}^{-1} \text{ mol}^{-1}$ . The molar conductivity of solution is \_\_\_\_\_

**Ans.** (130)

**Sol.**  $\Lambda_m = \Lambda_{\text{cation}} + \Lambda_{\text{anion}}$

**17.** For the reaction  $2\text{A} + \text{B} \rightarrow \text{C}$  is given

[A]	[B]	Rate
0.1	0.1	$6 \times 10^{-3}$
0.4	0.1	$12 \times 10^{-3}$
0.4	0.2	$48 \times 10^{-3}$

Find order reaction

**Ans.** (2.5)

**Sol.** Rate = k [A]<sup>x</sup>[B]<sup>y</sup>

$$\frac{6 \times 10^{-3}}{12 \times 10^{-3}} = \frac{[0.1]^x [0.1]^y}{[0.4]^x [0.1]^y}$$

$$\frac{1}{2} = \left[ \frac{0.1}{0.4} \right]^x$$

$$\frac{1}{2} = \left( \frac{1}{4} \right)^x$$

$$x = \frac{1}{2}$$

$$\frac{12 \times 10^{-3}}{48 \times 10^{-3}} = \frac{[0.4]^x [0.1]^y}{[0.4]^x [0.2]^y}$$

$$\frac{1}{4} = \left( \frac{1}{2} \right)^y$$

$$y = 2$$

So, order of reaction is 2.5

**18.** Most abundant isotopes of boron has X number of neutrons

B + O<sub>2</sub> → Oxidation number of boron (Y)

Find X + Y?

**Ans.** (9)

**Sol.** Isotope of B = <sub>5</sub>B<sup>11</sup>

Oxidation No. = +3

$$X = 6$$

$$Y = 3$$

$$X + Y = 9$$

**19.** Find the spin only magnetic moment of strongest oxidizing Agent ?

(1) Ti<sup>+2</sup>

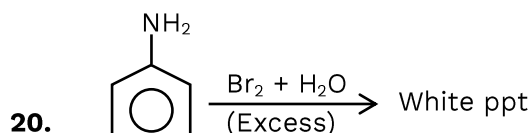
(2) V<sup>+2</sup>

(3) Mn<sup>+2</sup>

(4) Co<sup>+3</sup>

**Ans.** (4)

**Sol.**  $S = \sqrt{n(n+2)}$

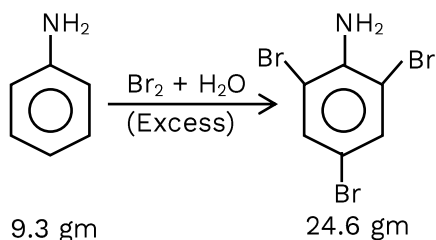


9.3 gm

24.6 gm

Find out % yield of white ppt product

**Ans.** (70%)



**Sol.** 9.3 gm

Moles = 0.1

$$\% \text{ yield} = \frac{0.07}{0.1} \times 100 = 70\%$$

24.6 gm

Moles = 0.07

**21.** Which of the following cation will give green colour in reducing flame in borax bead test

- (1) Iron                      (2) Cobalt                      (3) Manganese                      (4) Nickel

**Ans.** (1)

**Sol.** Iron cation will give green colour in reducing flame in borax bead test

**22.** Which postulate of Dalton's theory is wrong

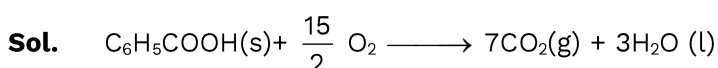
- (1) Matter consist of indivisible atoms  
 (2) All atoms of a given element have identical properties but different masses  
 (3) Compounds are formed when atoms of different elements combines in a fixed ratio  
 (4) Chemical reaction involves reorganisation of atoms

**Ans.** (2)

**Sol.** Theory Based

**23.** The heat of combustion of solid benzoic acid at constant volume is  $-321.30\text{K}$  at  $27^\circ\text{C}$ . The heat of combustion at constant pressure  $(-321.30-x)\text{KJ}$  the value of  $x$  is.

**Ans.** (1.25)



$$\Delta H = \Delta U + \Delta n_g RT$$

$$= -321.3 + \left(-\frac{1}{2}\right) \times \frac{8.314}{1000} \times 300$$

$$= -321.3 - 1.25$$

$$= -322.55 \frac{\text{KJ}}{\text{mol}}$$